Estimating the Price Elasticity of Gasoline Demand in Correlated Random Coefficient Models with Endogeneity

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Abstract

We propose a per-cluster instrumental variables approach (PCIV) for estimating linear correlated random coefficient models in the presence of contemporaneous endogeneity and two-way fixed effects. This approach estimates heterogeneous effects and aggregates them to population averages. We demonstrate consistency, showing robustness over standard estimators, and provide analytic standard errors for robust inference. In Monte Carlo simulation, PCIV performs relatively well in finite samples in either dimension. We apply PCIV in estimating the price elasticity of gasoline demand using state fuel taxes as instrumental variables. We find significant elasticity heterogeneity and more elastic gasoline demand on average than with standard estimators.

Keywords: instrumental variables, per-cluster estimation, heterogeneous effects, population average effects, local average treatment effects.

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1 Introduction

The price elasticity of the demand for gasoline is an integral parameter for climate mitigation policy, modeling energy and automotive markets, and urban planning (Dahl, 1986; Dahl and Sterner, 1991; Espey, 1998). However, several econometric issues complicate the estimation of this important parameter. First, gasoline prices and the volume purchased likely depend upon each other through the interaction of supply and demand forces. Second, quantities, prices, and taxes trend over time. Finally, there is marked heterogeneity across this market with geography, industry composition, population density, demographic composition, transportation substitutes, economic climates, regulations, and tax rates each varying across states. Assuming homogeneous elasticities across this landscape seems questionable (Wadud et al., 2010; Frondel et al., 2012; Blundell et al., 2012; Hausman and Newey, 2016; Levin et al., 2017), and ignoring this likely heterogeneity when using standard estimators may cause bias. As a result, we introduce an approach to estimate linear correlated random coefficient models in the presence of contemporaneous endogeneity and two-way fixed effects. The method we propose has the added benefit of estimating the distribution of heterogeneous effects rather than only the mean.

Our estimator for the price elasticity of gasoline demand has broader applicability than our current context. Empirical work often aims to identify the population average effect (PAE)—the average causal relationship between two variables over an entire population of interest. Heterogeneous effects within the population are inherent in these conceptualizations and often hold economic significance (Heckman and Vytlacil, 1998). These correlated random coefficient (CRC) models, however, add complications for estimation even when

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1 This method is well suited to settings in which data is grouped into moderately large clusters, endogeneity is plausible, and where heterogeneous effects are likely such as in development and political economy (Miguel et al., 2004), industrial organization and energy markets, (Bushnell et al., 2008), public finance and education (Jackson et al., 2016), labor economics (Kostol and Mogstad, 2014), and trade (Feyrer, 2019).

2 While Heckman and Vytlacil (1998) coined the helpful phrase “correlated random coefficients models,” similar models originate much earlier with examinations appearing in Rubin (1950); Klein (1953); Kuh (1959); Swamy (1971); Mundlak (1978); Raj et al. (1980), and Chamberlain (1992).
regressors are otherwise exogenous (Wooldridge 2005; Arellano and Bonhomme 2011; Graham and Powell 2012; Bates et al., 2014). This effect heterogeneity may produce even further complications in so-called two-way fixed effects models with multiple time periods (De Chaisemartin and d’Haultfoeuille 2020; Borusyak et al. 2021; Callaway and SantâAnna 2021; Goodman-Bacon 2021; Sun and Abraham 2021; Wooldridge 2021).

Applied economic researchers, however, often work in settings where some explanatory variables may be correlated with the error term (for instance due to omitted variables or simultaneity). In those cases when a valid instrument is available, it is typical for researchers to turn to pooled two-stage least squares (P2SLS) or fixed effects instrumental variables (FEIV) estimators. Murtazashvili and Wooldridge (2008) provide the conditions under which a general class of FEIV estimators consistently estimate PAEs with endogenous regressors. They find that in CRC models, consistency requires the assumption that the heterogeneous slopes are uncorrelated with the covariance between the instruments and endogenous regressors.\(^3\)

This restriction may not hold in many cases. Consider the local average treatment effect (LATE) framework from Imbens and Angrist (1994). The instrument is not relevant for some individual clusters within the population, and treatment effects differ on average by whether the individual is moved toward treatment by the instrument. Such a setting would prevent FEIV from consistently estimating the average treatment effect (ATE). Even in a population in which all are influenced by a valid instrument, if effect heterogeneity correlates with the strength of the instrument within-cluster, FEIV would continue to fail to estimate the ATE among a population of compliers with the instrument (the LATE).

Fernández-Val and Lee (2013) introduce an approach of estimating cluster-specific slopes and averaging over them.\(^4\) They iteratively apply generalized method of moments (GMM) estimators separately to the time series of each cluster. As the GMM approach is asymptotically biased, they introduce bias corrections. Per-cluster estimation, however, may be

\(^3\) P2SLS requires a similar restriction for consistency.

\(^4\) Kelejian (1974) also demonstrates that treating these random coefficients as fixed effects is useful for identification in such models with endogenous covariates.
taxing on the data, particularly when there are many covariates and relatively short panels. Designating some conditioning variables to have common coefficients may help. Fernández-Val and Lee (2013) preserves degrees of freedom for estimation by netting out the effects of covariates with common coefficients. They estimate this vector of common coefficients in an additional step within each iteration using time averages. Accordingly, parameters on variables that vary only across time cannot be identified, thus ruling out common applications such as two-way fixed effects models.

Our approach, which we term per-cluster instrumental variables (PCIV), in simple settings applies 2SLS estimation on a cluster-by-cluster basis before aggregating them. The general PCIV estimator accommodates differential cluster sizes and covariates with both heterogeneous and homogeneous slopes, allowing the dimension of the vector of covariates to exceed the number of observations per cluster ($T$), as in the presence of two-way fixed effects. We show that the asymptotic distribution of the estimator is normal and centered at the true parameter value without placing restrictions on the correlation between the explanatory variables and random coefficients. In each stage, we do this by first netting out cluster-specific slopes from the left-hand-side variables and variables with homogeneous slopes. Second, we pool over those residuals to consistently estimate homogeneous coefficients using both time-series and cross-sectional variation. We use those estimated common parameters to net out the effects of the covariates from the left-hand-side variables, which we regress on the variables with heterogeneous slopes again by cluster. We aggregate over those cluster-specific slopes using appropriate weights to estimate relevant parameters such as the PAE or LATE. We propose accompanying analytic standard errors that are robust to arbitrary within-cluster correlation. This approach can be viewed as extending an estimator described in Wooldridge (2010 Section 11.7.2) to account for endogeneity. Our Stata package pciv automates estimation using this approach both in cases with endogeneity and in cases where all regressors are strictly exogenous.
Due to the long panel and likely effect heterogeneity, the method is ideal for estimating the price elasticity of gasoline demand in the United States. We follow Davis and Kilian (2011); Blundell et al. (2012); Li et al. (2014); Hausman and Newey (2016); Coglianese et al. (2017); and Hoderlein and Vanhems (2018) in using state fuel taxes as our source of exogenous variation and use them to instrument for average state gasoline prices. Given the variation in state changes to gasoline taxes and the likely heterogeneity in gasoline demand, ignoring such heterogeneity may lead to inconsistent estimates. Accordingly, we perform estimation using standard approaches from the literature and the more robust PCIV approach. As earlier work relies on aging and discontinued data series, we update and bolster the analysis with novel data collection.

This analysis allows us to demonstrate additional advantages of PCIV estimation. First, we find that both the magnitude and significance of the results are sensitive to the methods used. The robust PCIV approach estimates a population average elasticity of the demand for gasoline of -0.4 to -0.6 whereas FEIV estimates range from -0.75 to -0.95. Second, PCIV provides the distribution of state-specific elasticities in addition to the mean effects. We see substantial heterogeneity in both. The standard deviation of state-specific elasticities are 38% of the mean elasticity. Third, in seeming violation of the key assumption for consistency of P2SLS and FEIV, we observe a meaningful correlation between the first-stage variation and the state-specific elasticity estimates. Fourth, we find a significant divergence between the implicit weighting of FEIV and the natural market share weights we employ with PCIV. Finally, as the instrument is not universally strong, we provide a LATE (-0.56) for the 46 states in which the instrument is strong, which is very close to the PAE though the LATE carries smaller standard errors.

We organize the remainder of the paper as follows. Section 2 introduces the econometric

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5Along with Davis and Kilian (2011); Li et al. (2014); and Coglianese et al. (2017), we rely on the U.S. Department of Energy, Energy Information Administration, Petroleum Marketing Monthly Report: Gasoline Prices by Formulation, Grade, Sales Type' for gasoline prices by state for 1989-2008. However, this series was discontinued in 2011. As a result, we add to this data state-by-month averages of at-the-pump gasoline prices collected from Gasbuddy.com.
model and the proposed estimator. Section 3 provides the main consistency results. Section 4 contains a Monte Carlo study showing that the PCIV estimator performs comparably to standard estimators in the ideal setting but outperforms P2SLS and FEIV when there is a correlation between effect heterogeneity and first-stage variation. We estimate the price elasticity of gasoline demand in Section 5 before concluding in Section 6.

2 Model specification and proposed estimator

Consider a correlated random coefficients (CRC) model as follows:

\[ y_{ij} = x_{1ij}b_i + x_{2ij}\delta + e_{ij}, \]

\[ x_{1ij} = z_{ij}\gamma_i + x_{2ij}\eta + u_{ij}, \quad i = 1, ..., n; \quad j = 1, ..., T, \quad (1) \]

where \( y_{ij} \) is the dependent variable of the \( j^{th} \) unit of a randomly sampled cluster \( i \) and \( e_{ij} \) is an idiosyncratic error. The \( 1 \times K \) vector, \( x_{1ij} \), includes 1 as well as covariates that may be endogenous and are allowed to vary both between and within clusters. We assume the presence of \( z_{ij} \), a \( 1 \times L \) (\( L \geq K \)) vector of instrumental variables, which are excluded from the second-stage equation. A vital feature of the model is the \( K \times 1 \) vector of cluster-specific slopes, \( b_i = \beta + d_i \), where \( E(d_i) = 0 \) by definition. We are primarily interested in estimating the PAE, \( \beta \). This vector indicates the heterogeneous effects that vary by cluster and may be correlated with \( x_{1ij} \). We allow for a \( 1 \times H \) vector of exogenous covariates, \( x_{2ij} \), with \( \delta \) and \( \eta \), \( H \times 1 \) vectors of homogeneous slopes. We use a standard formulation of the first stage except that we allow the relationship between the instruments and the endogenous variables to vary across clusters, as \( \gamma_i = \Gamma + g_i \) such that \( E(g_i) = 0 \).

This model is perhaps most naturally applied to long panel settings in which \( n \) clusters (indexed by \( i \)) are randomly sampled bringing with them \( T \) time observations per cluster (indexed by \( j \)). However, this model and the methods described below may also be applied to clustered cross-sections if there is reason to suspect effect heterogeneity across clusters. Likewise, if effects differ across time instead of space, we may think of time as comprising
clusters (indexed by \( i \)), while cross-sectional units comprise the observations per cluster (indexed by \( j \)).

The identification of CRC models has received earlier attention. Graham and Powell (2012), Arellano and Bonhomme (2011), and Chernozhukov et al. (2013) study the identification of CRC models when \( T \) is fixed and the explanatory variables are otherwise exogenous. In particular, Graham and Powell (2012) show that regular identification of CRC models may not be possible in many settings, such as if there is insufficient variation over time in covariates within each cluster. Fernández-Val and Lee (2013) consider the identification of CRC models in the presence of endogeneity as \( n \) and \( T \) tend to infinity, similar to this setting. In particular, they note that the number of parameters with heterogeneous slopes must be less than \( T \) and that the presence of endogeneity requires there to also be all-else-equal exogenous variation within each cluster in order to identify the model parameters. Accordingly, we require similar conditions to estimate PAEs. We provide more detail about the assumptions we require in the discussion of consistency below.

2.1 Proposed estimator in a simple model

Before handling the general case, we illustrate the intuition behind our approach by proposing a per-cluster instrumental variables estimator for a simplified setting (PCIV) in which all clusters are of equal size (such that all the weights are equal) and there are no influential exogenous covariates. PCIV estimation follows three steps:

1. Use OLS to regress each element of \( \mathbf{x}_{1ij} \) on \( \mathbf{z}_{ij} \) separately for each cluster \( i \), obtaining the vector of fitted values, \( \hat{\mathbf{x}}_{1ij} \).

2. Use OLS to regress \( y_{ij} \) on \( \hat{\mathbf{x}}_{1ij} \) within each cluster, obtaining the vector of cluster-specific estimates, \( \hat{\mathbf{b}}_{i,PCIV} \).

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\textsuperscript{6}The “statsby” command in Stata 15 (Stata Corp, 2015) allows these first two steps to be completed in a singular line of code.
3. Average over \( \hat{b}_{i,PCIV} \) for the population to provide the PAE estimate, \( \hat{\beta}_{PCIV} \).

Accordingly, we may write the cluster-specific PCIV estimates as the following:

\[
\hat{b}_{i,PCIV} = \beta + d_i + \left( \sum_{j=1}^{T} x'_{1ij} H_{z_{ij}} x_{1ij} \right)^{-1} \sum_{j=1}^{T} x'_{1ij} H_{z_{ij}} e_{ij}, \tag{2}
\]

where \( H_{z_{ij}} = z_{ij} \left( \sum_{j=1}^{T} z'_{ij} z_{ij} \right)^{-1} z'_{ij} \). The intuition here is that because \( d_i \) does not vary within the cluster, it must be mean independent of within-cluster deviations of \( z_{ij} \) and \( x_{1ij} \) used in the per-cluster regressions, even if it is correlated with both \( z_{ij} \) and \( x_{1ij} \). Maintaining random sampling and homogeneous cluster size, we then average over the estimated cluster-specific slopes to provide our PCIV estimate of \( \beta \).

This case restricts the model studied in Murtazashvili and Wooldridge (2008) by disallowing exogenous regressors and time effects. Common parameters pose a significant issue for the simple estimator above and the proposed estimator in Fernández-Val and Lee (2013). In both, the estimation of all parameters occurs on a per-cluster basis. Accordingly, each additional parameter significantly reduces the degrees of freedom in each regression and the number of parameters cannot exceed \( T \), disallowing the inclusion of time effects.

Furthermore, the class of FEIV estimators discussed in Murtazashvili and Wooldridge (2008) require additional assumptions for consistency. Consider the following representation of the estimate of \( \beta \) from 2SLS applied to the time-demeaned covariates and instruments:

\[
\hat{\beta}_{FEIV} = \beta + \left( \sum_{i=1}^{n} \sum_{j=1}^{T} \bar{x}'_{1ij} H_{\bar{z}} \bar{x}_{1ij} \right)^{-1} \left[ \sum_{i=1}^{n} \sum_{j=1}^{T} \bar{x}'_{1ij} H_{\bar{z}} \bar{x}_{1ij} d_i + \sum_{i=1}^{n} \sum_{j=1}^{T} \bar{x}'_{1ij} H_{\bar{z}} \bar{e}_{ij} \right], \tag{3}
\]

where \( H_{\bar{z}} = \bar{z}_{ij} \left( \sum_{i=1}^{n} \sum_{j=1}^{T} \bar{z}'_{ij} \bar{z}_{ij} \right)^{-1} \bar{z}'_{ij} \). Murtazashvili and Wooldridge (2008) observe that they also “need assumptions such that \( \bar{z}_{ij} \) is uncorrelated with \( \bar{x}_{1ij} d_i \).” This is required in

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7In the simulation and application, we will also consider pooled two-stage least squares and pooled two-stage least squares applied to first-differenced data. Neither estimator avoids making a similar assumption for consistency in estimating the PAE.
FEIV estimation because FEIV tends to apply relatively more weight to clusters with more identifying first-stage variation.

If the instrument’s strength is related to the effect heterogeneity (allowing a LATE to differ from the ATE), \( E[(\bar{\zeta}_{ij}'\bar{x}_{1ij})^{-1}\bar{\zeta}_{ij}'\bar{x}_{1ij}d_i] \neq 0 \) and FEIV may be inconsistent. Further, a correlation between the strength of the instrument and the heterogeneous effects at the intensive margin may cause FEIV to fail to estimate even the LATE consistently. It is this assumption that estimators in Fernández-Val and Lee (2013) and our paper avoid without imposing a homogeneous first-stage relationship.

### 2.2 Proposed estimator in a general model

Empirical contexts are wide-ranging. Clusters are often different sizes and the inclusion of time effects and other exogenous covariates is ubiquitous. Here, we introduce an estimator which researchers may apply to the multiplicity of contexts encompassed in equation 1. For ease of exposition, we use matrix notation such that \( y_i \) is a \( T \times 1 \) vector of a dependent variable, \( X_{1i} \) is a \( T \times K \) matrix of endogenous variables, \( X_{2i} \) is a \( T \times H \) matrix of exogenous covariates, and \( Z_i \) is a \( T \times L \) matrix of instruments. We also introduce weights for cluster-specific estimates, \( w_i \geq 0 \), such that \( \sum_{i=1}^{n} w_i = 1 \). We list the steps for estimating each stage of the general PCIV estimator below using OLS. The first-stage estimation is related to the estimators proposed in Pesaran (2006) and more closely follows an estimator described in Wooldridge (2010).

#### First-stage estimation:

1. Per-cluster, regress \( x_{1ij} \) and \( x_{2ij} \) on \( z_{ij} \), saving the residuals \( \tilde{X}_{1i} = M_{Z_i}X_{1i} \) and \( \tilde{X}_{2i} = M_{Z_i}X_{2i} \) where \( M_{Z_i} = I_T - Z_i(Z_i'Z_i)^{-1}Z_i' \). This step allows us to eliminate \( \gamma_i \) when we estimate \( \eta \) in the second step.
This step is akin to the common practice of detrending data to accommodate cluster-specific linear time trends.

2. To consistently estimate $\eta$, regress the residuals $\tilde{x}_{1ij}$ on $\tilde{x}_{2ij}$ pooling over clusters to estimate

$$\hat{\eta} = \left(\sum_{i=1}^{n} X'_{2i} M_{zi} X_{2i}\right)^{-1} \sum_{i=1}^{n} X'_{2i} M_{zi} X_{1i}.$$

In the analogous example of handling cluster-specific time trends, this step is similar to pooled OLS on detrended data.

3. Estimate $\gamma_i$ per-cluster by regressing $(x_{1ij} - x_{2ij} \hat{\eta})$ on $z_{ij}$. Then, we can construct

$$\hat{X}_{1i} = Z_i \hat{\gamma}_i + X_{2i} \hat{\eta},$$

where

$$\hat{\gamma}_i = (Z'_i Z_i)^{-1} Z'_i (X_{1i} - X_{2i} \hat{\eta}).$$

Here, we use OLS within each cluster to estimate cluster-specific slopes after accounting for covariates with homogeneous slopes.

**Second-stage estimation**

Second-stage estimation in steps 1 - 3 are directly comparable to the same steps in the first stage, except that $y_{ij}$ is substituted in for $x_{1ij}$ and $\hat{x}_{1ij}$ is substituted in for $z_{ij}$.

1. For the second stage, we regress $y_{ij}$ and $x_{2ij}$ on $\hat{x}_{1ij}$ per-cluster, obtaining the residuals

$$\hat{y}_i = M_{\hat{x}_{1i}} y_i$$

and

$$\hat{X}_{2i} = M_{\hat{x}_{1i}} X_{2i},$$

where $M_{\hat{x}_{1i}} = I_{T} - \hat{X}_{1i} (\hat{X}'_{1i} \hat{X}_{1i})^{-1} \hat{X}'_{1i}$.

2. Regressing the residuals $\hat{y}_{ij}$ on $\hat{x}_{2ij}$ pooling over clusters allows us to eliminate $b_i$ when estimating

$$\hat{\delta} = \left(\sum_{i=1}^{n} X'_{2i} M_{\hat{x}_{1i}} X_{2i}\right)^{-1} \sum_{i=1}^{n} X'_{2i} M_{\hat{x}_{1i}} X_{1i}.$$

3. The heterogeneous slopes

$$\hat{b}_i = \left(\hat{X}'_{1i} \hat{X}_{1i}\right)^{-1} \hat{X}'_{1i} (y_{ij} - X_{2ij} \hat{\delta})$$

can be consistently estimated by regressing $(y_{ij} - x_{2ij} \hat{\delta})$ on $\hat{x}_{1ij}$ per cluster.

4. Averaging over $\hat{b}_i$ obtains

$$\hat{\beta}_{PCIV} = \sum_{i=1}^{n} w_i \hat{b}_i.$$

The general PCIV estimator allows for flexibly weighting clusters and models where the dimension of covariates may be large, including when $K + H > T$. Researchers often include additional variables in their models, which they assume to be exogenous. In some instances,
the instrument may only be exogenous conditional on such covariates. Time effects provide one such example, where we may expect the outcome, endogenous, and instrumental variables to each trend over time.

There are a variety of contexts in which heterogeneously weighting cluster-specific estimates may be attractive. In many panel data settings, clusters represent individuals from the population of interest about whom we have multiple observations. Under random sampling of these individuals, we may wish to afford each individual equal weight. However, many popular panel data sets are not random samples of the population.

Such nonrandom sampling schemes would, in turn, lead the average of effects to overweight the populations which are over-represented, obscuring the true PAE. Solon et al. (2015) discuss overcoming such nonrandom sampling as one possible rationale for when empirical researchers should use weights. Fortunately, researchers may still uncover PAEs using per-cluster approaches with relative ease. In this case, the PAE can be identified using the inverse of the probability of selection as a cluster-level weight.

Varying cluster sizes may also necessitate weighting for uncovering the PAE. This may be the case in settings with grouped cross-sectional data or state-level panels, as in our application below. When clusters form the population of interest, we have a similar situation to the panel data setting above. However, if we are instead interested in the population of individuals nested in clusters, we must consider each cluster’s size in the population, and $w_i$ may take the relative size of each cluster. Our application falls into this situation, as states vary widely in their relevance to the nationwide market for gasoline.

Efficiency may provide a third rationale for heterogeneously weighting cluster-specific estimates. Swamy (1971) cites this rationale for introducing a precision weighted estimator for CRC models with exogenous regressors and Fernández-Val and Lee (2013) propose an analogous optimal weighting matrix for their GMM estimation. These weighting schemes

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9For instance, the Panel Survey of Income Dynamics over-samples low-income families, and the National Longitudinal Survey of Youth over-samples African American, Hispanic or Latino, military, and economically disadvantaged youth.
weight estimates of $b_i$ by the relative variance of $x_i$ or covariance between $x_i$ and $z_i$. We, however, view the primary advantage of the PCIV estimator to be its robustness. Were we to adopt a precision weighting approach similar to Swamy (1971) and Fernández-Val and Lee (2013), we would need to impose the same uncorrelated covariance assumption underpinning FEIV estimation. Consequently, we only pursue weighting schemes that do not impose such restrictive assumptions.

3 Consistency and inference of a proposed estimator

3.1 Consistency

While CRC models are perhaps more plausible representations of many economic contexts, incorporating such heterogeneity comes with greater demands on the data. We enumerate further assumptions below:\footnote{Note that $E_i[\cdot]$ refers to the expectation over $T$ for each cluster $i$.}

(A1) \{y_i, X_{1i}, X_{2i}, Z_i, d_i, g_i\}_{i=1}^n is i.i.d. across $i$.

(A2) $E[e_{ij} \mid X_{2i}, Z_i, d_i] = 0$, $E[u_{ij} \mid X_{2i}, Z_i, g_i] = 0$, $E[e_i^2] = \Omega$, $E[e_{ij}^4] < \infty$. Also, $E(d_i) = 0$ where $V(d_i) = \sigma_d^2 < \infty$, and $E(g_i) = 0$ where $V(g_i) = \sigma_g^2 < \infty$.

(A3) $\text{rank}[E_i(z_{ij}' x_{ij})] = K$, $\text{rank}[E_i(z_{ij}' z_{ij})] = L$, and $E[z_{ij}' z_{ij} e_{ij}^2]$ is positive definite.

(A4) $E[\|x_{2ij}\|^2] < \infty$, $E[\|z_{ij}\|^2] < \infty$; $E[\|z_{ij}\|^4] < \infty$, and $E[\|x_{2ij}\|^4] < \infty$.

(A5) $w_i = O_p(n^{-1})$ where $\sum_{i=1}^n w_i = 1$; As $n, T \to \infty$, $n/T \to 0$.

We assume independence across the cluster $i$ in our model to estimate the population average treatment effect. Assumption (A2) is a standard strict exogeneity assumption and says that once we control for $x_{2it}, z_{it}$, and $d_i$, $(x_{2is}, z_{is})$ (where $s \neq t$) do not explain $y_{it}$, and that the variance of the error is well-defined. $E(d_i) = 0$ and $E(g_i) = 0$ are true by definition when the expectation is taken over the population. The condition that $\text{rank}[E_i(z_{ij}' x_{ij})] = K$ is
meaningful, and can be viewed as an application of results from Graham and Powell (2012), extended to the endogenous case. It requires 1) variation in the instruments and endogenous regressors within each cluster, and 2) all clusters to be influenced by the instrument. This condition is demanding on the data, but as noted in Graham and Powell (2012), it is a function of the model rather than a particular estimator. Further, the first-stage PCIV regressions demonstrate its plausibility within the sample. Assumption (A4) ensures finite variances in the population model and is needed for the consistency of the estimator’s variance. We require an assumption about appropriate weights in (A5), which is needed for estimating the population average treatment effect. The second part of Assumption (A5) is in line with the assumption in Fernández-Val and Lee (2013). Since both Fernández-Val and Lee (2013) and our estimator require estimation at the cluster level after the within-cluster estimation, the assumption on the ratio of \( n \) and \( T \) convergence is needed. Combined with weighting, this assumption allows our estimator to be consistent both within the cluster and at the population level.

**Theorem 1** Under the assumptions (A1)-(A5),

\[
\hat{\beta}_{PCIV} = \beta + \sum_{i=1}^{n} w_i d_i + \sum_{i=1}^{n} w_i (X'_{1i} P_{i} X_{1i})^{-1} X'_{1i} P_{i} e_i \overset{p}{\rightarrow} \beta \text{ as } n, T \to \infty, \text{ where } P_{i} = H_{Z_i} + M_{Z_i} X_{2i}(X'_{2i} M_{Z_i} X_{2i})^{-1} X'_{2i} M_{Z_i}, \text{ where } H_{Z_i} = Z_i(Z_i' Z_i)^{-1} Z_i'.
\]

### 3.2 Inference

In this section, we derive the asymptotic variance of the general PCIV estimator for inference and describe its estimation. Since we first estimate cluster-level coefficients, \( b_i \), to obtain an estimate of the global-level estimate, \( \hat{\beta}_{PCIV} \), we need to account for possible estimation
error. We construct a sample variance as follows:

\[
\hat{V}(\hat{\beta}_{PCIV} - \beta) = V\left(\sum_{i=1}^{n} w_i \left[ \hat{d}_i + (X'_{i1} P i X_{1i})^{-1} X'_{i1} P i \hat{e}_i \right] \right) = \sum_{i=1}^{n} w_i^2 \hat{d}_i \hat{d}_i' + \sum_{i=1}^{n} w_i^2 \left( X'_{i1} P i X_{1i} \right)^{-1} X'_{i1} P i \hat{e}_i \hat{e}_i' X_{1i} \left( X'_{i1} P i X_{1i} \right)^{-1}
\]

where \( \hat{d}_i = \hat{b}_i - \hat{\beta}_{PCIV} \), and \( \hat{e}_i = y_i - X_{it} \hat{b}_i - X_{2i} \hat{\delta} \). Throughout this paper, we will apply this estimated variance in the simulation as well as application studies to construct the standard errors. The standard errors from this estimator are robust to heteroskedasticity and arbitrary correlation in the error term within clusters. The proof of Theorem 2 is shown in Appendix B.

**Theorem 2** Under the assumptions (A1)-(A5), \( \sqrt{n}(\hat{\beta}_{PCIV} - \beta) \to N(0, V(\hat{\beta}_{PCIV})) \), where \( \hat{V}(\hat{\beta}_{PCIV}) \) is a consistent estimator of \( V(\beta_{PCIV}) \).

### 3.3 Finite samples in one dimension

While very large data sets are becoming more commonplace, researchers may not wish to rely on asymptotic arguments with respect to both dimensions of their data in many applications. Consequently, we also consider the properties of the PCIV estimator with a fixed number of clusters (\( n \)) while the number of observations per cluster (\( T \)) \( \to \infty \), before considering the probability limit more comparable to FEIV with fixed observations per cluster and \( n \to \infty \). Re-writing the expression for our PCIV estimator,

\[
\hat{\beta}_{PCIV} - \beta = \sum_{i=1}^{n} w_i (\hat{b}_i - \beta) = \sum_{i=1}^{n} w_i (b_i - \beta) + \sum_{i=1}^{n} w_i (\hat{b}_i - b_i)
\]

\[
= \sum_{i=1}^{n} w_i d_i + \sum_{i=1}^{n} w_i (\hat{b}_i - b_i).
\]
We start with fixed \( n \) while the number of observations per cluster goes to infinity. While this could be true with panel data, this setting is perhaps more commonplace for clustered cross-sectional data. Accordingly, we take the probability limit of equation 5 as \( T \to \infty \), providing the following:

\[
\lim_{T \to \infty} (\hat{\beta}_{PCIV} - \beta) = \sum_{i=1}^{n} w_i d_i + \sum_{i=1}^{n} w_i E_i [\hat{b}_i - b_i]
\]

\[
= \sum_{i=1}^{n} w_i d_i + \sum_{i=1}^{n} w_i (E_i [X'_{1i} P_i X_{1i}])^{-1} E_i [X'_{1i} P_i e_i].
\]

\( E_i [\cdot] \) denotes the expectation over \( T \) only. The previously stated rank and validity assumptions applied to each cluster ensure that \( \sum_{i=1}^{n} w_i (E_i [X'_{1i} P_i X_{1i}])^{-1} E_i [X'_{1i} P_i e_i] = 0 \), which leads to the consistency of \( \hat{b}_i \). With finite \( n \), the first term is not zero, though, with random sampling, the expectation of it is zero by assumption. This finite sample bias with limited \( n \) shrinks as \( n \) grows as shown in the proof of Theorem 1. Thus, the PCIV approach is asymptotically unbiased in estimating the PAE, though consistency requires \( n \to \infty \).

Perhaps a more common setting exists when \( T \) is fixed and \( n \) tends to infinity. This setting is common in applications with panel data. Taking the probability limit of equation 5 with \( n \to \infty \) provides the following:

\[
\lim_{n \to \infty} (\hat{\beta}_{PCIV} - \beta) = \sum_{i=1}^{n} w_i E[d_i] + \sum_{i=1}^{n} w_i E[\hat{b}_i - b_i]
\]

\[
= \sum_{i=1}^{n} w_i E[d_i] + \sum_{i=1}^{n} w_i E[(X'_{1i} P_i X_{1i})^{-1} X'_{1i} P_i e_i].
\]

With a fixed number of observations per cluster, additional complications arise. While by definition, \( E(d_i) = 0 \), we first require that \( T \) is large enough (\( T > K \)) to estimate \( b_i \). Second, an asymptotic bias arises with a fixed \( T \) since we cannot rely on \( E[X'_{1i} P_i e_i] = 0 \) and \( \hat{b}_i - b_i = O_p(T^{-\frac{1}{2}}) \).\(^{11}\) Unlike in the exogenous case presented in Wooldridge (2010), each \( \hat{b}_i \)

\(^{11}\)A more detailed expression for the bias term is given in equation 8 in Appendix A.
will likely manifest some degree of finite sample bias. The question is whether we may expect
the biases to be well-behaved or mean zero in expectation as only the number of clusters
approaches infinity. The first way this finite sample bias is well-behaved is apparent from
the consistency argument above. The finite sample bias falls as the ratio of observations per
cluster to regressors (and instruments) grows, as shown in Theorem 1.

However, even with a reasonably large fixed $T$, each $\hat{b}_i$ will suffer from a finite-sample
bias if the instrument is weak within the cluster. As discussed in Bound et al. (1995) and
Staiger and Stock (1997), with weak instruments, the finite sample bias is in the direction
of the OLS estimates. If there are also correlations between instrument strength and effect
heterogeneity, it would be unreasonable to expect mean-zero finite sample bias. However, as
can be seen in equation 8 in Appendix A, this finite sample bias is well-behaved since it falls
as the strength of the instrument within each cluster increases. In the extreme, if we have
an exogenous instrument that perfectly predicts the regressor, there is no endogeneity issue,
and the unbiasedness result from Wooldridge (2005); Arellano and Bonhomme (2011); and
Bates et al. (2014) apply.

In cases where some clusters are unmoved by the instrument or the instrument is weak,
the PCIV estimator may still recover LATEs, which may be an advantage over competing
estimators. As we have modeled the treatment effect and compliance heterogeneity as varying
only across individuals, we need no further assumptions regarding monotonicity. That
is, while we do not maintain monotonicity across individual clusters, we do maintain mono-
tonnicity within each. Unlike with the independent cross-sectional data model discussed in
Imbens and Angrist (1994), we observe cluster- (or individual-) specific unbiased estimates
of compliance and may perform inference on each. Consequently, we can aggregate our
treatment effect estimates according to the cluster-specific, first-stage estimates to get dif-
ferent LATEs, including separate LATEs for compliers (say those who are moved towards
treatment by the instrument) and defiers (say those who are moved away from treatment
by the instrument). Accordingly, we may exclude never-takers and always-takers or those only weakly moved by the instrument (for instance, those with first-stage F-statistics less than 10, following the rule of thumb from Stock and Yogo (2005)). Thus, PCIV allows us to estimate LATEs over well-defined and identifiable populations for whom finite sample bias is likely to be small. Given the potential for bias in the PCIV approach with finite samples, we use a Monte Carlo study to examine how the per-cluster instrumental variables estimator performs as we vary the number of observations per cluster below.

4 Simulation Study

We now describe the simulations we use to examine the performance of the P2SLS, FEIV, and PCIV estimators in finite samples. In conducting this simulation study, we consider two conditions: (a) where the uncorrelated covariance assumption holds and (b) where it is violated. We evaluate the performance of each method with respect to the bias, asymptotic risk as measured by root mean square error (RMSE), the ratio of mean standard errors by the standard deviations of simulated estimates, and the coverage rate from each approach.

We focus the simulation discussion on the performance of the three estimators when \( n \) is large, and \( T \) is fixed as it is likely to arise in applied research and theoretically is more problematic for PCIV estimation. \(^{12}\)

We use different fixed levels of \( T \), ranging from 6 to 250, with \( n = 250 \) throughout the simulation. \(^{13}\)

We generate the data based on our model in equation (1):

\[
y_{ij} = x_{ij} b_i + e_{ij},
\]

\[
x_{ij} = z_{ij} \gamma + u_{ij},
\]

where \( b_i = \beta + d_i = 1 + d_i \) and \( \gamma = 1 \). The key difference in the two cases is that in

\(^{12}\)For completeness, we include the symmetric examination in which we hold \( T = 250 \) and vary \( n \) in Appendix C. Figure C.1 shows the density plots of the bias for all three estimators to summarize the results. Due to its asymptotic unbiasedness, Figure C.2 shows that PCIV generally performs relatively better in cases where \( n \) is fixed and \( T \) is large.

\(^{13}\)Each simulation is repeated 500 times using Stata 16 (Stata Corp, 2019).
case (a), the random slope, $d_i = d_{ai}$, is uncorrelated with the variance of $x_{ij}$ and $z_{ij}$, and in case (b), the random slope, $d_i = d_{bi}$, is correlated with both variances. Specifically, the excluded exogenous variable, $z_{ij} \sim N(0, \exp(2d_{bi}))$. Further, we define the composite error terms as $e_{ij} = \alpha_{1i} + o_{ij} + \epsilon_{ij}$ and $u_{ij} = \alpha_{1i} + 0.2w_i + 0.32v_{ij}$, where $\epsilon_{ij} \sim N(0, 1.1)$. Both $\alpha_{1i}$ and $\alpha_{0i} = \alpha_{1i} + 0.2w_i$ serve as random intercepts; and $\epsilon_{ij}$ and $v_{ij}$ are cluster- and time-varying errors. We set $v_{ij} \sim N(0, 1)$ for uncorrelated case and $v_{ij} \sim N(0, \exp(2d_{bi}))$ for the correlated case. An exogenous cluster-level error, $w_i$, is drawn from the standard normal distribution. We set $o_{ij} = \xi_{ij} + \eta_{ij}$ with $\eta_{ij}$ following $N(0, 1)$ and with $\xi_{ij}$ being residuals from regressing $x_{ij}$ on $z_{ij}$. Then endogeneity of our variable of interest, $x_{ij}$, enters through the presence of $o_{ij}$ in the generation of $y_{ij}$. Our random intercept $\alpha_{1i}$ and correlated random slope $d_{bi}$ are mean-zero bivariate normal with a correlation of 0.5 and standard deviations of 0.4 and 0.25 respectively. In case (a), $d_{ai}$ is generated in the same setup except we set the correlation as zero. The key assumption for the consistency of P2SLS and FEIV is that the within-cluster covariance between $x_{ij}$ and $z_{ij}$ is uncorrelated with the random slope. When there is no violation, $d_{ai}$ is not related to the variance of $z_{ij}$ or $x_{ij}$. In the second case, there is a violation of the key assumption as $d_{bi}$ acts as a random coefficient on $x_{ij}$ and determines the variance of $z_{ij}$ and $x_{ij}$.

The resulting correlations with $n = 250$ and $T = 250$ are shown in Table 1. Under both conditions, $x_{ij}$ is correlated with unobserved heterogeneity $\alpha_{1i}$, $d_{ai}$, and $d_{bi}$, and the omitted variable, $o_{ij}$, producing endogeneity. Our variable of interest, $x_{ij}$, is also strongly correlated with the instrument $z_{ij}$, and $z_{ij}$ is otherwise orthogonal to the other terms, such that our instrument is both relevant and valid. The key condition hinges on whether the heterogeneous slope, $d_{ai}$ or $d_{bi}$, is correlated with the strength of the instrument within-cluster. The correlations between $d_{ai}$ and $d_{bi}$ and $\bar{x} \bar{z}$ are 0.006 and 0.278 respectively reflecting two

---

14 In Appendix C we allow the correlation between effect heterogeneity and the first-stage variation to vary more continuously. We also allow for heterogeneity in first-stage coefficients.

15 Having the variance of $z_{ij}$ depend on $d_{bi}$ ensures that the variance of $z_{ij}$ in both cases are similar, while the variance of $z_{ij}$ is only related to the random coefficient of $x_{ij}$ on $y_{ij}$ in the second case.
possible states of the key condition.

Table 1: Simulated correlations with and without correlated covariance between \(d\) and \(\ddot{x}\ddot{z}\)

<table>
<thead>
<tr>
<th>Panel A: Uncorrelated Covariance</th>
<th>Panel B: Correlated Covariance</th>
</tr>
</thead>
<tbody>
<tr>
<td>(d) (\ddot{x}) (\ddot{z}) (x) (o) (z) (\alpha_1)</td>
<td>(d) (\ddot{x}) (\ddot{z}) (x) (o) (z) (\alpha_1)</td>
</tr>
<tr>
<td>(\ddot{x})</td>
<td>0.006</td>
</tr>
<tr>
<td>(x)</td>
<td>0.363</td>
</tr>
<tr>
<td>(o)</td>
<td>0.374</td>
</tr>
<tr>
<td>(z)</td>
<td>0.0004</td>
</tr>
<tr>
<td>(\alpha_1)</td>
<td>0.01</td>
</tr>
</tbody>
</table>

Notes: These correlations are calculated across both \(i\) and \(j\) after pooling a sample from the simulation. \(\ddot{x}\ddot{z}\) stands for the product of the time-demeaned variables of interest and the instrument when the key condition holds and is violated, respectively.

As the primary potential benefit of PCIV is robustness, we first consider the estimated bias for the coefficient \(\hat{\beta}\) to assess each estimator’s performance. Panel (a) of Figure 1 shows the average bias in the three estimators with \(n = 250\) as \(T\) increases, maintaining the uncorrelated covariance assumption on the left and violating it on the right. FEIV and P2SLS estimators perform consistently well but demonstrate consistent and significant bias once the uncorrelated covariance assumption is violated. In contrast, the PCIV estimator manifests finite sample bias under both conditions with very small clusters (when clusters have 10 or fewer observations). However, across cluster sizes, PCIV outperforms the other estimators when the uncorrelated covariance assumption is violated. Furthermore, while the estimated biases of FEIV and P2SLS estimators do not show any improvement even with the increasing cluster size, the estimated bias of the PCIV approach gets closer to zero as cluster sizes increase. Table C.1 in Appendix C shows that the magnitude of bias in both FEIV and P2SLS is almost identical at approximately 12 percent.

Naturally, researchers are not only interested in the bias of estimators but are also interested in the estimators’ precision. We use RMSEs, which comprise bias and imprecision as a summative measure of performance on both dimensions. As the scale of RMSEs depends on both cluster size and the number of clusters present, we show the RMSE of the estimated
coefficient from the three estimators, with a large number of clusters and the number of observations per cluster varying between 6 and 250. Again, we repeat the exercise both with and without the uncorrelated covariance assumption holding.

Panel (b) of Figure 1 reveals that with very small clusters, the PCIV approach is prone to large RMSE. However, in this simulation, by a cluster size of only 8, the PCIV approach has comparable or lower RMSE than FEIV or P2SLS. We were somewhat surprised by the relative performance of the PCIV estimator at such small cluster sizes as Staiger and Stock (1997) state that the asymptotic distributions provide good approximations on sampling distributions with 10 - 20 observations per instrument.

We evaluate the performance of the analytic standard errors over cluster size by first depicting the ratio of the mean of the estimated standard errors (SEs) divided by sampling standard deviations (SDs) in panel (c) of Figure 1.

In all cases, the analytic standard errors do reasonably well with large sample sizes along both dimensions. However, they are too small with very small clusters. By nine observations per cluster, the ratio of mean SE to SD for PCIV is comparable to the same ratio for FEIV. The ratio is consistently close to one with $T$ above ten, for all three estimators both with the uncorrelated covariance assumption holding and when it is violated.

Lastly, we show the rates at which the 95 percent confidence intervals constructed from our estimated standard errors include the true value of the parameter. Naturally, this should occur 95 percent of the time. Panel (d) of Figure 1 shows the evolution of coverage rates for each estimator in the uncorrelated covariance case on the left and correlated covariance on the right with 250 clusters as $T$ grows. In the uncorrelated covariance case, the coverage rates for all three estimators range from 0.89 to 0.98 for all cluster sizes, though they converge close to 0.95 as the cluster size grows.

When there is a correlation between the strength of the instrument and random coefficients, the bias in FEIV and P2SLS is meaningful. Neither standard estimator includes the
true value in the 95 percent confidence interval more than 40 percent of the time. Moreover, the rejection rate of the true parameter grows as cluster size grows. In contrast, the PCIV rejection rate at the 95 percent confidence level is never more than 6 percentage points from 95 percent, and again, it converges to 95 percent as cluster size grows. Though PCIV inference performs well overall, the relatively poorer performance when T is small may give researchers reason to adopt a bootstrap approach to standard error estimation with restricted samples.

5 Estimating the price elasticity of demand for gasoline

There is extensive literature estimating the price elasticity of gasoline demand. However, estimating this important parameter is not straightforward. Gasoline prices and the volume purchased likely depend upon each other through the interaction of supply and demand forces. This simultaneity issue requires a source of exogenous variation to establish a unidirectional causal link. Consequently, we use instrumental variables estimation and follow Davis and Kilian (2011); Blundell et al. (2012); Hausman and Newey (2016); and Coglianese et al. (2017) in using state gasoline taxes to instrument for prices. In many ways, the empirical setting and design are ideal, especially considering that the efficacy of carbon taxes in lowering fuel consumption is one reason why the price elasticity of gasoline demand is of particular interest.

Works such as Davis and Kilian (2011); Levin et al. (2017); and Coglianese et al. (2017) econometrically model the relationship between gasoline prices and the quantity sold as though responsiveness to prices is homogeneous. However, heterogeneity in elasticities seems likely in this context. Regulation of this market varies across states, as does industry composition, population density, demographic composition, transportation substitutes, macroeconomic climate, and, most importantly, taxes.

Wadud et al. (2010); Frondel et al. (2012); Blundell et al. (2012); and Hausman and

1See Dahl (1986) for a helpful review of early examples and Davis and Kilian (2011); Blundell et al. (2012); Hausman and Newey (2016); Coglianese et al. (2017); Levin et al. (2017); and Hoderlein and Vanhems (2018) for more recent examples.
Newey (2016) examine how demand elasticities for gasoline may differ across individual characteristics. Of these, only Blundell et al. (2012) and Hausman and Newey (2016) deal with the endogeneity of prices, and both use state gasoline taxes and distance from the Gulf of Mexico as instrumental variables. However, in so doing, each implicitly assumes that the identifying variation (tax changes and tax pass-through) and distance from the gulf are unrelated to the potentially heterogeneous demand elasticities. We believe that this assumption may not be benign. For instance, it is plausible that states with developed transportation substitutes may have more elastic demand than states with less developed transportation networks. Further, these same states may be more prone to raise taxes on gasoline than states with fewer transportation substitutes and less elastic demand. Figure D.1 in Appendix D shows that states with greater public transportation ridership prior to our sample have greater subsequent changes in their gasoline tax rates than do states with lower usage of public transportation.

5.1 Model and estimation

We allow for heterogeneity in both the first and second stages of our econometric model.16 We allow each state (indexed by $i$) to differ in both the level of gasoline demand, $\alpha_{1i}$, and in the price elasticity of gasoline demand (depicted by $b_i = \beta + d_i$) according to the following CRC model similar in structure to equation 1:

$$\text{logsales}_{ij} = \alpha_{1i} + \text{logprice}_{ij} b_i + x_{ij} \delta + \epsilon_{ij},$$

$$\text{logprice}_{ij} = \alpha_{0i} + \text{logtaxes}_{ij} \gamma_i + x_{ij} \eta + u_{ij}. \tag{7}$$

We are primarily interested in the population average price elasticity of gasoline demand, $E[b_i] = \beta$. We use the log of taxes to instrument for the potentially endogenous log of prices.

16Heterogeneous elasticities may exist at more or less granular levels. However, elasticity heterogeneity only leads to inconsistency in existing estimators when systematically related to heterogeneity in the first stage. The first stage does not vary across individuals but across states, making states an intuitive level to model heterogeneity.
We allow for possible heterogeneity in tax pass-through rates, as denoted by $\gamma_i$.

Given this suspected heterogeneity, our preferred approach is PCIV. Both for comparability to prior elasticity estimates and to benchmark the performance of the PCIV approaches, we apply P2SLS on first differences and FEIV to the data and model above. We use the general PCIV estimator presented in section 2.2 rather than the simplified PCIV estimator. This is because $x_{ij}$ indicates the presence of exogenous regressors with common parameters in the model. Most notably, there are general time and seasonality trends in gasoline prices, consumption, and taxes, such that our instrument is only exogenous conditional on them. As the inclusion of month-by-year fixed effects is standard in P2SLS and FEIV, we adopt them for all three estimators. Including month-by-year fixed effects is impossible using the simple approach or that described in Fernández-Val and Lee (2013), and allowing for heterogeneous month and year effects by cluster would be extremely taxing on the data.

Furthermore, states vary substantially in size and relevance to the market for gasoline. The inclusion of heterogeneous slopes in the econometric model leads us to pay particular attention to differences in state sizes and volumes of gasoline purchased. Were the responsiveness to prices homogeneous across states, such differences in size may only influence the efficiency of the estimates. However, if the price-elasticities of gasoline demand differ by state, failing to account for such differences in states’ relevance to the market may lead to inconsistent estimates of the parameter over the population of gasoline sales. Thus, we incorporate weights representing the relative average volume purchased in each state. We use these weights in weighted P2SLS and FEIV regressions, as well as in aggregating the state-specific coefficients in PCIV estimation. In contrast with PCIV, however, weighting does not necessarily help recover the PAE with P2SLS and FEIV estimation in the presence of random coefficients (Solon et al. 2015). We also provide results from regressions without these weights for comparison.
5.2 Data

The data we use carries a fittingly wide scope, containing monthly observations of gasoline prices, taxes, and volume sold from January 1989 through December 2018 throughout the United States. The data provides us with 360 time observations over the 50 states and the District of Columbia.

The data on monthly, statewide, gasoline price averages for 1989 through 2011 comes from the U.S. Department of Energy, Energy Information Administration (EIA), ‘Petroleum Marketing Monthly Report: Gasoline Prices by Formulation, Grade, Sales Type.’ It measures tax-exclusive prices to end-users. We add state and federal taxes to the tax-exclusive prices to approximate at-the-pump prices. However, the EIA discontinued this series and the survey on which it relied in 2011, requiring updated subsequent tax changes and significant additional data collection. We supplement this pricing data with average at-the-pump price data from Gasbuddy.com.

We begin with the annual ‘Highway Statistics Series’ for effective dates of state gasoline taxes and refine these dates against state governmental documentation when possible. Since thirty states have changed their state gasoline taxes in the last decade (some multiple times), the recent data provides useful identifying variation. Following Davis and Kilian (2011), we net out any portion of the state gasoline tax rate due to changes in gasoline prices to avoid building endogeneity back into our estimation. Throughout, we use the EIA, ‘Petroleum Marketing Monthly Report: Prime Supplier Sales Volumes by Product and Area’ for data.

\[17\] This data was retrieved as the maximum 10-year (January 2009 - January 2019) charts for each state plus the District of Columbia from [https://www.gasbuddy.com/Charts](https://www.gasbuddy.com/Charts) on March 22, 2019, and digitized into four or five daily price averages using [https://automeris.io/WebPlotDigitizer/](https://automeris.io/WebPlotDigitizer/). We then averaged over these prices to form a monthly average. There is a level shift between the at-the-pump prices from Gasbuddy.com and the series from EIA. However, for the three years in which the data is overlapping, the trends and fluctuations in prices move in concert. As a result, we believe the month-by-year fixed effects will absorb the constant gap. There are overlapping periods between March 2009 and February 2011 for the EIA and Gasbuddy data. The summary statistics during these periods are given in Table D.1.

\[18\] We largely use data from Davis and Kilian (2011) during the period from 1989 through 2008 though discovered a few instances in which the taxes they used either failed to capture per-unit taxes fully or had price changes built into them. We document these tax changes in the Stata do-file (titled “newtaxes.do”) and provide within that file links to the documentation for each tax change.
on gasoline sales volume.

We add several covariates to check the robustness of our results and possibly improve efficiency. In particular, we include the log of unemployment rates; real per-capita income; population; the number of licensed drivers; the number of road miles; average, minimum, and maximum temperatures; and precipitation; as well as indicators for missing values of each. We list the summary statistics and sources of control variables in Table D.2 in Appendix D.

5.3 Results

We present the elasticity estimates from all three estimators in Table 2. Results without volume weights appear on the left, and estimates incorporating the state-specific gasoline-volume weights appear on the right. For PCIV, the standard errors are estimated as described in section 3.2. We present the first-stage F-statistics for each estimator along the bottom row of Table 2. We calculate the F-statistics for PCIV using Hotelling’s T-squared test.

Table 2: Summary of Results Using Three Estimation Methods

<table>
<thead>
<tr>
<th></th>
<th>Without volume weights</th>
<th>Volume weighted</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>P2SLS       FEIV</td>
<td>PCIV</td>
</tr>
<tr>
<td>Log price</td>
<td>-0.724</td>
<td>-0.929</td>
</tr>
</tbody>
</table>
<pre><code>               | (0.193)     | (0.415)              | (0.227)          | (0.154)  | (0.394)  | (0.240)  |
</code></pre>
<p>| First-stage F-statistic | 36.66   | 79.71               | 58.35           | 47.47    | 63.70    | 61.16    |
| Controls             | Y          | Y                   | Y               | Y        | Y        | Y        |
| Log price            | -0.736      | -0.828              | -0.543           | -0.512   | -0.760   | -0.561   |
| (0.189)     | (0.327)              | (0.278)          | (0.138)  | (0.271)  | (0.294)  |
| First-stage F-statistic | 36.58   | 80.92              | 58.71           | 46.83    | 60.26    | 59.93    |
| Controls             | Y          | Y                   | Y               | Y        | Y        | Y        |</p>

Notes: The sample consists of 18,360 state-by-month observations. First-stage F-statistics for P2SLS and FEIV are obtained from the regression of each endogenous regressor on the exogenous regressors and the instruments. The calculation of the first-stage F-statistics for the PCIV was done using Hotelling’s T-squared test. State-clustered standard errors appear in parentheses.

\[19\] We present first-stage coefficient estimates in Table D.3 in Appendix D. We estimate the model with year and month-fixed effects and find similar results in Table D.4.
We first note that the log of state gasoline taxes is generally strongly predictive of at-the-pump prices across specifications. The F-statistics range from 36.58 (PCIV without volume weights) to 80.92 (FEIV without volume weights).

The estimates of the elasticity of gasoline demand are consistent in sign, though the magnitudes of the estimated elasticities range meaningfully across estimators, and in some instances, across specifications within estimators. FEIV provides the largest point estimates in magnitude, estimating elasticities of -0.929 (unweighted and without covariates) to -0.760 (weighted and with covariates) with standard errors of 0.415 and 0.271 respectively. These FEIV estimates are double the prevailing estimates in the energy economics literature. The P2SLS estimator using first differences is most efficient, with standard errors often less than half the size of those for FEIV, yet is the most sensitive to including weights for sales volume. While the unweighted P2SLS elasticity estimate is large at -0.724, the weighted P2SLS estimate ranges from -0.463 to -0.512 (depending on the inclusion of covariates), making the FEIV estimate around 40 percent larger than those from P2SLS. The PCIV estimates of the elasticity of gasoline demand fall between those two with point estimates ranging tightly from -0.543 to -0.561 across all specifications. The standard errors associated with the PCIV estimates range from 0.227 to 0.294.

5.4 Examination of identifying variation

It is natural to ask which estimates are preferable according to the context and econometric theory. We take multiple approaches to shed light on this question. First, we consider the weighting employed by all three estimators. We examine whether the implicit weighting used in FEIV and P2SLS mimics the weights by sales volume and find significant divergence. Second, we follow Coglianese et al. (2017) and explore whether anticipatory behavior drives the results. Third, we inspect whether there appears to be a relationship between the first-stage variation and the estimated elasticities—an apparent violation of the key condition.
for the consistency of P2SLS and FEIV. We then explore the heterogeneity in the first- and second-stage relationships between gasoline taxes, prices, and sales volume. In sum, these examinations of the data lead us to prefer the weighted PCIV approach as our decision to model such heterogeneity is borne out by the data. This rich accounting of the identifying variation in the data reveals four states for which the log of gasoline taxes does poorly in predicting changes in prices. As a result, we also estimate a LATE, a weighted average of the state-specific elasticities for the 46 states in which the instrument is strong.

Our population of interest is all gasoline sales within the United States. If there are heterogeneous elasticities across states, we must afford each state weight according to its relevance in the market. In this context, it turns out that the PCIV point estimates are very similar when we do and do not use weights for sales volume, though a priori, that result was not obvious. As shown in Murtazashvili and Wooldridge (2008) and discussed in Section 2 above, P2SLS and FEIV each implicitly apply additional weight to state-specific coefficients where there is relatively more first-stage variation. We examine the agreement between the two weighting schemes in Figure 2. On the left, we report the negative of the relative first-stage variation in each state from FEIV estimation. Functionally, this is the sum of the products of demeaned and detrended $x$ and $z$ for each state divided by the sum of those state totals. The share of total gasoline sales that occur in the state over the panel is on the right.

Figure 2 shows vast disagreement between the two weighting schemes. The explicit weights we employ are intuitive, with larger gasoline-consuming states receiving influence commensurate with their relevance in the market. California has the highest sales volume, consuming 11.3 percent of the gasoline in the country. The District of Columbia has the lowest sales volume with just 0.1 percent of the national market.

The FEIV weighting scheme also affords California the highest weight, though it is 63 percent higher than the weights based on sales volume. Texas consumes the second most
gasoline in the country (9.5 percent) yet is twenty-second in first-stage variation (1.3 per-
cent). On the other end, there are notable exceptions. With only 1.1 percent of gasoline
sales, standard FEIV estimation affords Connecticut the fifth largest weight. As a further
complication for FEIV estimation in this context, both Hawaii and Minnesota receive nega-
tive weight in this exercise.

Might using weights with FEIV rectify the mismatch of its implicit weights? Not gener-
ally. First, even with the addition of volume weights, FEIV will continue to overweight states
for which the instrument is strong. Secondly, as shown in Solon et al. (2015), weighted least
squares estimation in the presence of heterogeneous effects generally does not consistently
estimate the PAE, nor does it always dominate unweighted least squares.

Coglianese et al. (2017) remark that anticipatory behavior biases the estimates of Davis
and Kilian (2011). In Appendix E, we examine the issue theoretically and empirically. The
anticipatory behavior is primarily a concern only for the P2SLS estimator as it is persistently
inconsistent with such violations to strict exogeneity. In contrast, while PCIV and FEIV are
inconsistent with fixed T, the inconsistency from this source in FEIV and PCIV shrinks to
zero as the number of time periods grows large. Consistent with theory, Figure E.1 shows
the robustness of PCIV and FEIV to the inclusion of additional lags and leads of log prices
and log taxes whereas the P2SLS estimator is sensitive to this violation of strict exogeneity.
We additionally provide a replication of Davis and Kilian (2011) and Coglianese et al. (2017)
in Appendix E.

One advantage of the PCIV estimator is revealing the heterogeneity in first- and second-
age stage estimates across clusters. We observe significant heterogeneity in the location-specific
elasticities and tax pass-through rates. Figure 3 reveals this variation.\(^\text{20}\) The right-hand
side of Figure 3 shows the state-specific tax pass-through rates from the first-stage regres-
sion of logged prices on logged state taxes. The results reveal significant heterogeneity in

\(^{20}\)For detailed state-specific estimates, see Table D.5 in Appendix D.
coefficients. In the District of Columbia and Washington State, the pass-through rates are double the average at 0.61 and 0.47, respectively. On the other end, Georgia, Hawaii, Michigan, and Indiana each have estimated first-stage coefficients of 0.08 and lower, with the estimated effect in Georgia defying the average sign. Unsurprisingly, the F-statistics on the log of taxes in these states are each less than 10, failing to surpass the weak instruments rule of thumb from Stock and Yogo (2005). There is sufficient noise in the District of Columbia estimate to also drive its F-statistic below 10. As a result, we should interpret the second-stage estimates from these locations with caution.

The estimates of state-specific gasoline demand elasticities on the left-hand side of Figure 3 also show significant variation. Montana, Arizona, Idaho, Nevada, and Wyoming have the most inelastic gasoline demand (elasticities at or smaller than -0.32). Perhaps inelastic gasoline demand makes sense in these rural states, which are not densely populated and mostly lack robust public transportation substitutes. In contrast, 12 states have estimated elasticities that are larger than -0.64 and Pennsylvania has an estimated elasticities of -0.98.

Estimating the state-specific second-stage slopes also allows us to examine the key condition for the consistency of FEIV estimation, namely, whether there is any relationship between effect heterogeneity and first-stage variation. We show the relationship between the relative elasticities and the relative first-stage variation in Figure 4. The PCIV estimates of \(b_i\) provide a natural way to examine heterogeneous elasticities. We present these estimates relative to the mean along the x-axis. We measure the relative first-stage variation similar to the measure used in Figure 2, scaled to the mean, which we present along the y-axis. Each circle represents a state with the size scaled by the state’s relevance to the gasoline market.

Figure 4 reveals a strong upwards slope as the two statistics have a correlation of 0.14 across states. In general, this means that states with relatively more exploitable variation

\[\text{We also uncover significant variation in estimated elasticities employing PCIV across each of the seven EIA Petroleum Administration for Defense Districts. These estimates range from -0.845 to -1.160. However, these results assume no heterogeneity in effects within each region and may suffer from some of the same issues as FEIV. We report the results in Table D.6 in Appendix D.}\]
in the first stage also have larger estimated elasticities. This is consistent with the idea that states with less developed public transportation infrastructure (and less elastic gasoline demand) raise gasoline taxes less frequently. This relationship would lead to an upwards bias in the elasticity estimate from FEIV. Indeed, the FEIV elasticity estimates of the PAE are 35 to 90 percent larger in magnitude than the PCIV estimates of the same parameter.

CRC models that place no restrictions on the correlations between effect heterogeneity and first-stage variation require sufficient first-stage variation within each cluster to allow PAEs to reflect all clusters. However, we find that the predictive power of the instrument is weak in Hawaii (F-stat = 2.57), Indiana (2.92), Georgia (5.16), Michigan (0.64), and Washington D.C. (7.81). As a result, we redo the analysis on the 46 states in which the first-stage F-statistic is above ten, following the rule of thumb proposed by Staiger and Stock (1997) and justified in Stock and Yogo (2005). Though we acknowledge this parameter may not be relevant for the entire population, this exercise provides us with an estimate of the average price elasticity of gasoline demand on a specified and well-defined group of compliers, namely, states in which the F-statistic of the instrument is above ten.

We report the results from weighted and unweighted PCIV on this population of compliers in Table 3. For comparison, we also apply FEIV and P2SLS to the same data. Among states for which the instrument is strong, the PCIV estimates are -0.551 to -0.554, with their standard errors of 0.227 and 0.240 depending on weighting. Despite the reduction in sample size, the standard errors here are modestly smaller than those in Table 2 using the entire sample, as those states with weak first stages had relatively extreme second-stage estimates. The P2SLS and FEIV are larger when estimated on this restricted sample. Recall that the apparent violation of the key condition may prohibit P2SLS and FEIV from consistently estimating even a LATE. Indeed, the relationship between estimated elasticities and first-stage variation is just as strong if not stronger within the states in which the instrument is strong.
Table 3: Estimated elasticities among states in which the instrument is strong (LATE)

<table>
<thead>
<tr>
<th></th>
<th>Without volume weights</th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>P2SLS</td>
<td>FEIV</td>
<td>PCIV</td>
</tr>
<tr>
<td>Log price</td>
<td>-0.724</td>
<td>-0.929</td>
<td>-0.551</td>
</tr>
<tr>
<td></td>
<td>(0.193)</td>
<td>(0.415)</td>
<td>(0.227)</td>
</tr>
<tr>
<td>First-stage F-statistic</td>
<td>36.66</td>
<td>79.71</td>
<td>58.35</td>
</tr>
</tbody>
</table>


6 Concluding Remarks

Whether the purpose of empirical work is to inform and evaluate theory, uncover and explain phenomena, or inform practitioners of best practices, population average effects are generally of high interest. We propose per-cluster instrumental variables estimation to provide both population average estimates and effect heterogeneity in correlated random coefficient models when key variables may be endogenous. Given the vast unobserved differences between people and the heterogeneity of their behavior, we believe such environments are widespread, as is the applicability of this approach.

We present the conditions under which PCIV is consistent in estimating such generally representative parameters and show that it has robustness properties beyond more standard approaches such as pooled two-stage least squares and fixed effects instrumental variables, specifically in the presence of heterogeneous responsiveness to treatment. We develop the theory behind this and demonstrate the performance of PCIV in simulation.

Our use of PCIV adds rigor to the investigation of the price elasticity of demand for gasoline. Our cumulative evidence suggests a price elasticity for the demand for gasoline in the United States to fall between -0.5 and -0.55, keeping in mind that the confidence intervals are wide. These estimates imply that consumers are more sensitive to price hikes than would
be implied by Coglianese et al. (2017), Hughes et al. (2008), and Levin et al. (2017), which find elasticities ranging from -.37 to -.03. However, only Coglianese et al. (2017) address the endogeneity issue in prices. We find that the small estimates there are due to the use of P2SLS applied to first differences, which is particularly afflicted by anticipatory behavior and is only identified off short-run (first month) responses.

These high elasticity estimates may also reflect that price increases due to tax increases are more permanent and salient to consumers than most other gasoline price increases. Indeed, Davis and Kilian (2011); Scott (2012); Baranzini and Weber (2013); Li et al. (2014); and Coglianese et al. (2017) each make this argument, with Li et al. (2014) in particular demonstrating both points. As a result, these estimates of the price elasticity of gasoline demand pertain to permanent changes in prices for relatively informed consumers. However, the responsiveness to permanent and salient price changes is often the parameter of interest in modeling gasoline-dependent industries and many policy discussions.

Our application shows that the flexibility of PCIV estimation provides more transparency about the underlying data. For instance, we can view whether the implicit weighting of standard estimators corresponds to the appropriate population weights and whether there appears to be a near-zero correlation between the strength of the instrument and heterogeneous effects, which may inhibit the estimation of population average effects with standard estimators. PCIV also reveals heterogeneity within the first stage including whether monotonicity holds at the cluster level. Many of these may be estimated even without large numbers of observations per cluster. Finally, in cases where there appears to be insufficient first-stage variation within a subset of clusters to produce a reliable cluster-specific estimate, PCIV allows for the estimation of a local average effect in a defined population of clusters in which the instrument is strongly predictive.

References


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Figure 1: Simulation results across cluster sizes

(a) Bias for coefficient $\beta$ of $x_{ij}$

(b) Root mean square error for coefficient $\hat{\beta}_1$ of $x_{ij}$

(c) Mean standard errors over estimates’ standard deviations

(d) Standard error coverage rates

Notes: P2SLS = Pooled Two-Stage Least Squares; FEIV = Fixed Effects Instrumental Variables; PCIV = Per-Cluster Instrumental Variables. Each point represents the results from 500 repetitions. Within each panel, figures on the left are when the uncorrelated covariance assumption holds, and figures on the right are when it is violated. The ratio of mean standard errors (SEs) divided by standard deviations (SDs) of the estimates. The horizontal line in (c) denotes a ratio of one. The horizontal line in (d) is to denote the exact 95 percent coverage rate. In many instances, FEIV total overlaps with P2SLS, though this is an artifact of the specific DPG in this simulation.
Figure 2: Weighting under FEIV and PCIV approaches

Notes: On the left we report the negative of the relative first-stage variation for FEIV estimation, as measured by the sum of the products of demeaned and detrended logprice and logtax for each state divided by the sum of those state totals. On the right, we report the share of total gasoline sales that occur in the state over the panel.

Figure 3: State-specific first- and second-stage coefficients

Notes: On the left, we report PCIV state-specific elasticity estimates. We report state-specific first-stage tax pass-through estimates on the right. The standard deviation of the state-specific elasticities is 0.204 or 38% of the mean. The standard deviation of the state-specific pass-through rates is 0.115 or 42% of the mean.
Figure 4: Heterogeneous elasticities and first-stage variation

Notes: We present elasticity estimates relative to the mean along the x-axis. Along the y-axis is relative first-stage variation as measured by the sum of the products of demeaned and detrended logprice and logtax for each state divided by the mean of those state totals. The fitted line has a slope coefficient of 2.000 and a standard error of 1.663.
A  Proof of Theorem 1

\( \hat{\beta}_{PCIV} \) is consistent if and only if \( \lim_{n,T \to \infty} MSE(\hat{\beta}_{PCIV}) \to 0 \). We will show both asymptotic bias and variance will converge to zero asymptotically.

Define \( P_i = HZ_i + MZ_i X_2i(X_{2i}'MZ_i X_{2i})^{-1}X_{2i}'MZ_i \), where \( HZ_i = Z_i(Z_i'Z_i)^{-1}Z_i' \) and \( MZ_i = I_T - HZ_i \). Given the model as \( y_i = X_{1i}b_i + X_{2i}\delta + e_i \) and the estimated \( \hat{\delta} \), per-cluster estimator \( \hat{b}_i \) can be written as follows as derived in Section 2.2:

\[
\hat{b}_i = (X_{1i}'P_i X_{1i})^{-1}X_{1i}'P_i (y_i - X_{2i}\hat{\delta})
\]

\[
= (X_{1i}'P_i X_{1i})^{-1}X_{1i}'P_i (X_{1i}b_i + e_i)
\]

\[
= b_i + (X_{1i}'P_i X_{1i})^{-1}X_{1i}'P_i e_i
\]

Then our estimator of main interest, \( \hat{\beta}_{PCIV} \) can be written as follows:

\[
\hat{\beta}_{PCIV} = \sum_{i=1}^{n} w_i \hat{b}_i
\]

\[
= \sum_{i=1}^{n} w_i (\beta + d_i + (X_{1i}'P_i X_{1i})^{-1}X_{1i}'P_i e_i)
\]

\[
= \beta + \sum_{i=1}^{n} w_i d_i + \sum_{i=1}^{n} w_i (X_{1i}'P_i X_{1i})^{-1}X_{1i}'P_i e_i
\]

As \( MSE(\hat{\beta}_{PCIV}) = (Bias(\hat{\beta}_{PCIV}))^2 + V(\hat{\beta}_{PCIV}) \), we will show each term converges to zero asymptotically. Note that the weight, \( w_i \), is known and satisfies the condition as in Assumption (A6).

\[
Bias(\hat{\beta}_{PCIV}) = E[\hat{\beta}_{PCIV} - \beta]
\]

\[
= E \left[ \sum_{i=1}^{n} w_i (\hat{b}_i - \beta) \right]
\]
\[
E[\hat{b}_i - b_i] = E\left[ (X'_{1i} P_i X_{1i})^{-1} X'_{1i} P_i e_i \right]
= (E[X'_{1i} P_i X_{1i}]^{-1}) E[X'_{1i} P_i e_i]
\]

Note that \( X_{1i} = Z_i \gamma_i + X_{2i} \eta + u_i \) as in equation 1. Then, both terms in the denominator and the numerator can be written as follows:

\[
E[X'_{1i} P_i X_{1i}] = E\left[ (Z_i \gamma_i + X_{2i} \eta + u_i)' P_i (Z_i \gamma_i + X_{2i} \eta + u_i) \right]
= E[\gamma_i' Z_i' P_i Z_i \gamma_i] + E[\eta' X_{2i}' P_i X_{2i} \eta]
+ E[\eta' X_{2i}' P_i Z_i \gamma_i] + E[u_i' P_i Z_i \gamma_i] + E[\gamma_i' Z_i' P_i X_{2i} \eta]
+ E[u_i' P_i X_{2i} \eta] + E[\gamma_i' Z_i' P_i u_i] + E[\eta' X_{2i}' P_i u_i] + E[u_i' P_i u_i]
\]

Note that \( P_i Z_i = H_{Z_i} Z_i + M_{Z_i} (X_{2i}' M_{Z_i} X_{2i})^{-1} X_{2i}' M_{Z_i} Z_i \) and \( X_{2i}' P_i X_{2i} = X_{2i}' X_{2i} \).

Also, \( E[u_i' P_i Z_i \gamma_i] = 0 \), \( E[u_i' P_i X_{2i} \eta] = 0 \), \( E[\gamma_i' Z_i' P_i u_i] = 0 \), and \( E[\eta' X_{2i}' P_i u_i] = 0 \) by Assumption (A2). Also, as \( \text{rank}(P_i) = L + H \), we get \( E[u_i' P_i u_i] = (L + H) \cdot \sigma_u^2 \). Then,

\[
E[X'_{1i} P_i X_{1i}] = \gamma_i' Z_i' Z_i \gamma_i + \eta' X_{2i}' Z_i \gamma_i + \gamma_i' Z_i' X_{2i} \eta + \eta' X_{2i}' X_{2i} \eta + (L + H) \cdot \sigma_u^2.
\]

By WLLN, as \( \frac{1}{T} Z_i' Z_i \overset{P}{\to} E[Z_i' Z_i] \equiv Q_{ZZ} \), the first term \( \gamma_i' Z_i' Z_i \gamma_i = O_p(T) \). Likewise, the second, third, and the fourth terms follow the order of \( T \). Next, the numerator in \( E[\hat{b}_i - b_i] \) can be simplified as follows. With \( M_{Z_i} Z_i = 0 \) and (A2), the first and second terms become zero.
\[
E[X'_i P_i e_i] = E[(Z_i \gamma_i + X_{2i} \eta + u_i)' P_i e_i] \\
= E[\gamma'_i Z_i' P_i e_i] + E[\eta' X'_{2i} P_i e_i] + E[u'_i P_i e_i] \\
= (L + H) \cdot \sigma_{u,e}
\]

We write

\[
E[\hat{b}_i - b_i] = \frac{(L + H) \cdot \sigma_{u,e}}{\gamma'_i Z_i' Z_i \gamma_i + \eta' X'_{2i} Z_i \gamma_i + \gamma'_i Z_i' X_{2i} \eta + \eta' X'_{2i} X_{2i} \eta + (L + H) \cdot \sigma_u^2} = O_p(T^{-1}).
\]

Then, \(\text{Bias}(\hat{\beta}_{PCIV}) = O_p(T^{-1})\).

Now, we will look at the variance of \(\hat{\beta}_{PCIV}\). By Assumption (A1),

\[
V(\hat{\beta}_{PCIV} - \beta) = V\left(\sum_{i=1}^n w_i d_i + \sum_{i=1}^n w_i (\hat{b}_i - b_i)\right) \\
= \sum_{i=1}^n w_i^2 V(d_i) + \sum_{i=1}^n w_i^2 V(\hat{b}_i - b_i)
\]

First, \(V(d_i) = \frac{1}{n} \sum_{i=1}^n d_i d_i' \equiv \sigma_d^2 I_K\). Second,

\[
V(\hat{b}_i - b_i) = V((X'_{1i} P_i X_{1i})^{-1} X'_{1i} P_i e_i) \\
= E[(X'_{1i} P_i X_{1i})^{-1} X'_{1i} P_i e_i e'_i P_i X_{1i} (X'_{1i} P_i X_{1i})^{-1}].
\]

We will break down by each component of the variance.

\[
X'_{1i} P_i X_{1i} = X'_{1i} H Z_i X_{1i} + X'_{1i} M Z_i X_{2i} (X'_{2i} M Z_i X_{2i})^{-1} X'_{2i} M Z_i X_{1i} \\
= X'_{1i} (Z'_{i} Z_i)^{-1} Z'_i X_{1i} + X'_{1i} (I_N - Z_i (Z'_{i} Z_i)^{-1} Z'_i) X_{2i} (X'_{2i} (I_N - Z_i (Z'_{i} Z_i)^{-1} Z'_i) X_{2i})^{-1} \\
\times X'_{2i} (I_N - Z_i (Z'_{i} Z_i)^{-1} Z'_i) X_{1i}
\]
By WLLN, \( \frac{1}{T} \mathbf{X}'_{1i} \mathbf{Z}_i \xrightarrow{p} \mathbb{E}[\mathbf{X}'_{1i} \mathbf{Z}_i] \equiv Q_{1Z} \). Likewise, we define \( Q_{Z1} \equiv \mathbb{E}[\mathbf{Z}'_i \mathbf{X}_{1i}] \), \( Q_{ZZ} \equiv \mathbb{E}[\mathbf{Z}'_i \mathbf{Z}_i] \), \( Q_{Z2} \equiv \mathbb{E}[\mathbf{Z}'_i \mathbf{X}_{2i}] \), \( Q_{22} \equiv \mathbb{E}[\mathbf{X}'_{2i} \mathbf{X}_{2i}] \), \( Q_{12} \equiv \mathbb{E}[\mathbf{X}'_{1i} \mathbf{X}_{2i}] \), and \( Q_{21} \equiv \mathbb{E}[\mathbf{X}'_{2i} \mathbf{X}_{1i}] \). Then, we write
\[
\frac{1}{T} \mathbf{X}'_{1i} \mathbf{P}_i \mathbf{X}_{1i} = Q_{1Z} Q_P Q_{Z1}
\]
asymptotically, where \( Q_P = Q_{ZZ}^{-1} + (Q_{12} - Q_{1Z} Q_{ZZ}^{-1} Q_{Z2})(Q_{22} - Q_{ZZ}^{-1} Q_{Z2})^{-1}(Q_{21} - Q_{ZZ}^{-1} Q_{Z1}) \). Next, the second component of the variance is written as below.

By WLLN, we define \( \frac{1}{T} \mathbf{Z}'_i \mathbf{e}_i \mathbf{e}'_i \mathbf{Z}_i \xrightarrow{p} \mathbb{E}[\mathbf{Z}'_i \mathbf{e}_i \mathbf{e}'_i \mathbf{Z}_i] \equiv Q_{Ze} \). Then, we write \( \mathbf{X}'_{1i} \mathbf{P}_i \mathbf{e}_i \mathbf{e}'_i \mathbf{P}_i \mathbf{X}_{1i} = Q_{1Z} Q_P Q_{Z2} \). By CMT,
\[
V(\mathbf{b}_i - \mathbf{b}_i) = \frac{1}{T}(Q_{1Z} Q_P Q_{Z1})^{-1}(Q_{1Z} Q_P Q_{Z2} Q_P Q_{Z1})(Q_{1Z} Q_P Q_{Z1})^{-1} = O_p(T^{-1})
\]
Then, we have \( V(\mathbf{\hat{b}}_{PCIV}) = O_p(1/n) + O_p(1/nT) = O_p(1/n) \). To summarize,
\[
MSE(\mathbf{\hat{b}}_{PCIV}) = (Bias(\mathbf{\hat{b}}_{PCIV}))^2 + V(\mathbf{\hat{b}}_{PCIV}) = O_p(1/T^2) + O_p(1/n).
\]
As we assume Assumption (A5), we can show that \( \lim_{n,T \to \infty} MSE(\mathbf{\hat{b}}_{PCIV}) \xrightarrow{p} 0 \). As \( n,T \to \infty \),
\[
\mathbf{\hat{b}}_{PCIV} \xrightarrow{p} \mathbf{\beta}.
\]
B  Proof of Theorem 2

First, we will show the consistency of an estimated variance.

\[ \hat{V}(\hat{\beta}_{PCIV} - \beta) = \hat{V} \left( \sum_{i=1}^{n} w_i d_i + \sum_{i=1}^{n} w_i (X'_{1i} P_i X_{1i})^{-1} X'_{1i} P_i e_i \right) \]

By using Assumptions (A1) and (A2),

\[ \hat{V}(\hat{\beta}_{PCIV} - \beta) = \sum_{i=1}^{n} w_i^2 \hat{V}(d_i) + \sum_{i=1}^{n} w_i^2 \hat{V}((X'_{1i} P_i X_{1i})^{-1} X'_{1i} P_i e_i) \]

First, we will show \( \hat{V}(d_i) \to V(d_i) \).

\[ \hat{V}(d_i) = \frac{1}{n} \sum_{i=1}^{n} \hat{d}_i \hat{d}_i' = \frac{1}{n} \sum_{i=1}^{n} (d_i - d_i + d_i) (\hat{d}_i - d_i + d_i)' \]

\[ = \frac{1}{n} \sum_{i=1}^{n} d_i d_i' + \frac{1}{n} \sum_{i=1}^{n} (\hat{d}_i - d_i) (\hat{d}_i - d_i)' \]

By WLLN, it is easy to show that \( \frac{1}{n} \sum_{i=1}^{n} d_i d_i' \overset{p}{\to} \sigma_d^2 \mathbf{I}_K \) as \( E[d_i] = 0 \). Also, as \( \hat{d}_i \overset{p}{\to} d_i \) as \( n \to \infty \), the second term then converges to zero asymptotically. Therefore, we can show \( \hat{V}(d_i) \to \sigma_d^2 \mathbf{I}_K \equiv V(d_i) \) asymptotically. Next, let’s show the convergence of the second term of the sample variance.

\[ V((X'_{1i} P_i X_{1i})^{-1} X'_{1i} P_i e_i) = E[(X'_{1i} P_i X_{1i})^{-1} X'_{1i} P_i \hat{e}_i \hat{e}_i' P_i X'_{1i}(X'_{1i} P_i X_{1i})^{-1}] \]

Given that \( P_i = H_{Z_i} + M_{Z_i} X_{2i} (X_{2i}' M_{Z_i} X_{2i})^{-1} X_{2i}' M_{Z_i} \), we will show that \( \frac{1}{T} Z_i' \hat{e}_i \hat{e}_i' Z_i \overset{p}{\to} E[Z_i' e_i e_i' Z_i] \equiv \Omega_{Z_i} \).

Next, let’s show the convergence of the second term in equation \( \text{10} \) Using the above expression, we will show the convergence of the below inequality.

\[ \left\| \frac{1}{T} Z_i' (\hat{e}_i - e_i) (\hat{e}_i - e_i)' Z_i \right\| \leq \frac{1}{T} \| Z_i \|^2 \| \hat{e}_i - e_i \|^2 \] (9)
Using $\hat{X}_{1i} = Z_i \hat{\gamma}_i + X_{2i} \hat{\eta}$, we write $\tilde{e}_i = y_i - \hat{X}_{1i} \hat{b}_i - X_{2i} \hat{\delta} = e_i - Z_i (\hat{\gamma}_i - \gamma_i) (\hat{b}_i - b_i) - X_{2i} (\hat{\eta} - \eta) (\hat{b}_i - b_i) - Z_i (\hat{\gamma}_i - \gamma_i) b_i - X_{2i} (\hat{\gamma}_i - \gamma_i) b_i - X_{2i} \gamma_i (\hat{b}_i - b_i) - X_{2i} \eta (\hat{b}_i - b_i) - X_{2i} (\delta - \delta)$.

Then, we write equation 9 as follows.

$$\frac{1}{T} \|Z_i\|^2 \|\tilde{e}_i - e_i\|^2$$

$$\leq \frac{1}{T} \|b_i - b_i\|^2 \|\tilde{\gamma}_i - \gamma_i\|^2 \|Z_i\|^2 + \frac{1}{T} \|b_i - b_i\|^2 \|\tilde{\eta} - \eta\|^2 \|X_{2i}\|^2 \|Z_i\|^2 + \frac{1}{T} \|b_i - b_i\|^2 \|\tilde{\gamma}_i - \gamma_i\|^2 \|Z_i\|^2$$

$$\leq \frac{1}{T} \|\hat{\delta} - \delta\|^2 \|X_{2i}\|^2 \|Z_i\|^2 + 2 \frac{1}{T} \|\hat{b}_i - b_i\|^2 \|\tilde{\gamma}_i - \gamma_i\|^2 \|Z_i\|^3 \|X_{2i}\| \|\tilde{\eta} - \eta\| \|b_i\|$$

$$+ \frac{1}{T} \|\hat{b}_i - b_i\|^2 \|\tilde{\gamma}_i - \gamma_i\|^2 \|Z_i\|^4 + 2 \frac{1}{T} \|\hat{b}_i - b_i\|^2 \|\tilde{\gamma}_i - \gamma_i\|^2 \|Z_i\|^3 \|X_{2i}\| \|\tilde{\eta} - \eta\| \|b_i\|$$

The convergence of the above inequality can be shown by the consistency of the three estimators respectively: 1) $\hat{\eta} \xrightarrow{P} \eta$, 2) $\hat{\gamma}_i \xrightarrow{P} \gamma_i$, and 3) $\hat{\delta} \xrightarrow{P} \delta$. In addition, using the Hölder’s inequality, we can easily show $E[\|Z_i\|^3 \|X_{2i}\|] \leq \left( E[\|Z_i\|^3 \|X_{2i}\|] \right)^{\frac{3}{4}} \left( E[\|X_{2i}\|^4] \right)^{\frac{1}{4}} < \infty$ under Assumption (A4).
First, \( \hat{\eta} = \eta + \left( \sum_{i=1}^{n} X'_{2i}M_{Zi}X_{2i} \right)^{-1} \left( \sum_{i=1}^{n} X'_{2i}M_{Zi}u_i \right) \). By Assumption (A3),

\[
\text{plim}_{n,T \to \infty} \hat{\eta} = \eta + (Q_{2Z}Q_{ZZ}^{-1}Q_{Z2})^{-1}Q_{2Z}Q_{ZZ}^{-1} \text{plim}_{n,T \to \infty} \frac{1}{nT} \sum_{i=1}^{n} Z'_{i}u_i = \eta
\]

Next, \( \hat{\gamma}_i = \gamma_i + (Z'_iZ_i)^{-1}Z'_iu_i + (Z'_iZ_i)^{-1}Z'_{2i}(\hat{\eta} - \eta) \). Under Assumption (A3) and the consistency of \( \eta \),

\[
\text{plim}_{n,T \to \infty} \hat{\gamma}_i = \gamma_i + Q_{ZZ}^{-1} \text{plim}_{n,T \to \infty} \frac{1}{T}Z'_{i}u_i + Q_{ZZ}^{-1}Q_{Z2} \text{plim}_{N,T \to \infty} (\hat{\eta} - \eta) = \gamma_i
\]

Lastly, \( \hat{\delta} = \delta + \left( \sum_{i=1}^{n} X'_{2i}M_{X_{1i}}X_{2i} \right)^{-1} \left( \sum_{i=1}^{n} X'_{2i}M_{X_{1i}}e_i \right) \), where \( M_{X_{1i}} = I_T - \hat{X}_{1i}(\hat{X}'_{1i}\hat{X}_{1i})^{-1}\hat{X}'_{1i} = I_T - P_iX_{1i}(X'_{1i}P_iX_{1i})^{-1}X'_{1i}P_i' \). Define \( Q_P = Q_{ZZ}^{-1} + (Q_{12} - Q_{1Z}Q_{ZZ}^{-1}Q_{Z2})(Q_{22} - Q_{2Z}Q_{ZZ}^{-1}Q_{Z2})^{-1}(Q_{21} - Q_{2Z}Q_{ZZ}^{-1}Q_{Z1}) \).

\[
\text{plim}_{n,T \to \infty} \hat{\delta} = \delta + (Q_{2Z} - Q_{2Z}Q_PQ_{Z1}(Q_{1Z}Q_PQ_{Z1})^{-1}Q_{1Z}Q_PQ_{Z2})^{-1} \times \left[ \text{plim}_{n,T \to \infty} \frac{1}{nT} \sum_{i=1}^{n} X'_{2i}e_i + Q_{2Z}Q_PQ_{Z1}(Q_{1Z}Q_PQ_{Z1})^{-1}Q_{1Z}Q_P \text{plim}_{n,T \to \infty} \frac{1}{nT} \sum_{i=1}^{n} Z'_ie_i \right] = \delta,
\]

By WLLN, \( \frac{1}{T}Z'_i\hat{e}_i\hat{e}'_iZ_i \xrightarrow{p} E[Z'_ie_i\hat{e}'_i] \equiv \Omega_{Ze} \). As \( n, T \to \infty \), and \( n/T \to c \) where \( 0 < c < \infty \),

\[
\hat{V}(\hat{\beta}_{PCIV}) \xrightarrow{p} V(\hat{\beta}_{PCIV}).
\]

Now, we show the asymptotic normality of \( \hat{\beta}_{PCIV} \).

\[
\frac{1}{T}Z'_i\hat{e}_i\hat{e}'_iZ_i = \frac{1}{T}Z'_ie_i\hat{e}'_iZ_i + \frac{1}{T}Z'_i(\hat{e}_i - e_i)(\hat{e}_i - e_i)'Z_i (10)
\]

Using the Cauchy-Schwarz inequality, we can show that \( \Omega_{Ze} \) is finite by Assumptions (A2) and (A3). Note that (\( E[e'_{ij}] \)) \( \frac{1}{T} = (E[(y_{ij} - x_{1ij}b_i - x_{2ij}\delta)^4]) \) \( \frac{1}{T} \leq (E[y_{ij}']) \) \( \frac{1}{T} + \|b_i\|(E[x_{2ij}^4]) \) \( \frac{1}{T} + \|b_i\|(E[x_{2ij}^4]) \) \( \frac{1}{T} \).
\[\|\delta\|(E[|x_{2,ij}|])^{\frac{1}{4}} < \infty \text{ by Assumption (A4). Then,}\]

\[\|\Omega Ze\| \leq E\left[\|Z_i\|^2 \|e_i\|^2\right] \leq (E[\|Z_i\|^4])^{\frac{1}{2}} (E[\|e_i\|^4])^{\frac{1}{2}} < \infty.\]

. We then have \(\frac{1}{T} Z_i'e_i \xrightarrow{d} N(0, \Omega Ze)\).

\[\sqrt{n}(\hat{\beta}_{PCIV} - \beta) = \sqrt{n} \sum_{i=1}^{n} w_i d_i + \sqrt{n} \sum_{i=1}^{n} w_i (X_i'P_iX_i)^{-1} X_i'P_i e_i\]

\[\xrightarrow{O_p(1)} \quad \xrightarrow{O_p\left(\frac{\sqrt{n}T}{\sqrt{n}}\right)}\]

\[\xrightarrow{d} N(0, V(\hat{\beta}))\]

where \(V(\hat{\beta}) = \lambda(\sigma_d^2 I_K + (Q_1ZQ_PQ_{Z1})^{-1}Q_1ZQ_P\Omega ZeQ_PQ_{Z1}(Q_1ZQ_PQ_{Z1})^{-1})\), and \(\lambda = O_p(1)\).
C Additional Simulation Results

Here, we present additional summaries of the simulations, performance evaluation of the estimators with finite numbers of clusters, and performance evaluation of the estimators with heterogeneous first-stage coefficients. Figure C.1 provides a summary of the main simulation results. It shows the kernel density plot of the bias over each simulation, maintaining the uncorrelated covariance assumption on the left and violating it on the right. Further, we show these density plots first with 250 clusters and 250 observations per cluster at the top, then with only the number of clusters reduced to 10, and finally with 250 clusters and 10 observations per cluster at the bottom. Table C.1 summarizes point estimates from the simulations.

Figure C.2 shows the average bias, the RMSE, the ratio of standard errors to standard deviation of estimates across simulations, and the 95 percent coverage rates in the three estimators with T fixed at 250 as n increases, again both maintaining and violating the key assumption.

The primary advantage of PCIV over P2SLS and FEIV is its robustness to possible correlations between heterogeneous slopes (b_i) and first-stage variation (\tilde{z}_{it}\tilde{x}_{it}). One way in which \tilde{z}_{it}\tilde{x}_{it} may vary across clusters is through heterogeneous first-stage coefficients, though it is certainly not the only way. Here, we demonstrate the performance of PCIV with heterogeneous first-stage coefficients.

The data-generating process we employ here is similar to that used in Section 4 in the main text except for a few changes. First, whereas in the main text \gamma = 1, here \gamma_i \sim N(1,0.1) varies by cluster. Second, to demonstrate how the performance of the estimators change as the correlation between b_i and \tilde{z}_{it}\tilde{x}_{it} grows we generate b_i, x_{it}, and z_{it} so that we can vary the correlation between them according to weight, \kappa, that varies between 0 and 1. Thus, b_1 = 1 + d_i and d_i = \kappa \times d_{bi} + (1 - \kappa)d_{ai}. We introduce s_i \sim N(0,0.25) and construct z_{ij} \sim N(0,\exp(\kappa d_{bi} + (1-\kappa)s_i)). We introduce q_i \sim N(0,0.25) and construct the idiosyncratic error component of x_{it}, \epsilon_{ij} \sim N(0,\exp(\kappa d_{bi} + (1-\kappa)q_i)).
The simulation results appear in figure C.3. The bias and RMSE of FEIV and P2SLS rise smoothly as the correlation between the heterogeneous slopes \(b_i\) and the first-stage variation \(\tilde{z}_{it}\tilde{x}_{it}\) rises, while both remain flat for PCIV. Likewise, the coverage rates of FEIV and P2SLS fall, while for PCIV they remain quite close to 0.95.

Table C.1: Comparison of Estimates for \(\hat{\beta}[x_{ij}]\) with Simulated Data

<table>
<thead>
<tr>
<th>Method</th>
<th>Uncorrelated Covariance</th>
<th>Correlated Covariance</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Bias</td>
<td>SD</td>
</tr>
<tr>
<td>P2SLS</td>
<td>0.000</td>
<td>0.020</td>
</tr>
<tr>
<td>FEIV</td>
<td>0.000</td>
<td>0.020</td>
</tr>
<tr>
<td>PCIV</td>
<td>0.000</td>
<td>0.017</td>
</tr>
<tr>
<td>n = 250, T = 250</td>
<td></td>
<td></td>
</tr>
<tr>
<td>P2SLS</td>
<td>0.000</td>
<td>0.089</td>
</tr>
<tr>
<td>FEIV</td>
<td>0.000</td>
<td>0.090</td>
</tr>
<tr>
<td>PCIV</td>
<td>0.000</td>
<td>0.083</td>
</tr>
<tr>
<td>n = 10, T = 250</td>
<td></td>
<td></td>
</tr>
<tr>
<td>P2SLS</td>
<td>0.001</td>
<td>0.035</td>
</tr>
<tr>
<td>FEIV</td>
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<td>0.038</td>
</tr>
<tr>
<td>PCIV</td>
<td>-0.017</td>
<td>0.048</td>
</tr>
</tbody>
</table>

Note: Both bias and RMSE are multiplied by 100. P2SLS=Pooled Two-Stage Least Squares; FEIV=Fixed Effects Instrumental Variable; PCIV=Per-Cluster Instrumental Variable; RMSE=Root Mean Squared Error; \(\frac{\text{MeanSE}}{SD}\)=Ratio of the mean of standard errors divided by standard deviations; CR=Coverage Rate.
Figure C.1: Kernel Density Plots of Estimation Errors, $\hat{\beta} - \beta$

Notes: $\hat{\beta}$ is the coefficient of $x_{ij}$ across replications for all methods. The left panels are when the uncorrelated covariance assumption holds, and the right panels are when it is violated. P2SLS = Two-Stage Least Squares; FEIV = Fixed Effects Instrumental Variable; PCIV = per-cluster instrumental variables.
Figure C.2: Simulation results across number of clusters

(a) Bias for coefficient $\hat{\beta}$ of $x_{ij}$

(b) Root mean square error for coefficient $\hat{\beta}$ of $x_{ij}$

(c) Mean standard errors over estimates’ standard deviations

(d) Standard error coverage rates

Notes: P2SLS = Pooled Two-Stage Least Squares; FEIV = Fixed Effects Instrumental Variables; PCIV = Per-Cluster Instrumental Variables. Each point represents the results from 500 repetitions. Within each panel, figures on the left are when the uncorrelated covariance assumption holds, and figures on the right are when it is violated. The ratio of mean standard errors (SEs) divided by standard deviations (SDs) of the estimates. The horizontal line in (c) denotes a ratio of one. The horizontal line in (d) is to denote the exact 95 percent coverage rate. In many instances, FEIV total overlaps with P2SLS, though this is an artifact of the specific DGP in this simulation.
Figure C.3: Simulation results across correlations between first-stage variation and effect-heterogeneity with heterogeneous first-stage coefficients

(a) Bias for coefficient $\hat{\beta}$ of $x_{ij}$

(b) Root mean square error for coefficient $\hat{\beta}$ of $x_{ij}$

(c) Mean standard errors over estimates’ standard deviations

(d) Standard error coverage rates

Notes: P2SLS = Pooled Two-Stage Least Squares; FEIV= Fixed Effects Instrumental Variables; PCIV=Per-Cluster Instrumental Variables. Each point represents the results from 500 repetitions. Within each panel, figures on the left are when the uncorrelated covariance assumption holds, and figures on the right are when it is violated. The ratio of mean standard errors (SEs) divided by standard deviations (SDs) of the estimates. The horizontal line in (c) denotes a ratio of one. The horizontal line in (d) is to denote the exact 95 percent coverage rate. In many instances, FEIV totally overlaps with P2SLS, though this is an artifact of the specific DGP in this simulation.
D Supplementary tables and figures

Figure D.1: Relationship between tax changes and public transportation

Notes: We relate the log population share that used public transportation in 1980 to the log of the cumulative gas tax changes in the state. By using a measure of public transportation that predates our tax changes, we hope to avoid the simultaneity of ridership responding to the tax changes. Each point represents a state and the regression is over 50 states plus Washington D.C.
Table D.1: Difference between EIA and GasBuddy Data (March 2009 - February 2011)

<table>
<thead>
<tr>
<th>State</th>
<th>EIA Mean</th>
<th>EIA Std</th>
<th>GasBuddy Mean</th>
<th>GasBuddy Std</th>
<th>Difference Mean</th>
<th>Difference Std</th>
</tr>
</thead>
<tbody>
<tr>
<td>AL</td>
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<td>1.28</td>
</tr>
<tr>
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<td>25.93</td>
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<td>26.62</td>
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<td>1.65</td>
</tr>
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<td>25.63</td>
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<td>2.11</td>
</tr>
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<td>247.93</td>
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</tr>
</tbody>
</table>

Notes: This is the level difference between the EIA data and Gasbuddy data during the overlapping period between March 2009 and February 2011. Due to missing values of the EIA data, they are excluded from the calculation.
Table D.2: Summary Statistics

<table>
<thead>
<tr>
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<th>Mean</th>
<th>SD</th>
<th>p25</th>
<th>Median</th>
<th>p75</th>
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<tbody>
<tr>
<td>After-tax price (1999 USD)</td>
<td>2.69</td>
<td>0.93</td>
<td>1.97</td>
<td>2.34</td>
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<tr>
<td>State taxes (1999 USD)</td>
<td>0.52</td>
<td>0.09</td>
<td>0.45</td>
<td>0.52</td>
<td>0.58</td>
</tr>
<tr>
<td>Unemployment rate</td>
<td>5.54</td>
<td>1.86</td>
<td>4.20</td>
<td>5.20</td>
<td>6.60</td>
</tr>
<tr>
<td>Real per-capita income (1999 USD thousands)</td>
<td>39.37</td>
<td>20.42</td>
<td>21.47</td>
<td>35.80</td>
<td>54.19</td>
</tr>
<tr>
<td>Population (in millions)</td>
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<td>6.43</td>
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<td>6.73</td>
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<td>Licensed drivers (in millions)</td>
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<td>4.16</td>
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<td>2.85</td>
<td>4.94</td>
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<td>Road miles (in thousands)</td>
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<td>55.70</td>
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<tr>
<td>Minimum temperature (degrees F)</td>
<td>40.99</td>
<td>17.05</td>
<td>28.70</td>
<td>41.40</td>
<td>54.70</td>
</tr>
<tr>
<td>Average temperature (degrees F)</td>
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<td>17.82</td>
<td>38.90</td>
<td>53.35</td>
<td>66.90</td>
</tr>
<tr>
<td>Maximum temperature (degrees F)</td>
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<td>65.30</td>
<td>79.00</td>
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<td>Rainfall (inches)</td>
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<td></td>
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Table D.3: First-Stage Estimation Results

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<th>Without volume weights</th>
<th>Volume weighted</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>P2SLS</td>
<td>FEIV</td>
</tr>
<tr>
<td>Log tax</td>
<td>0.204</td>
<td>0.248</td>
</tr>
<tr>
<td></td>
<td>(0.034)</td>
<td>(0.028)</td>
</tr>
<tr>
<td>First-stage F-statistic</td>
<td>36.66</td>
<td>79.71</td>
</tr>
<tr>
<td>Controls</td>
<td>N</td>
<td>N</td>
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<tr>
<td>Log tax</td>
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<td>0.241</td>
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<tr>
<td></td>
<td>(0.034)</td>
<td>(0.027)</td>
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<td>First-stage F-statistic</td>
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<td>80.92</td>
</tr>
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<td>Controls</td>
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<td>Y</td>
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</table>

Notes: Standard errors are clustered by state. The calculated first-stage F-statistics for P2SLS and FEIV are obtained from the regression of each endogenous regressor on the exogenous regressors and the instruments. The calculation of the first-stage F-statistics for the PCIV was done using Hotelling’s T-squared test.
Table D.4: Estimated elasticities using month and year fixed effect

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<th></th>
<th>Without volume weights</th>
<th>Volume weighted</th>
</tr>
</thead>
<tbody>
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<td></td>
<td>P2SLS</td>
<td>FEIV</td>
</tr>
<tr>
<td>Log price</td>
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<td>-0.884</td>
</tr>
<tr>
<td></td>
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<td>(0.389)</td>
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<td>First-stage F-statistic</td>
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<tr>
<td>Controls</td>
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<td>N</td>
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</tbody>
</table>

Notes: All regressions include month and year-fixed effects instead of month-by-year fixed effects. The calculated first-stage F-statistics for P2SLS and FEIV are obtained from the regression of each endogenous regressor on the exogenous regressors and the instruments. The calculation of the first-stage F-statistics for the PCIV was done using Hotelling’s T-squared test.
Table D.5: State-Specific Statistics

<table>
<thead>
<tr>
<th>State</th>
<th>First-stage Coefficient</th>
<th>First-stage F-stat</th>
<th>Second-Stage Coefficient</th>
<th>State</th>
<th>First-stage Coefficient</th>
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<tr>
<td>CA</td>
<td>0.26</td>
<td>96.98</td>
<td>-0.55</td>
<td>NJ</td>
<td>0.29</td>
<td>65.23</td>
<td>-0.66</td>
</tr>
<tr>
<td>CO</td>
<td>0.39</td>
<td>925.73</td>
<td>-0.44</td>
<td>NM</td>
<td>0.36</td>
<td>1,067.34</td>
<td>-0.56</td>
</tr>
<tr>
<td>CT</td>
<td>0.26</td>
<td>1,684.51</td>
<td>-0.60</td>
<td>NY</td>
<td>0.16</td>
<td>350.58</td>
<td>-0.59</td>
</tr>
<tr>
<td>DE</td>
<td>0.19</td>
<td>553.34</td>
<td>-0.62</td>
<td>NC</td>
<td>0.27</td>
<td>542.76</td>
<td>-0.51</td>
</tr>
<tr>
<td>DC*</td>
<td>0.61</td>
<td>7.81</td>
<td>-1.55</td>
<td>ND</td>
<td>0.35</td>
<td>148.33</td>
<td>-0.48</td>
</tr>
<tr>
<td>FL</td>
<td>0.11</td>
<td>65.81</td>
<td>-0.49</td>
<td>OH</td>
<td>0.30</td>
<td>321.95</td>
<td>-0.68</td>
</tr>
<tr>
<td>GA*</td>
<td>-0.03</td>
<td>5.16</td>
<td>-0.49</td>
<td>OK</td>
<td>0.17</td>
<td>48.56</td>
<td>-0.60</td>
</tr>
<tr>
<td>HI*</td>
<td>0.08</td>
<td>2.57</td>
<td>-0.34</td>
<td>OR</td>
<td>0.27</td>
<td>160.17</td>
<td>-0.56</td>
</tr>
<tr>
<td>ID</td>
<td>0.40</td>
<td>63.60</td>
<td>-0.28</td>
<td>PA</td>
<td>0.30</td>
<td>645.35</td>
<td>-0.98</td>
</tr>
<tr>
<td>IL</td>
<td>0.26</td>
<td>585.79</td>
<td>-0.61</td>
<td>RI</td>
<td>0.33</td>
<td>852.93</td>
<td>-0.62</td>
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<tr>
<td>IN*</td>
<td>0.03</td>
<td>2.92</td>
<td>-0.57</td>
<td>SC</td>
<td>0.26</td>
<td>352.31</td>
<td>-0.38</td>
</tr>
<tr>
<td>IA</td>
<td>0.17</td>
<td>202.26</td>
<td>-0.78</td>
<td>SD</td>
<td>0.38</td>
<td>565.64</td>
<td>-0.56</td>
</tr>
<tr>
<td>KS</td>
<td>0.30</td>
<td>378.40</td>
<td>-0.57</td>
<td>TN</td>
<td>0.30</td>
<td>854.90</td>
<td>-0.67</td>
</tr>
<tr>
<td>KY</td>
<td>0.22</td>
<td>353.23</td>
<td>-0.64</td>
<td>TX</td>
<td>0.31</td>
<td>985.06</td>
<td>-0.40</td>
</tr>
<tr>
<td>LA</td>
<td>0.32</td>
<td>1,000.56</td>
<td>-0.46</td>
<td>UT</td>
<td>0.30</td>
<td>149.98</td>
<td>-0.42</td>
</tr>
<tr>
<td>ME</td>
<td>0.44</td>
<td>276.81</td>
<td>-0.74</td>
<td>VT</td>
<td>0.22</td>
<td>188.52</td>
<td>-0.33</td>
</tr>
<tr>
<td>MD</td>
<td>0.25</td>
<td>1,037.18</td>
<td>-0.54</td>
<td>VA</td>
<td>0.30</td>
<td>1,249.75</td>
<td>-0.59</td>
</tr>
<tr>
<td>MA</td>
<td>0.27</td>
<td>654.83</td>
<td>-0.66</td>
<td>WA</td>
<td>0.47</td>
<td>33.15</td>
<td>-0.52</td>
</tr>
<tr>
<td>MI*</td>
<td>0.01</td>
<td>0.64</td>
<td>-0.64</td>
<td>WV</td>
<td>0.33</td>
<td>626.07</td>
<td>-0.34</td>
</tr>
<tr>
<td>MN</td>
<td>0.43</td>
<td>457.88</td>
<td>-0.58</td>
<td>WI</td>
<td>0.35</td>
<td>572.51</td>
<td>-0.51</td>
</tr>
<tr>
<td>MS</td>
<td>0.36</td>
<td>1,207.74</td>
<td>-0.45</td>
<td>WY</td>
<td>0.23</td>
<td>67.84</td>
<td>-0.32</td>
</tr>
<tr>
<td>MO</td>
<td>0.24</td>
<td>311.03</td>
<td>-0.60</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Notes: All estimates are from PCIV estimation without covariates. "*" denotes states with first-stage F-statistics lower than 10.
Table D.6: Analysis by Petroleum Administration For Defense District (PADD)

<table>
<thead>
<tr>
<th>PADD</th>
<th>New England</th>
<th>Central Atlantic</th>
<th>Lower Atlantic</th>
<th>Midwest</th>
<th>Gulf Coast</th>
<th>Rocky Mountains</th>
<th>West Coast</th>
</tr>
</thead>
<tbody>
<tr>
<td>log price</td>
<td>-0.970</td>
<td>-1.160</td>
<td>-0.889</td>
<td>-1.011</td>
<td>-0.977</td>
<td>-0.845</td>
<td>-0.866</td>
</tr>
<tr>
<td></td>
<td>(0.369)</td>
<td>(0.369)</td>
<td>(0.369)</td>
<td>(0.369)</td>
<td>(0.369)</td>
<td>(0.369)</td>
<td>(0.369)</td>
</tr>
<tr>
<td>F-statistic</td>
<td>1.83</td>
<td>1.83</td>
<td>1.83</td>
<td>1.83</td>
<td>1.83</td>
<td>1.83</td>
<td>1.83</td>
</tr>
<tr>
<td>Number of states</td>
<td>6</td>
<td>6</td>
<td>6</td>
<td>15</td>
<td>6</td>
<td>5</td>
<td>7</td>
</tr>
<tr>
<td>Observations</td>
<td>2,160</td>
<td>2,160</td>
<td>2,160</td>
<td>5,400</td>
<td>2,160</td>
<td>1,800</td>
<td>2,520</td>
</tr>
</tbody>
</table>

Notes: All regressions include state FE, control for local unemployment rates, and detrended data. State-clustered standard errors appear in parentheses.

E Anticipatory behavior

The difference in estimates between P2SLS applied to first differences and FEIV may imply a violation of the strict exogeneity assumption of the instrument. Indeed in revisiting the analysis of [Davis and Kilian (2011), Coglianese et al. (2017)] note evidence of anticipatory behavior providing one such violation. This violation is particularly important when using first differences in taxes, prices, and quantities, as in [Davis and Kilian (2011)]. Coglianese et al. (2017) accordingly use leads and lags of prices and taxes to address the anticipatory behavior of large consumers on their estimated price elasticity of demand for gasoline.

However, as long as the dependence between lag or lead values of the instrument is only weakly related to the error term, the inconsistency in FEIV from this dependence converges to zero as T grows large (Wooldridge, 2010). In contrast, P2SLS on first differences does not enjoy this same result.\(^\text{22}\) Given that we are flexibly detrending the data, strong dependence seems unlikely. We investigate this possible dependence by running reduced form regression of volume purchases on the log of taxes and a lead of log taxes. Significant coefficient estimates on the lead of log taxes would indicate strong dependence.

We present the results from these regressions in Table E.1. Indeed, examining the coefficient estimates of lead taxes on the volume purchased, we see that the lead is only statistically

\(^{22}\text{See Wooldridge (2010) Chapters 10 and 11 for more complete discussions of the issue.}\)
Table E.1: Anticipatory behavior and dependence in reduced-form regressions

<table>
<thead>
<tr>
<th></th>
<th>Without volume weights</th>
<th>Volume weighted</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>P2SLS</td>
<td>FEIV</td>
</tr>
<tr>
<td>Log tax</td>
<td>-0.150</td>
<td>-0.157</td>
</tr>
<tr>
<td></td>
<td>(0.053)</td>
<td>(0.047)</td>
</tr>
<tr>
<td>Lead of log tax</td>
<td>0.070</td>
<td>-0.043</td>
</tr>
<tr>
<td></td>
<td>(0.026)</td>
<td>(0.066)</td>
</tr>
<tr>
<td>First-stage F-statistic</td>
<td>18.39</td>
<td>44.11</td>
</tr>
</tbody>
</table>

Notes: Headings refer to the estimator for which the reduced form estimates appear. Regressions use the entire sample. The calculation of the first-stage F-statistics for the PCIV was done using Hotelling’s T-squared test. State-clustered standard errors appear in parentheses.

significant with P2SLS applied to the first differences. We find no evidence that additional gasoline purchases in anticipation of tax increases drive the FEIV (or PCIV) estimates, as all the coefficients are negative and quantitatively small. This apparent lack of strong dependence leads us to prefer the FEIV estimates over P2SLS applied to first differences. Despite the small coefficient estimates on the lead of taxes, as a precaution, we follow Coglianese et al. (2017) in examining the sensitivity of elasticity estimates to the inclusion of leads and lags. We report the results from this exercise in Figure E.1 in Appendix D, which shows that the magnitude of FEIV and PCIV estimates are robust to the inclusion of leads and lags of log prices and log taxes.
Figure E.1: Sensitivity of elasticity estimates across specifications by estimator

Notes: Specification options include volume-weighted (W), unweighted (UW), leads (LD), and lags (LG). All elasticity estimates are cumulative as they sum over the contemporaneous lead and lag coefficient estimates where applicable.
We apply all three methods to the data and modeling of Davis and Kilian (2011) and Coglianese et al. (2017) here. Davis and Kilian (2011) provides an early example of instrumenting for gasoline price changes using changes in state gasoline taxes to account for the simultaneity issues in studying prices and quantities. The data comes from the Energy Information Administration and stops in 2008 before the series on state gasoline prices was discontinued. Davis and Kilian (2011) use pooled OLS applied to first-differences in all variables to address unobserved, time-invariant, state-level intercepts.

Coglianese et al. (2017) note apparent anticipatory behavior in gasoline sales to state gasoline taxes changes, violating the strict exogeneity assumption of the instrument. Unlike FEIV and PCIV, this is particularly problematic for first-difference estimation as the inconsistency persists even as the length of the panel grows long (Wooldridge, 2010). As a result, Coglianese et al. (2017) address the issue by examining how the cumulative effect changes when they include a lead and a lag of log prices and instrument for them using a lead and a lag of log taxes. In additional robustness checks, they also include an additional lead and lag of log taxes for over-identified specifications.

We replicate the results from both studies in Table F.1 exploring how the results change with using FEIV and PCIV instead of pooled OLS applied to first-differences and when we apply volume weights with each estimator. The furthest left column provides estimates that are directly comparable to Davis and Kilian (2011) in Panel A and to Coglianese et al. (2017) in Panels B and C. As neither Davis and Kilian (2011) and Coglianese et al. (2017) weight by volume of gasoline sold, we refrain from using volume weights for regressions on the left and apply volume weights on the right. Panel A of Table F.1 presents the estimates of contemporaneous deviations in log gasoline prices on log gasoline sales, instrumented by the contemporaneous deviation in log gasoline taxes. Panel B of Table F.1 accounts for
anticipatory behavior following Coglianese et al. (2017) by including a lead and lag of log prices as additional endogenous regressors instrumenting the set with log taxes and well as the lead and lag of log taxes. The cumulative effect is the sum of all three coefficients. Panel C is similar to Panel B except that we follow Coglianese et al. (2017) in including two leads and two lags of taxes used to instrument for the endogenous prices.

The exercise shows a few key points. First, we replicate the results of Davis and Kilian (2011) and Coglianese et al. (2017) in the first column, which is unsurprising given that Lucas Davis graciously provides all data and code on his website. Second, consistent with theory, FEIV and PCIV are less sensitive to the inclusion of leads and lags of log prices than is pooled 2SLS applied to first-differences. Pooled 2SLS applied to first-differences is the most volatile estimator with both the largest and smallest point estimates depending on the specification. In fact, when we account for anticipatory behavior and weight by the states’ relevance to the market, the cumulative effect of log prices on volume sold switches sign showing demand increasing with an increase in prices. Finally, the PCIV estimates continue to be markedly smaller (and some would say more plausible) than those from FEIV, insinuating that the correlation between first-stage variation and heterogeneous slopes is meaningful.
Table F.1: Replication of Davis and Kilian (2011) and Coglianese et al. (2017)

<table>
<thead>
<tr>
<th></th>
<th>Without volume weights</th>
<th>Volume weighted</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>P2SLS</td>
<td>FEIV</td>
</tr>
</tbody>
</table>

Panel A: Contemporaneous log prices, just identified

<table>
<thead>
<tr>
<th></th>
<th>Cumulative Log price</th>
<th>First-stage F-statistic</th>
</tr>
</thead>
<tbody>
<tr>
<td>DK2011</td>
<td>-1.135 (-0.250)</td>
<td>246.65</td>
</tr>
<tr>
<td></td>
<td>-0.777 (0.394)</td>
<td>82.69</td>
</tr>
<tr>
<td></td>
<td>-0.414 (0.279)</td>
<td>55.64</td>
</tr>
<tr>
<td></td>
<td>-0.714 (0.209)</td>
<td>76.82</td>
</tr>
<tr>
<td></td>
<td>-0.801 (0.327)</td>
<td>28.69</td>
</tr>
<tr>
<td></td>
<td>-0.405 (0.463)</td>
<td>47.99</td>
</tr>
</tbody>
</table>

Panel B: Additional lead and lag of log prices, just identified

<table>
<thead>
<tr>
<th></th>
<th>Cumulative Log price</th>
<th>First-stage F-statistic</th>
</tr>
</thead>
<tbody>
<tr>
<td>CDKS2017</td>
<td>-0.360 (-0.241)</td>
<td>31.21</td>
</tr>
<tr>
<td></td>
<td>-0.691 (0.396)</td>
<td>51.21</td>
</tr>
<tr>
<td></td>
<td>-0.355 (0.356)</td>
<td>54.89</td>
</tr>
<tr>
<td></td>
<td>0.219 (0.509)</td>
<td>54.84</td>
</tr>
<tr>
<td></td>
<td>-0.779 (0.334)</td>
<td>44.61</td>
</tr>
<tr>
<td></td>
<td>-0.348 (0.591)</td>
<td>48.08</td>
</tr>
</tbody>
</table>

Panel C: Additional lead and lag of log prices, over identified

<table>
<thead>
<tr>
<th></th>
<th>Cumulative Log price</th>
<th>First-stage F-statistic</th>
</tr>
</thead>
<tbody>
<tr>
<td>CDKS2017</td>
<td>-0.368 (-0.239)</td>
<td>52.26</td>
</tr>
<tr>
<td></td>
<td>-0.728 (0.402)</td>
<td>82.99</td>
</tr>
<tr>
<td></td>
<td>-0.367 (0.233)</td>
<td>55.04</td>
</tr>
<tr>
<td></td>
<td>0.349 (0.529)</td>
<td>73.32</td>
</tr>
<tr>
<td></td>
<td>-0.781 (0.335)</td>
<td>8.49</td>
</tr>
<tr>
<td></td>
<td>-0.359 (0.388)</td>
<td>47.68</td>
</tr>
</tbody>
</table>

Notes: All regressions include month-by-year fixed effects and control for state unemployment rates. DK2011 corresponds to replications of Davis and Kilian (2011) and CDKS2017 corresponds to Coglianese et al. (2017). Cluster-robust standard errors are in parentheses.