Abstract

We study public policies designed to improve access and reduce costs for In Vitro Fertilization (IVF). High out-of-pocket prices can deter potential patients from IVF, while active patients have an incentive to risk costly high-order pregnancies to improve their odds of treatment success. We analyze IVF’s rich choice structure by estimating a dynamic model of patients’ choices within and across treatments. Policy simulations show that insurance mandates for treatment or hard limits on treatment aggressiveness can improve access or costs, but not both. Insurance plus price-based incentives against risky treatment, however, can together improve patient welfare and reduce medical costs.

Keywords: In Vitro Fertilization, insurance mandates, healthcare access and cost, pricing risky behavior

JEL Codes: G22, I11, I13, I18, J13

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1 Introduction

Healthcare policymakers struggle with the conflicting goals of providing ready access to medical care while simultaneously containing costs. For example, in the U.K. a medical treatment may not be covered by national insurance if it fails to meet a cost-effectiveness criterion. U.S. insurance plans have focused on alternative cost-sharing arrangements as a means of influencing patient choice, but the scope of such arrangements is limited due to relatively low out-of-pocket maximum payments (Feldstein and Gruber, 1995). Optimal health insurance design suggests that a patient desiring an expensive, technologically advanced treatment should face higher co-payments (e.g., Chernew et al., 2000). In this spirit, recently introduced “value-based” insurance plans tie patient co-pays to the clinical value of treatment (Chernew et al., 2007). Spurred by the Affordable Care Act, value-based principles have been experimented with in primary care and pharmaceutical plans. However, such insurance policies are still uncommon and few empirical studies (e.g. Einav et al., 2016) evaluate the ability of treatment-dependent pricing to influence patient behavior and control costs.\(^1\)

In this paper, we study the impact of alternative policies on patients’ access to care, patients’ surplus, and healthcare costs in a context that embodies many of the features of more complicated medical treatment: the market for In Vitro Fertilization (IVF) in the U.S. Over the last 20 years, IVF use has increased four-fold to 160,000 treatment cycles annually, driven in part by delayed fertility decisions by women.\(^2\) Because individual cycles of IVF treatment often fail, potential IVF patients must solve a complex sequential decision problem under uncertainty about whether to initiate and/or continue therapy.\(^3\) Patients (in consultation with their physicians) must also decide on the type of treatment, based on their preferences and the cost of therapy. More aggressive treatment increases the probability of pregnancy, thus reducing the need for additional IVF cycles, but it also increases the risk of costly higher-order births. IVF patients now account for approximately 50% of all higher-order births, which are generally four (twins) to sixteen (triplets) times more expensive than a singleton birth. Consequently, IVF resembles other medical treatments, like those

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\(^1\)Baicker et al. (2013) simulate the impact of an alternative to Medicare in which all individuals are guaranteed basic benefits, but are provided the option to “top-up” by purchasing additional coverage for more expensive, less cost-effective treatments. Such a scheme may lead to more unequal healthcare spending but lower cost growth.

\(^2\)IVF currently accounts for 1% of U.S births. Treatment rates are even higher in some other countries; IVF accounted for over 3% of 2011 births in Israel, Belgium, Sweden, and Denmark. The aggregate treatment statistics reported in this paragraph for the U.S. are for fresh-embryo treatments during 2012, the most recent year for which U.S. data are available (Centers for Disease Control and Prevention (CDC), 2014). Statistics from European countries are from the European Society of Human Reproduction and Embryology’s (2014) ART Fact Sheet. Israel’s IVF birth share is reported by Simonstein et al. (2014).

\(^3\)Relatively young U.S. patients (under 35 years old) in 2012 achieved a birth after 40% of cycles, while patients just under 40 years old had success rates approximately half as large.
for heart disease or cancer, where dynamic decisions are made across a variety of treatment steps while health information is gradually revealed, and patients weigh the direct effects of alternative treatment options against potential side effects (Chan and Hamilton, 2006).4

High out-of-pocket costs for IVF (typically $10,000 - $15,000 per cycle of treatment) and the high rate of expensive multiple births have led policymakers to consider a variety of interventions in the hopes of achieving two goals: improving IVF access in the population and reducing treatment risks and costs. To increase access, ten U.S. states have mandated insurance coverage for IVF; these policies endow each potential patient with several covered treatment attempts for an out-of-pocket price of $2,000-$3,000. While mandates should lead to higher utilization rates, the policy also has the potential to contain costs. This might be the case if patients, aware that future insured attempts would also occur at a lower price, decide to engage in less aggressive treatment by taking fewer embryos. Transferring more embryos increases both the probability of pregnancy and the likelihood of a multiple birth. As the medical costs associated with birth are generally paid by insurers, treatment aggressiveness may be described as moral hazard.

Concern about moral hazard and the high rate of costly multiple births has led some European countries to limit the treatment options available to IVF patients in the form of an explicit cap on the number of embryos transferred during treatment. U.S. medical experts have recently advocated for embryo caps due to their perspective that a singleton birth is the best possible outcome of treatment.5 While this treatment restriction nearly eliminates costly high-order births, it may have the effect of reducing access to IVF. When a patient can transfer only a single embryo, her odds of conceiving a child are greatly reduced, and this could lead patients to forego IVF altogether or abandon treatment after unsuccessful initial attempts.

To evaluate the impact of these and other alternative policies, we specify a structural model of forward-looking, infertile patients’ decisions to initiate and or/continue IVF treatment using fresh non-donor eggs and embryos.6 Treatment choice dynamics for IVF patients reflect a number of

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4Medical treatment guidelines themselves traditionally have been static or open-loop. Murphy (2003) introduced the notion of “optimal dynamic treatment regimes” to construct adaptive decision rules, and this framework has been applied to physicians treating disease. Murphy’s approach builds on earlier work by Robins (1997) on dynamic treatment effects. Her approach, however, focuses on dose-response relationships and does not incorporate or estimate patient preferences. This inhibits the study of settings where patients exercise some discretion over treatment protocol, and limits the focus to objective outcomes (e.g. biological responses) rather than also allowing subjective ones (e.g. welfare). Abbring and Heckman (2007) describe this area of the statistics literature, and they contrast the literature’s assumptions with structural econometric approaches that, as in our paper, rely on dynamic choice models.

5The Practice Committee for the Society for Assisted Reproductive Technology (2012) summarizes a number of studies on single embryo transfer and concludes that IVF clinics should promote elective single embryo transfer.

6A large majority of IVF cycles use the patient’s own eggs (i.e. nondonor) and transfer embryos that were never frozen.
mechanisms. First, patients must consider both the current and future price of treatment because outcomes are uncertain. Due to high potential future costs, patients may choose aggressive current treatment that raises both the probability of pregnancy and the likelihood of a multiple birth. Second, patients may expect their medical condition to change over time. In the case of IVF, female fertility declines with age, particularly after age 35. Anticipation of future health declines affects current decisions regarding both the initiation choice and aggressiveness of treatment. As treatment choices are affected by intertemporal variation in prices, health, and information, we expect that possible regulatory changes could have subtle impacts throughout the decision process.

We estimate the model using a novel dataset of the treatment histories of women undergoing IVF at an infertility clinic (“the clinic”) between 2001 to 2009, as well as data on potential patients in the St. Louis, Missouri, market where the clinic is located. This setting provides a valuable opportunity to understand how prices, preferences, and health affect IVF treatment. The clinic serves patients from both Illinois, which mandates insurance coverage of IVF, and Missouri, which does not. Consequently, we are able to analyze the decisions of observationally equivalent patients facing vastly different prices (about $3,000 for covered patients versus $11,000 for those without insurance) undergoing the same procedure with the same physicians. Using highly detailed information on the fertility attributes of the patients and their treatment choices and outcomes, we estimate the various stochastic processes that determine success at each stage of an IVF treatment cycle. These processes, together with the specifications of patient preferences over children and the disutility from payments, yield a finite-horizon dynamic optimization problem that spans the reproductive years of (otherwise) clinically infertile women. The model delivers policy functions that specify: a) whether to initiate an IVF treatment, b) the treatment choices within an IVF cycle, and c) whether (and when) the patient re-attempts to conceive through IVF. We estimate the empirical model in three steps. The first step is the estimation of the treatment “technologies” determining outcomes during the four stages of a given IVF cycle. The second step recovers the structural parameters of our within-clinic patient decision model by maximizing the likelihood of the observed treatment choice histories. These parameters indicate that patients prefer singleton and twin births to the more dangerous triplet births, and the utility from additional children falls in the number of children.

As discussed below, insured patients may be concerned about exhausting their benefits, which raises future prices for IVF. This is in contrast to other insurance scenarios in which patients initially experience high out-of-pocket costs for treatment and then face low prices once their insurance deductible is reached. Aron-Dine et al. (2015) examine the dynamic implications of changes in out-of-pocket costs induced by exhaustion of deductibles. In a study of insurance’s role in risk protection and moral hazard, Kowalski (2015) accounts for the impact of deductibles, coinsurance, and stoplosses in consumers’ nonlinear budget sets.
the patient already has. These estimates are necessary to assess how patients would respond to policies designed to reduce treatment aggressiveness. The third step captures potential patients' decisions to ever initiate treatment.

We use the estimated model to conduct counterfactual experiments that investigate the impact of alternative policy proposals on individual patient actions, outcomes, and surplus. We first consider the widely-discussed policies of mandated insurance coverage and treatment restrictions in the form of embryo caps. Relative to a baseline case in which no women have insurance, introducing universal coverage for IVF results in more than a doubling of the share of infertile women who initiate treatment (24% vs. 58%). This increase in access is accompanied by an increase in consumer surplus from $2,700 to $6,600 per potential patient. While insurance reduces the opportunity cost of failed treatment, which in principle could affect embryo transfer rates, we find only a small reduction in treatment aggressiveness because our estimates imply that patients receive about the same utility from singleton and twin births, implying little reason to transfer fewer embryos. Therefore, while this policy succeeds at increasing access, it is of little help in terms of cost control. In an effort to contain costs, we next evaluate the policy of a “European-style” treatment restriction combined with universal insurance. The strictest policy is a hard limit of one embryo per patient, which pushes treatment initiation down to its no-insurance level, but with greatly reduced total costs and aggregate births. In terms of costs per birth, however, the embryo cap is actually more expensive than the no-insurance baseline due to low birth rates.

Given the cost growth induced by universal insurance, and the consumer surplus losses associated with treatment restrictions, we explore pricing schemes closer to those suggested by theoretical models of optimal insurance design. While current practice in IVF allows patients to increase the number of embryos at zero additional price, the full social cost of additional embryos is positive due to the increased medical costs of higher-order pregnancies. Consequently, we evaluate the introduction of a value-based plan in which insured patients face “top-up prices” when transferring more than one embryo. We select top-up prices that cover the (expected) increase in medical expense relative to single-embryo transfers to minimize this potential source of moral hazard. Under the top-up policy, patients reduce but do not eliminate multiple-embryo transfers, reflecting both a preference for twin births and the incentive to reduce lifetime treatment costs. The presence of insurance allows utilization (32%) to be greater than the no-insurance baseline, but with signifi-

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8Einav et al. (2016) consider a closely related policy of top-up prices for medical care beyond a basic level covered by insurers.
cantly lower costs per birth ($63,100 per delivery versus $69,400 under the baseline), due to patient payments against birth expenses and a reduction in multiple birth rates. In fact, total insurance payments are lower with actuarially fair top-up prices and therefore insurance companies might be content with insurance mandates that allow top-up price designs similar to those we analyze.

While insurance coverage for IVF in the U.S. is generally proposed as protection against the high costs of infertility treatment, Israel takes a different approach by insuring birth outcomes directly to encourage family formation. In particular, Israel allows unlimited IVF attempts until the patient has two or more children. Our final set of counterfactuals compares such outcome-based insurance designs with more traditional policies that provide a fixed number of treatments. We find that an outcome-focused policy has nearly identical patient benefits and costs as mandated universal insurance coverage found in U.S. states such as Illinois. The Israeli design also highlights the dynamic impacts of IVF policies. We show that age-related limits on the Israeli policy leads to welfare and choice differences related to patients anticipating future reductions in policy generosity.

The remainder of the paper proceeds as follows: Section 2 provides a preview of the four stages of an IVF treatment cycle, and describes state level policies governing insurance coverage of infertility treatment. Section 3 covers assumptions on model components, which are incorporated into our dynamic structural model of treatment choice developed in Section 4. In Section 5 we describe the data we obtained from the clinic, plus additional market-level data. Section 6 discusses the empirical specification of our model and Section 7 provides estimation details. Section 8 presents the parameter estimates and measures of model fit, and Section 9 contains the results from our counterfactual policy simulations. Conclusions follow.

2 IVF overview and our setting

2.1 IVF background

A couple is defined to be medically infertile if they are unable to conceive after attempting to do so for 12 months. Initial treatment for infertility often includes the use of the drug clomiphene to induce ovulation, or the use of hormone shots with or without intrauterine insemination. While such treatments are relatively low cost, they are less effective than more technologically advanced treatments, more likely to lead to higher order pregnancies, and can be especially poorly suited to older patients and those with male factor infertility. Due to these limitations, couples may choose

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9Greater IVF access can be achieved with smaller top-up prices, if desired.
to directly undergo IVF. Others may eventually turn to IVF after failing to conceive through these less advanced treatments.

Once a patient has decided to use IVF, the treatment cycle unfolds in stages. First, the woman takes drugs to stimulate egg production. The patient and doctor monitor the response to these drugs and may choose to cancel the cycle if the patient’s response is not favorable; if a cycle is cancelled, the patient may start IVF again in the future. If the cycle is not cancelled, the eggs are retrieved during a minor surgical procedure and then fertilized in the laboratory. The doctor may recommend the use of intracytoplasmic sperm injection (ICSI), in which a single sperm is injected into the egg. ICSI was initially used to address male-factor infertility problems, but has become more widely used. The patient then decides how many fertilized eggs (cleavage-stage embryos) to transfer to the womb; this choice may be constrained by the number of embryos that develop. At this point the patient faces an important tradeoff: the probability of a live birth increases with the number of embryos transferred, but so does the likelihood of a potentially costly and medically risky multiple birth. Lemos et al. (2013) calculate that the average medical cost of a singleton IVF pregnancy and initial child medical care is $26,922, while twin and triplet births entail costs of $115,238 and $434,668, respectively.\footnote{Lemos et al. (2013) obtained a sample from MarketScan of 437,924 deliveries covered by commercial insurance over the period 2005-2010 to derive their cost figures. Approximately 6,500 of these deliveries were IVF-related pregnancies. Reported costs were the sum of mother’s medical expenses from 27 weeks prior to delivery to 30 days after, plus infant medical expenses up to the first birthday. Average health care costs were $5,510 (singleton) to $27,469 (triplet) higher for IVF pregnancies compared to other births.} The high costs of multiple births are due largely to shorter gestation periods, which can lead to newborns being admitted to neonatal intensive care units. The medical costs calculated by Lemos et al. (2013) are typically not paid in full by the IVF patient herself, so they introduce the possibility of moral hazard to the embryo transfer decision.\footnote{Some medical conditions associated with early births can require life-long medical care, but we do not consider that care’s costs in this paper.}

If the IVF cycle does not result in a live birth, the patient then must decide whether (and when) to attempt another cycle of treatment. Anticipation of future opportunities to receive IVF is an important part of a patient’s decisions during the current IVF cycle. Because fertility declines with age, subsequent cycles are less likely to be successful, all else equal, and couples potentially incur substantial out-of-pocket cost if they try again. Patients whose treatments succeed may also try IVF again if they want to add more children to their families. More broadly, there exists some survey evidence (Hojgaard et al., 2007; Ryan et al., 2004) which suggests that patients may prefer a twin birth to a singleton. This preference could be motivated by a variety of factors, including declining fertility with age and the view that a twin birth is a cost-effective way to achieve a goal...
of multiple children.

2.2 Public policy and analysis of its impact

A key feature of the U.S. market for IVF is the presence of state-level mandates regarding whether and how insurers must offer coverage for infertility treatment, including IVF. During the period of our study, 2001-2009, seven states had mandates requiring some form of insurance coverage for IVF. Connecticut (after 2005), Illinois, Massachusetts, New Jersey, Rhode Island had the strongest mandates for IVF, requiring insurers to cover a certain number of IVF treatment cycles.\textsuperscript{12} Prior empirical research on insurance mandates has used a variety of approaches to examine issues related to IVF access, embryo transfer patterns, and birth outcomes. The distinguishing feature of the past research is that potential patients' activity and outcomes are examined in aggregate, either at the population or clinic level. Schmidt (2005, 2007), Bitler (2008), Bundorf et al. (2008), and Buckles (2013) examine the impact of insurance mandates on population-level fertility rates, multiple birth rates, and child health. Hamilton and McManus (2011), Jain et al. (2002), and Henne and Bundorf (2008) investigate the impact of mandates on the number of patients served, embryo-transfer patterns, and birth outcomes at IVF clinics. Bitler and Schmidt (2006, 2012) use survey data to examine similar issues. While patient-level decisions and characteristics play a central role in generating the aggregate activity studied in these papers, their empirical approaches do not allow a direct examination of choices, counterfactual experiments, or welfare effects.\textsuperscript{13}

An additional policy proposal, motivated by the goal of reducing multiple births and their medical costs, is a single-embryo cap for IVF. While single embryo transfer is uncommon in the United States (only 10\% of IVF cycles in 2009 involved a transfer of one embryo), it is widely practiced in Europe. For example, 69\% of IVF cycles in Sweden transfer a single embryo and in Belgium it is required. The prior literature on this policy has focused on the medical impact of single-embryo transfers, whether voluntary or by rule. For examples, see Ryan et al. (2007), Jungheim et al. (2010), Csokmay et al. (2011), or Velez et al. (2014). By contrast, our focus on individual utility-maximizing patients allows us to consider treatment initiation decisions and patient welfare in addition to the impact of an embryo cap on multiple birth rates and medical costs. Patient initiation and welfare are likely to be affected by a cap because additional (costly)

\textsuperscript{12}See Schmidt (2005, 2007). Maryland, Arkansas, Hawaii and Montana are also classified mandate-to-cover states where the mandate includes IVF. Texas has a mandate requiring insurers to offer plans that include IVF coverage. Nothing prevents insurers, however, from charging substantially higher prices for plans that include this coverage.

\textsuperscript{13}Some studies exist in the medical literature that use patient-level IVF data (e.g. Malizia, Hacker, and Penzias, 2009), but their focus and approach are naturally different from our own.
cycles are needed, in expectation, to achieve a pregnancy, and because some patients may prefer
twin outcomes to singletons births.

2.3 The clinic we study and its market

In order to put our study of a single IVF clinic in context, we assess how the clinic and market
we study compares to the full U.S. IVF market (Centers for Disease Control, 2014). In Table 1
we present some statistics on clinic characteristics during the sample period of 2001 to 2009. The
clinic we study was larger than the average U.S. clinic, with 370.2 cycles per year compared to the
U.S. average of 217.1 cycles. This may be due to the clinic’s position in a large research-oriented
hospital, which could both influence demand and facilitate the hiring of the clinic’s medical staff.
The median patient age in our sample is 34 years old, which is slightly below the national median.
The difference in patient age could be due to demographic patterns, or a response to insurance
coverage, which may encourage potential patients to try IVF more quickly following difficulty
conceiving a child naturally. Patient health, as measured by the fraction of patients with multiple
female infertility diagnoses and the fraction of cases with a male infertility diagnosis, are similar
between the clinic we study and the national averages. Patient treatment choices over ICSI and
embryos transferred reflect less aggressive treatment in the clinic we study relative to the U.S.
averages. These treatment patterns, along with a greater birthrate per cycle (33.5% at the clinic
vs. 29.9% nationally), may be influenced by the difference in median patient age, which affects
both treatment choices and outcomes.

Turning to the clinic’s market, we examine how some critical demographic features compare to
the U.S. population. In our empirical analysis, we assume that potential patients are drawn from
all zip codes with centroids within 75 miles of our clinic. The area includes the city of St. Louis, its
surrounding suburbs, and some rural towns outside of the metro area. This area captures almost
all of the patients who ever visit the clinic; a small number come from greater distances. Our model
accounts for age at first birth and wealth as measured through housing value. Fertility timing in
the St. Louis market is nationally representative: within the age range 22-44, the median maternal
age at first birth in 2001 was 31 in both the St. Louis metro area and nationally. We use zip code
median home value as a proxy for wealth. In the St. Louis MSA this value was $103,900 in the
year 2000, while nationally the value was slightly higher at $112,100. More specifically, 54.4% of
St. Louis-area women lived in zip codes with median home values above $100,000; nationally the
share was 56.7%. The market’s share of African American women ages 25-44 was 19.9% in 2000,
while the U.S. share was 13.3%.

Our study exploits the fact that the clinic draws patients from the greater St. Louis metro area, which includes both Missouri, which has no insurance mandate, and Illinois, which has a mandate. For patients in our study residing in Illinois and working for an employer covered by the mandate, insurance plans are required to pay for up to 4 IVF cycles if the woman has no children. This insurance coverage pays the majority of IVF costs, but about $3,000 in expenses remain for insured patients due to co-payments and deductibles. For patients paying out-of-pocket for IVF in our sample, the clinic charged about $11,000 per treatment cycle throughout the sample period; this figure includes all drugs and medical procedures that are part of a complete IVF cycle. The Illinois mandate exempts firms with fewer than 25 employees and organizations such as the Catholic Church that may object to IVF for religious reasons. These individuals pay the full price of IVF. Despite the absence of a mandate, some patients from Missouri have private insurance for IVF; in these cases the clinic has found that IVF coverage details are similar to those of Illinois patients. Some Missouri employers may choose to offer IVF coverage as a means to attract and retain employees. We calculate that potential patients from Illinois are three times more likely (30% versus 11%) to have IVF coverage than women from Missouri, but even in Illinois insurance penetration is fairly low.

The patient-level information on insurance status allows us to exploit two sources of price variation in this setting: cross-section variation is present through the locations of potential patients, while longitudinal variation arises as patients exhaust their insurance coverage over the course of multiple IVF cycles. We assume that St. Louis-area potential patients do not endogenously move or change employers in order to receive mandated insurance coverage under Illinois’s IVF insurance regulations.

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14If the patient has already had a birth through IVF, the number of remaining covered cycles is set to 2. This implies that an Illinois resident can have as few as three or as many as six covered cycles, depending on when or whether she has a successful cycle.

15The typical patient takes two IVF treatments, which would provide up to $16,000 in savings on out-of-pocket treatment expenses. Individuals who seek these savings, however, could experience substantial monetary or utility costs related to job search and switching, housing search and switching, and potentially suboptimal matches in the Illinois labor and housing markets.
3 Model preliminaries

3.1 Timing

We consider two timing concepts in the model below. First, there are decision *periods* when active patients choose whether to start or delay an IVF cycle. Second, in an IVF treatment cycle there are four treatment *stages* during which patients make one choice per stage. The time unit of the model is a 3-month period. We index the age of the patient (in 3-month periods) with \( a \) and calendar time periods (also quarterly) with \( t \), and we use \( j \) to index stages within a period during which an IVF cycle is started. At each age \( a \), within stage \( j \), the patient selects an action \( y_{j,a} \) from the set \( Y_j \). The set \( Y_j \) does not vary with \( a \) or \( t \). Note that there will be two indexes, \( a \) and \( t \), to keep track of time-varying objects in the model; the primary index is “\( a \)”.

Age is important because we specify a finite horizon model, and also because age itself enters various stage technologies.

We assume that potential patients’ decisions begin with an exogenous event which prompts them to consider having children. Women who are able to reproduce naturally (or with less technologically advanced infertility treatments) are immediately removed from the process we study in this paper. The remaining women have reproductive difficulties that can be solved by IVF only. These women, who constitute our “at risk” population, evaluate the expected benefit of beginning IVF relative to an outside option. The outside option, which we parameterize below, could include adoption, surrogacy methods of reproduction, or remaining childless. If the woman does not begin IVF at this critical moment, we assume she collects the value of the outside option and exits the model permanently. We assume that policy changes that affect the value of pursuing IVF do not change the value of this outside option.

Individual patients vary in the age at which they consider reproduction. We denote as \( a_0 \) the patient’s age (in quarters) when she considers IVF. The patient’s choice over IVF, if necessary, arrives four quarters after her exogenous decision to first attempt reproduction, i.e. at age \( a_{-4} \). This timeline is consistent with a simplified setting in which all women believe themselves to be fertile (but are unaware of their true infertility status) until their first pregnancy attempt at age \( a_{-4} \). A woman who is fertile conceives after 3 months of attempts and gives birth to her first baby 9 months later. An infertile woman experiences a year of unsuccessful pregnancy attempts until, at age \( a_0 \), she considers whether to pursue IVF and therefore become a patient at the clinic.

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16 Due to data limitations, we do not study the potential patient’s decisions of how quickly to turn to IVF, and how this is affected by insurance coverage. We assume, instead, that all couples with fertility problems exhaust the same set of alternatives before arriving at the IVF decision.
at that point she opts to pursue IVF treatment, the patient may continue to make decisions until a terminal age, $a_{\text{max}}$. At this age the IVF clinic will no longer treat the patient and her birth probability (via IVF or naturally) is zero.\footnote{We assume this age upper bound for tractability. The clinic does not have a preset age limitation and, instead, evaluates each patient on a case-by-case basis.} This allows a maximum of $4 \times (a_{\text{max}} - a_0 + 1)$ periods for a patient whose reproductive decisions start at age $a_0$. In our data we observe patients with $a_0$ between their late twenties and early forties. We define $a_{\text{min}}$ to be the youngest patient age considered in our model. We set $a_{\text{min}}$ to be the first quarter of age 28, and $a_{\text{max}}$ is the final quarter of age 44. Once a patient’s total number of children reaches 3 (or more), she automatically stops making decisions within the model.

In addition to the age index, a time index ($t$) is useful for describing the data sample and econometric procedure. This index is also necessary to describe the prevailing embryo-transfer guidelines offered by the American Society for Reproductive Medicine (ASRM); these guidelines changed once during our sample period, in 2004. Let $t_{i,0}$ represent the period during which we first observe patient $i$. We see a patient for the last time in $T_i$, which might be equal to $a_{\text{max}}$ or $T$, the end of the sample period. We assume that all treatment stages that follow from a treatment starting in period $t$ also occur in period $t$.

### 3.2 State variables and initial information

A patient who is considering treatment is aware of several personal characteristics that affect treatment effectiveness and utility. There are two types of state variables in the model. First, there are the state variables collected in the vector $Z$, which remain constant within periods but may transition between them. Second, there are state variables which are revealed during the stages of a treatment cycle, but do not carry over between periods. These variables include information about treatment progress and additional taste shocks that affect the value of each treatment option at a decision stage. We discuss these variables in detail below, when we introduce our model of IVF treatment behavior.

We divide the state vector $Z$ into two parts. We track a patient’s age ($a$), a measure of her wealth ($z_w$), number of prior children ($k$), record of previous payments for IVF ($z_p$), insurance status ($i$), and race ($z_r$) in the state vector $Z^D$.\footnote{Bitler and Schmidt (2006) document differences in infertility diagnoses and IVF usage across racial, ethnic, and socioeconomic groups. Due to data limitations we consider a simple binary specification for $z_r$, which records whether a woman is African American.} Some of these state variables are time-invariant and others vary in how they evolve between periods. Age increases exogenously by three months every period.
Race is a permanent patient characteristic, and we assume wealth is constant also. We construct \( z_w \) with zip code-level data on housing values. We focus on patients with zero prior children (\( \tilde{k} = 0 \)) at the treatment initiation decision, and then \( \tilde{k} \) evolves endogenously as a controlled Markov process which depends on treatment outcomes.\(^{19}\) Likewise, the patient’s record of prior IVF payments (\( z_p \)) and remaining insured cycles evolve endogenously according to the patient’s decisions within the model. We initialize the number of insured cycles (\( t \)) to four (the Illinois mandate value) for all patients who ever use insurance, and this number falls by one whenever an insured patient advances to the second stage of treatment, when eggs are removed during surgery.\(^{20}\) The forward-looking patient is aware that IVF’s price increases substantially after her fourth insured cycle.

The second part of \( Z \) includes the patient’s biological characteristics, \( Z^B \). We assume that the patient learns her own \( Z^B \) if she initiates treatment. The characteristics in \( Z^B \) include: the women’s antral follicle count (AFC score, \( z_{afc} \)), an indicator of her egg-producing ability; whether she has one or more specific infertility diagnoses (\( z_{ff} \)), e.g. endometriosis; and whether her partner has male-factor infertility (\( z_{mf} \)). At the treatment initiation decision, the patient considers the possible values of \( Z^B \) she may have using the population frequency of these characteristics conditional on her initiating age, \( f_{Z^B}(Z^B|a_0) \). We assume that the distribution of \( Z^B \) conditional on \( a_0 \) is independent of race.

Our assumptions on \( Z \) include a few simplifications that we impose to maintain tractability. First, we do not allow patients to receive a detailed fertility screening before deciding to initiate treatment, which could be used to reveal \( Z^B \). This is a simplification that abstracts away from real-world opportunities for potential patients to learn about \( Z^B \) during less sophisticated infertility treatments or stand-alone screenings. We make this simplification in order to reduce the dimensions of potential patient heterogeneity prior to treatment, and because of data scarcity about this heterogeneity among the population at large. Second, we assume that patients (and their doctors) use no biological data other than \( Z^B \) in choosing a treatment path for patients. We assume that the patient’s observed biological state variables \( Z^B \) and age fully capture her relevant fertility characteristics; there are no unobserved state variables that directly affect treatment outcomes, and previous cycles’ choices and outcomes also have no direct impact on the current cycle’s outcomes. As implied by this assumption, we do not model additional unobserved health characteristics which

\(^{19}\)All patients start with \( \tilde{k} = 0 \), and \( \tilde{k} \) evolves stochastically in each following period. The evolution of \( \tilde{k} \) depends on whether a cycle is started and what choices are made within that cycle. If no cycle is started or an ongoing cycle is cancelled, then \( k_{a+1} = k_a \). \( \tilde{k} \) remains constant as well if a cycle is unsuccessful. If a cycle at age \( a \) reaches the embryo transfer stage and at least one child is born as a result of that cycle (\( k_a > 1 \)) then \( k_{a+4} = k_{a+1} + k_a \).

\(^{20}\)We abstract away from some of the complicated details of the Illinois insurance code, discussed above.
the patient and her doctor learn about through IVF treatment itself.

Once the value of $Z^B$ is realized we consolidate notation and refer to the state vector $Z = [Z^D, Z^B]$. In addition to acting as a state variable which influences treatment outcomes, patient age also functions as a time index, so we add an ‘a’ subscript to $Z$ where appropriate. During an arbitrary age $Z_a = [Z_a^D, Z_a^B]$, and at treatment initiation the state variables have the value $Z_{a0}$. We assume that the doctor knows how the variables in $Z_a$ affect treatment outcome probabilities. Each patient receives this information from her doctor and also knows her own preferences over treatment outcomes.

3.3 Patients’ preferences

Patients have preferences over birth outcomes ($k$), and these preferences can depend on the patient’s existing number of children ($\tilde{k}$) at the start of an IVF cycle and other personal characteristics. Possible values of $k$ are in $\{0, 1, 2, 3\}$, and $\tilde{k}$ takes values in $\{0, 1, 2\}$. (These values for $\tilde{k}$ cover 98% of the patient population at the clinic.) We allow patients to have permanent unobservable heterogeneity, indexed by $\tau$. Let $U(k|\tilde{k}, \tau)$ represent the lump-sum utility payoff from a treatment cycle that produces $k$ children in that individual cycle, conditional on $\tilde{k}$ prior children and $\tau$. As a normalization, we assume that treatment outcomes with $k = 0$ always result in $U(k|\tilde{k}, \tau) = 0$ for all patients. Beyond this normalization, we place no restrictions (e.g. concavity) on how $U(k|\tilde{k}, \tau)$ changes with $k$; the restrictions, if present, could have the effect of imposing risk preferences over values of $k$. While we treat $U(k|\tilde{k}, \tau)$ as a lump-sum benefit, we interpret it as the expected utility from having $k$ additional children, which may include health risks from high-order births.

The utility from children in $U(k|\tilde{k}, \tau)$ is policy-invariant. Other aspects of the model, introduced below, may change due to policies we consider, and these can impact the forward-looking patient’s continuation value from different birth outcomes.

To maintain tractability, we combine $U(k|\tilde{k}, \tau)$ additively with other payoff-related terms in an indirect intertemporal expected utility function. Patients undergoing treatment experience disutility, scaled by $\alpha$, from paying positive prices. When a patient pays $p$ within treatment, she has the immediate utility loss of $\alpha p$. We allow the value of $\alpha$ to depend on a patient’s wealth, so we write $\alpha(z_w)$. This specification for the effect of $p$ on utility is consistent with a model where consumption of other goods enters additively into the utility, and there is a static budget constraint that allocates income between consumption of other goods and IVF expenses.\(^{21}\) Likewise, a patient’s

\(^{21}\)We have access only to a time invariant, proxy measure of wealth, $z_w$. Therefore, we chose not to include an
price depends on her insurance status, so we write \( p(\iota) \). An additional potential source of disutility is in a patient’s choice to deviate from the American Society for Reproductive Medicine (ASRM) guidelines for embryo transfers. During our sample period the ASRM generally recommended against four-embryo transfers for all patients, and single-embryo transfers for older patients.\(^{22}\) We assume that a patient’s utility falls by \( \eta_0 \) if she makes a choice outside of the guidelines, with no penalty otherwise. We specify the function \( \eta(x, Z_a) \) to combine the penalty value and the conditions under which it is applied, with \( x \) as the number of embryos and \( Z_a \) capturing the contemporary ASRM guidelines and their relationship to the patient’s current age. We assume that ASRM guidelines changes come as a surprise to decision-makers, i.e. patients always believe the current policy environment is permanent. When the ASRM guidelines change, patients immediately reoptimize their treatment plans for the current rules, and then resume the belief that the guidelines will never change again.

The remaining parts of patients’ preferences include the value from starting versus delaying an individual treatment and a terminal value. Relative to a baseline flow utility from delay that is normalized to zero, we assume that patients receive the flow benefit (or cost) of \( u_a \) during any period in which she begins IVF treatment. \( u_a \) can include any physical or psychological stress from undergoing IVF. Patients’ terminal payoffs are captured by the parameter vector \( u_T(z_p) \), which depends on her prior payments. The patient receives \( u_T \) at age \( a^\text{max} + 1 \) regardless of whether she remains active in the model up until \( a^\text{max} \) or if her decision process ends due to \( k + \tilde{k} \geq 3 \) at some earlier \( a \).

At each treatment node, the patient’s benefit from the available options includes an additional taste shock, \( \varepsilon \), which represents heterogeneity in patient’s circumstances and preferences. Following Rust (1987), for computational ease, we assume that \( \varepsilon \) is distributed i.i.d. type 1 extreme value across patients, time periods, treatment stages, and alternatives within each stage. We offset Euler’s constant so that \( E [\varepsilon] = 0 \).

Finally, we assume that patients discount future decision periods by the factor \( \beta \). We assume that all discounting occurs across periods, and not across treatment stages. Treatment options and

\(^{22}\)Prior to the September 2004 rule change, the ASRM recommended against single-embryo transfers for all patients, as well as four-embryo transfers for patients under age 35 and undergoing their first cycle. After the guidelines changed in September 2004, the recommendation against four-embryo transfers was extended to all patients under age 38 regardless of cycle number, plus patients between ages 38 and 40 who were taking their first cycle. The guideline revision also removed the recommendation against single-embryo transfers for patients under age 35 on their first cycle.
outcomes that occur \( t \) periods into the future are discounted by \( \beta^t \). We do not estimate \( \beta \) in this paper, so we set its value equal to \( \beta = 0.97^{23} \).

### 3.4 Technology and prices

During each IVF stage, a patient makes a choice about treatment; possibly pays a price out-of-pocket; and anticipates the outcome of a random process, the results of which are revealed before the next choice occurs. We now review notation for these processes, i.e. the treatment technologies, and the prices patients pay. We assume that the technologies did not change during the sample period. This accords with the actual practice of IVF during the early 2000s.

For a patient who has committed to the first stage of IVF treatment, her personal characteristics and drug regimen will yield a Peak E2 score (\( e \)) to be revealed at the start of stage 2. The score is a signal of the patient’s success in generating eggs. During the first stage, however, the patient knows only the distribution of possible \( e \) values rather than the signal’s realization. Let \( f_e(e|Z_a) \) represent the probability that a patient with characteristics \( Z_a \) receives a score with value \( e \), which takes positive integer values. Moving to the second stage, we denote as \( f_r(r|e, Z_a) \) the probability of successfully retrieving \( r \) eggs for a patient with Peak E2 score \( e \) and personal characteristics \( Z_a \). A patient with a greater value of \( r \) is more likely to generate a large number of embryos in the next stage. Once the patient reaches the third IVF stage, she observes her value of \( r \) and considers the distribution over possible numbers of embryos, denoted \( X \), available for transfer, which will be realized following her decision on fertilization method (\( m \)). We write this distribution as \( f_X(X|r,m,Z_a) \), and note that it may be shifted by \( r, m \), and the patient’s state variables. Finally, in stage four the patient considers the number of children (\( k \)) that will be born, which is affected by the number of embryos transferred (\( x \) out of the realized \( X \)) and the patient’s \( Z \) values. The distribution over realizations of \( k \) is \( f_k(k|x,Z_a) \).

We specify the prices that patients may pay at three treatment stages. The price of action \( y \) in stage \( j \) is \( p_{y,j}(s) \). In the first treatment stage, uninsured patients pay \( p_{s,1} = $3,000 \) if they choose the action ‘start’ (\( s \)), while insured patients pay \( p_{s,1} = $1,000 \). The positive price for insured patients is due to deductibles, co-payments, and co-insurance charges. Patients who continue (\( c \)) treatment in stage 2 pay \( p_{c,2} = $6,000 \) if uninsured, and \( p_{c,2} = $2,000 \) if insured. The third-stage option to use ICSI (\( m_2 \)) carries a price of \( p_{m_2,3} = $2,000 \) for uninsured patients, and a price of zero.

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\(^{23}\)In principle, the nonstationary nature of our model could allow for identification \( \beta \). In practice, however, this parameter is often very difficult to estimate so we chose to fix it at a conventional value.
for insured patients. The final stage, embryo transfer, has zero price for all patients regardless of the number of embryos transferred.

4 Decision model and value functions

We now describe how patient preferences and IVF technology come together into a multi-stage decision process. Conditional on starting IVF treatment, a patient makes a series of choices regarding the aggressiveness of her treatment and whether the treatment continues at all. The patient’s current incentives are affected by her future treatment opportunities and prices. Along the way, the patient uses information that is known at the start of treatment (e.g. age, current number of children, basic fertility diagnoses) and information that is collected incrementally as treatment progresses (e.g. the numbers of eggs retrieved and embryos available for transfer). See Figure 1 for an illustration of the IVF treatment stages described below. The figure contains some notation on utility payoffs that is introduced later.

Some notational conventions are common across stages. We write \( W_{y,j}(Z_a, \varepsilon_{y,j,a}) \) as the value of choice \( y \) during stage \( j \) of a treatment cycle. This function accounts for: expectations over future treatment outcomes, taste shocks in current and future stages, and optimal behavior in future stages. Patients’ values of \( W_{y,j}(Z_a, \varepsilon_{y,j,a}) \) depend on \( \tau \), but we suppress this term for notational simplicity. Let \( \overline{W}_{y,j} \) be the systematic component of \( W_{y,j}(Z_a, \varepsilon_{y,j,a}) \), i.e. \( W_{y,j} \) net of the additive preference shock \( \varepsilon_{y,j,a} \). We then have

\[
W_{y,j}(Z_a, \varepsilon_{y,j,a}) = \overline{W}_{y,j}(Z_a) + \varepsilon_{y,j,a}. \tag{1}
\]

The patient observes the realization of the vector \( \varepsilon_{j,a} \) before making her choice during stage \( j \). The patient’s value at the start of stage \( j \) is

\[
W_j(Z_a, \varepsilon_{j,a}) = \max_{y \in Y_j}\{W_{j,y}(Z_a, \varepsilon_{y,j,a})\} = \max_{y \in Y_j}\{\overline{W}_{y,j}(Z_a) + \varepsilon_{y,j,a}\}. \tag{2}
\]

\( E[W_j(Z_a, \varepsilon_{j,a})] \) represents the expected value from an optimal decision within treatment stage \( j \), before observing the realization of \( \varepsilon_{j,a} \). Due to the extreme value assumption for \( \varepsilon \), we can write
\[
E[W_j(Z_a, \varepsilon_{j,a})] \text{ with the inclusive value expression:}
\]
\[
E[W_j(Z_a, \varepsilon_{j,a})] = \log \left( \sum_{y \in Y_j} \exp[W_{y,j}(Z_a)] \right).
\]

We begin by focusing on the treatment stages that occur within IVF, after the patient has learned her value of \( Z^B \). Later in this section we return to the initiation decision.

### 4.1 Stage 1: Start treatment vs. delay

In all periods after the initiation decision, patients who began IVF previously will return to stage 1 and choose between the actions start \((s)\) and delay \((d)\). If the patient starts treatment, she pays the price \( p_{s,1}(\iota) \) out-of-pocket and begins a regimen of pharmaceuticals to promote egg production.

The value from starting a treatment cycle at age \( a \) is \( W_{s,1}(Z_a, \varepsilon_{s,1,a}) \), and it includes the expected value from continuing to the second stage of treatment \( E[W_2(Z_a, \varepsilon_{2,a})] \); the utility normalization relative to delay, \( u_s \); the price of starting a treatment cycle, \( p_{s,1}(\iota) \); and a taste shock, \( \varepsilon_{s,1,a} \). The value of the second stage depends on the realization of \( e \) (the Peak E2 score), but this is not known during stage 1. The value from starting a treatment cycle at age \( a \) is then

\[
W_{s,1}(Z_a, \varepsilon_{s,1,a}) = W_{s,1}(Z_a) + \varepsilon_{s,1,a} + u_s - \alpha(z_w)p_{s,1}(\iota) + \varepsilon_{s,1,a} + \sum_e E[W_2(e, Z_a, \varepsilon_{2,a})] f_e(e|Z_a).
\]

The value of delaying the IVF decision until the start of the next period is:

\[
W_{d,1}(Z_a, \varepsilon_{d,1,a}) = W_{d,1}(Z_a) + \varepsilon_{d,1,a} + \beta E[W_1(Z_{a+1}, \varepsilon_{1,a+1})] + \varepsilon_{d,1,a}.
\]

Changes in \( Z \) across periods, in this case, are due to the patient becoming older, which affects her fertility characteristics and the probability of a favorable outcome at any treatment stage. The discounted expected value \( \beta E[W_1(Z_{a+1}, \varepsilon_{1,a+1})] \) accounts for the expectation of \( \varepsilon \), the payoffs in \( W_1 \) associated with starting or delaying IVF at age \( a + 1 \), and patient’s option to choose the optimal action. If the patient is already at age \( a_{\max} \), however, she receives the terminal value \( W_T(Z_{a_{\max}}) = u_T(z_p) \) at the start of the next period and exits the model. This type of exit is also possible in stages 2 and 4, described below, but we do not list it explicitly.
4.2 Stage 2: Continue vs. cancel

The patient makes her next significant choice after the value of $e$ is realized. A larger value of $e$ is generally associated with a larger number of eggs ($r$) that are ready for retrieval from the patient’s ovaries. During the second treatment stage, she considers $e$ and her personal characteristics ($Z_a$) while deciding whether to continue ($c$) or cancel ($nc$) treatment, thus $Y_2 = \{nc, c\}$. If the patient cancels treatment, she pays no additional treatment fees, and she is able to consider starting treatment again in the future. If the patient continues treatment, she pays the additional fee $p_{c,2}(t)$ and undergoes a surgical process in which eggs are retrieved.

If the patient decides to stop treatment, she receives the value

$$W_{nc,2}(e, Z_a, \varepsilon_{nc,2,a}) = \bar{W}_{nc,2}(Z_a) + \varepsilon_{nc,2,a}$$

(6)

$$= 0 + \beta E[W_1(Z_{a+1}, \varepsilon_{1,a+1})] + \varepsilon_{nc,2,a}.$$ 

The value of continuing treatment includes an expectation taken over values of $r$ conditional on the realized signal $e$ and other patient characteristics:

$$W_{c,2}(e, Z_a, \varepsilon_{c,2,a}) = \bar{W}_{c,2}(e, Z_a) + \varepsilon_{c,2,a}$$

(7)

$$= -\alpha(z_w)p_c(t) + \varepsilon_{c,2,a} + \sum_r E[W_3(r, Z_a, \varepsilon_{3,a})] f_r(r|e, Z_a).$$

The full value of the second stage is the maximum of these two options.

4.3 Stage 3: Fertilization

If treatment is not cancelled, the patient’s eggs are retrieved and she observes the realized value of $r$. The patient’s next choice is how to fertilize the eggs. The fertilization method is represented by the variable $m$, and the patient’s options are: natural fertilization ($m_1$) or with ICSI ($m_2$). Thus $Y_3 = \{m_1, m_2\}$. The patient’s characteristics ($Z_a$), her number of eggs ($r$), and her fertilization choice ($m$) determine the number of viable embryos generated for the patient. Couples with male factor infertility ($z_{mf} = 1$) are likely to receive the greatest benefits from fertilizing via ICSI ($m = m_2$).

When $m = m_2$, the patient pays the additional price $p_{m,3}(t)$.

Let $X$ represent a possible realization for the number of embryos. Possible values of $X$ are in $\{0, 1, 2, 3, 4+\}$. We cap the maximum value of $X$ at 4 because this is the greatest number of embryos that we see transferred to patients during the final treatment stage. When making her choice over
fertilization method, the patient considers the probability of receiving $X$ embryos, $f_X(X|\tau, m, Z_a)$. We write the patient’s choice-specific value from a third-stage action:

$$W_{m,3}(r, Z_a, \varepsilon_{m,3,a}) = \overline{W}_{m,3}(r, Z_a) + \varepsilon_{m,3,a} \quad (8)$$

$$= -\alpha(z_m)p_m(r|Z_a) + \varepsilon_{m,3,a} + \sum_X E[W_4(X, Z_a)] f_X(X|\tau, m, Z_a).$$

The patient selects the action, $m$, with the greater of two $W_{m,3}(r, Z_a, \varepsilon_{m,3,a})$ values.

### 4.4 Stage 4: Embryo transfer

At the start of the fourth and final treatment stage, the patient learns her number of viable embryos, $X$. The patient chooses $x$, the number of embryos to transfer during the final treatment stage, subject to $x \leq X$. We assume that the patient selects $x = 0$ only if $X = 0$. A patient’s treatment outcome is influenced by her number of embryos ($x$) and her personal characteristics ($Z$). As a result of treatment, $k$ children are born with probability $f_k(k|x, Z_a)$. Under current policy, there is no price for this treatment stage. If treatment fails she moves to the start of the next period, but if treatment is successful she waits for three additional periods (i.e. 9 months) before making her next reproductive decision.

When the patient elects to transfer $x$ embryos, she receives an expected benefit of

$$W_{x,4}(X, Z_a, \varepsilon_{x,4,a}) = \overline{W}_{x,4}(X, Z_a) + \varepsilon_{x,4,a} \quad (9)$$

$$= \eta(x, Z_a) + \varepsilon_{x,4,a} + f_k(0|x, Z_a)\beta E[W_1(Z_{a+1}, \varepsilon_{1,a+1})]$$

$$+ \sum_{k>0} f_k(k|x, Z_a) \left\{ U(k|\bar{k}_a, \tau) + \beta^4 E[W_1(Z_{a+4}, \varepsilon_{1,a+4})] \right\}.$$

This expression includes the possibilities of failed treatment ($k = 0$) and successful treatment ($k > 0$). The future value of a patient’s decision, $E[W_1(.)]$, depends on the realization of the current treatment and the prices and policies that constrain the patient in future periods. If the treatment is successful, $Z_a$ evolves to a value $Z_{a+4}$ which reflects that the patient is one full year older and has $k$ additional children. Moreover, this future value is discounted at $\beta^4$. If treatment fails, then the next decision’s value is discounted by $\beta$, and $Z_{a+1}$ reflects that the patient is just three months older. The value function captures the patient’s benefit from building a family of a certain size during her fertile years, so statements about a patient’s desire to avoid the risk of lifetime childlessness would be made in reference to $W$ rather than $U(k|\bar{k}, \tau)$. 

20
4.5 Initiation decision

Now consider the decision of a potential patient at age $a_0$ who is deciding whether to start IVF for the very first time. This is somewhat different from the decision to begin a new cycle by an already-active patient. We make the simplifying assumption that this potential patient does not yet know her values of $Z^B$, but she knows the population distribution of $Z^B$ values conditional on age, $f_{Z^B}(Z^B_{a_0}|a_0)$. The potential patient’s expected value from starting treatment is:

$$W(Z^D_{a_0}) = E[W_{s,1}(Z_{a_0})|Z^D_{a_0}] = \sum_{Z^B_{a_0}} W_{s,1}(Z^D_{a_0}, Z^B_{a_0}) f_{Z^B}(Z^B_{a_0}|a_0),$$

where we make the distinction between the state variables known prior to treatment ($Z^D_{a_0}$) and those learned after treatment begins. The potential patient compares $W(Z^D_{a_0})$ to the utility from foregoing treatment, which we specify as $W^{OUT} (z_r) = \mu(z_r) + \nu$. The parameter $\mu$ captures the mean value of the outside option for potential patients of different races, and it is common across potential patients of a given race. There is evidence that African-American women are less inclined to pursue infertility treatment, and in our model this would be reflected in a higher value of $\mu$. $\nu$ is specific to each potential patient and captures heterogeneity in the value of permanently foregoing IVF treatment; it explains why potential patients with the same $Z^D_{a_0}$ and (unobserved) $\tau$ make different choices with respect to ever pursuing IVF.\(^{24}\) One possible interpretation of $\nu$ is that of a sunk utility cost that must be paid to pursue IVF. Some infertile women with strong objections to IVF, e.g. because of religious beliefs, may refuse treatment even if it is free and has no chance of failure. $\tau$ and $\nu$ play fundamentally different roles in the model. $\tau$ characterizes permanent differences in utility from children. Potential patients know both their $\nu$ and $\tau$ before embarking in IVF treatment. $\nu$ captures idiosyncratic preferences for taking the outside option relative to pursuing IVF but plays no further role once the potential patient becomes a patient.\(^{25}\)

Under these assumptions, the potential patient enters the clinic to initiate her first IVF cycle if the expected value of pursuing IVF is greater than the value of foregoing treatment, and she exits the model otherwise. We let the indicator $I$ equal one whenever a potential patient initiates IVF.

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\(^{24}\)Note that there is no $\varepsilon_{1,s}$ for this very first cycle.

\(^{25}\)In a more general model, observationally similar patients, even with same $\tau$ and facing same $\varepsilon$, could make different decisions, perhaps with those with high values of $\nu$ being more reluctant to use IVF multiple times than those with low values of $\nu$. For computational tractability, though, we work with a simpler model in which once a woman decides to use IVF, heterogeneity in $\nu$ is no longer relevant for her decision-making within the clinic.
treatment, and equal zero otherwise. Then

\[ I = 1 \Leftrightarrow W(Z_{a_0}^{I}) \geq \mu(z_r) + \nu. \]

To make the decision problem more explicit in some of the analysis below, we sometimes add the policy index \( g \) to our notation for the value of starting a patient’s first cycle, i.e. \( W_{s,1}(Z_{a_0}, g) \). We let \( g = g_E \) represent the empirical baseline that we observe during the sample period. The index \( g \) captures elements such as pricing, insurance, regulations, etc. Under alternative environments, the value of \( W_{s,1} \) (and all other \( W_{y,j} \) that follow) changes and therefore initiation decisions are affected.

5 Data

5.1 Clinic data

Our primary data cover individual patient histories at the clinic during 2001-09. We observe all treatment cycles conducted during this period for patients who underwent their first-ever IVF cycle between 2001 and 2007, plus we observe cycles during 2001-09 for some patients who first received IVF before 2001. While the data allow us to describe many patients’ IVF histories from the start of their treatments, we do not observe whether a patient returns to the clinic after 2009 or visits a different clinic after her final visit at the clinic. We handle this potential right-censoring by assuming that patients continue to make choices as described by our model, with no changes to the policy environment, prices, or technology.

The main data sample contains treatment histories for 587 patients who use only fresh embryos (i.e. not frozen), received their first-ever IVF cycle at the clinic between 2001 and 2007, and have complete data on their personal characteristics and treatment details.\(^{26}\) We supplement these observations with data from an additional 519 patients for whom we have data on all state variables and most treatment choices. We refer to the expanded data as the “first-stage sample.” The treatment histories contain information on 1,027 initiated cycles in the main sample and 2,176 in the full first-stage sample. Beyond the initiation decision and its Peak E2 score realization, the main sample contains information on an additional 2,785 choices and stochastic health state outcomes from stages 2-4 of IVF cycles. In the full first-stage sample we have complete data on

\(^{26}\)In practice, patients may choose to freeze excess embryos for potential later use, but we do not examine that decision. Frozen-embryo cycles account for only 12% of the clinic’s treatments during the sample period.
4,779 stage 2-4 choices and health outcomes.

In Table 2 we display some basic characteristics of the patients, their treatment choices, and their outcomes; we separately report statistics for the main sample of 587 patients and the 1106 patients in the full first-stage sample. The average patient in the main sample is 34 years old at the time of her first cycle in the clinic, and over half of all patients have insurance. Most insured patients are from Illinois but not all; likewise most Illinois patients are insured but not all of them. Most patients’ homes are in a zip code with a median house price above $100,000, which we use as a proxy for patient wealth ($z_w$). We track race as a binary variable which indicates whether the patient is African American ($z_r = 1$) or not ($z_r = 0$); 95% of patients have $z_r = 0$. The patients in the main sample have no children when they initiated treatment, but some patients in the first-stage sample have prior children. The biological variables ($Z^B$) exhibit some minor differences between the main and first-stage samples, with the former set of patients displaying slightly worse fertility characteristics.

At the bottom of Table 2 we display patient-level statistics on treatment choices and outcomes. Patients in the main sample average 1.75 treatments during the sample period, and about half experience at least one birth during their full treatment history. In Table 3 we report summary statistics on choices and outcomes within treatment stages. Most patients at stage 2 choose to continue treatment, with only a 14% cancellation rate. Most patients (60%) fertilize their eggs with ICSI; this rate is closer to 90% when male-factor infertility is present.27 Finally, patients take 2.3 embryos on average during a treatment. The embryo transfer choices are most often made with a choice set of 4+ embryos, due to over 6 embryos being generated during an average cycle. At the bottom of Table 3 we report treatment-level outcomes. To obtain the main sample’s average of 0.51 children born per cycle, we include all stage 4 decisions with $x > 0$ and birth outcomes in \{0, 1, 2, 3\}. A singleton birth occurs in 27% of cycles, and twins occur in an additional 12%. While we observe no triplet births in the main sample, they occur at a rate of about 1% in the larger first-stage sample; this allows us to account for triplet risk when estimating the structural model.28

Some correlations among patient characteristics and treatment sequences suggest the role of dynamics and the importance of the state variables in patients’ decision-making. Almost 60% of patients whose first cycle was unsuccessful returned for one or more additional cycles, while 16% of

\[27\] While the options “full ICSI” and “partial ICSI” are separated in the data, we group them together in our model.

\[28\] In 2009, 1.6% of all U.S IVF births from fresh nondonor cycles were triplets or more. Conditional on 3 or more embryos transferred, the triplet rate was 3.6% (Centers for Disease Control, 2014).
patients with a first-cycle singleton and zero patients with first-cycle twins returned for additional treatment. Patients who receive Peak E2 scores in the lowest quartile chose to cancel treatment in 40% of all cases, while patients with scores in the $25^{th} - 75^{th}$ percentile cancel only 4% of cycles. Patients who are 35 or older take an average of 2.6 embryos in their first cycle, while younger patients take 2 embryos on average. Uninsured patients take more embryos (2.4) during their first cycle than insured patients (2.2), but this difference, which is statistically significant at the first cycle, shrinks in the second and third cycle as insurance coverage is drawn down.

5.2 Market data

We use several pieces of market data to describe the set of potential patients for our clinic. These data are used in a separate estimation step to estimate a model of treatment initiation. We assume that potential patients are drawn from all zip codes with centroids within 75 miles of our clinic. The area includes the city of St. Louis, its surrounding suburbs, and some rural towns outside of the metro area. This area captures almost all of the patients who ever visit the clinic; a small number come from greater distances.

We first describe the various data sources for the market data, and then we describe how they are assembled into an estimate of the “at risk” population. We use the Centers for Disease Control and Prevention’s (CDC) Vital Statistics database to construct the market’s distribution of maternal age at first birth. This distribution, along with estimates of infertility rates by age from Dunson et al. (2004), allows us to construct an age distribution for women who may consider IVF. We supplement the Dunson et al. estimates with data from the National Survey of Family Growth (NSFG) to estimate the difference in infertility rates by race. For zip code level information on the population share with private IVF insurance, we use data from the 2012 American Community Survey (ACS) and combine it with other sources of information, which we describe in the appendix. We collect zip code level data on race and the median home values from the 2000 Decennial Population Census. The home value data allows us to provide an estimate for the distribution of patients’ wealth. We combine the various zip code level data to construct an estimate of the joint distribution of wealth IVF insurance coverage and our measure of wealth. Finally, we use data from the CDC on the number of cycles conducted at each infertility clinic in the market to assess how many in the pool of potential patients would rely on the clinic we study (rather than a different clinic), if they decided to pursue IVF.

Next, we describe how we construct the pool of potential patients. Assuming stationarity and
stable cohort sizes, at any given point in time (quarter) there are $N_{stl}$ couples in the St. Louis region who have optimal life cycle fertility plans that induce them to pursue their first pregnancy. Therefore, in every quarter $t$ there is a race-specific distribution of age at first (attempted) birth for these women $f_t(a|z_r)$. Some of them will succeed immediately, while others will take more time. If, after 12 months of natural attempts, the woman does not get pregnant, the couple is diagnosed with clinical infertility. Let $inf(a,z_r)$ be an age- and race-specific infertility rate which increases with age. Together, $(N_{stl}, f_t(a|z_r), inf(a,z_r))$ provide the number of women, $\bar{N}_{init}^{inf}$, of each age and race who realize that they are unable to conceive without IVF. These $\bar{N}_{init}^{inf}$ women constitute the risk set, i.e. all women in the St. Louis region who may consider IVF treatment. In a final step, we obtain the risk set for our clinic by deflating $\bar{N}_{init}^{inf}$ to match the clinic’s market share as reported by the CDC. In total across all years of the sample period, we estimate that $N_{init}^{inf} = 2781$ women consider treatment at the clinic we study. See Appendix B for additional details on the calculation of $N_{init}^{inf}$ and its relationship to $f_{ZD}(Z_{ad0})$, the distribution of patient characteristics.

We compute race-specific empirical initiation shares, $s_{init}(z_r)$, for the clinic. We observe that $N_{clin} = 828$ new patients (including 35 African American) initiated treatment at the clinic during the period 2001-2007.\footnote{We use the 587 with complete data in estimation, but have records for 828 patients initiating treatment over this period.} Using our estimates of $N_{init}^{inf}(z_r)$, we calculate the share

$$s_{init}(z_r) \approx \frac{N_{clin}^{init}(z_r)}{N_{init}^{inf}(z_r)}$$

We find $s_{init}(0) = 0.072$ and $s_{init}(1) = 0.346$ which means that 7.2% of the clinic’s African American potential patients and 34.6% of its remaining potential patients decided to pursue treatment. The remaining 1953 potential patients could be induced to seek IVF treatment through large enough increases in $W_{1,s}$.

6 Empirical Specification

In this section we describe our assumptions regarding functional forms and how outcomes and utility may vary with patients' observable characteristics.
6.1 Treatment Technologies

During each treatment stage, a patient makes her choice while considering a probability distribution over outcomes that will be realized at the stage’s conclusion. We now describe the functional forms and data assumptions that describe the distributions.

In the first stage, a woman knows some basic facts about her fertility including $Z^B$, and takes drugs to stimulate egg production. We assume that the drug dosage is a function of the patient’s age and her values of $Z^B$. The woman’s characteristics and drug dosage affect a stochastic process that determines her Peak E2 score, $e$. We model the probability of a particular $e$ with a multinomial logit model for $f_e(e|Z_a)$. In the data we observe $e$ values between 0 and 10,196 pg/mL, with a mean and median around 1,600, and 99% of all values below 4,500. In the empirical implementation, we assume that the possible realizations of $e$ are in discrete bins with values 0-500, 500-1000, 1000-1500, 1500-2000, 2000-2500, and over 2500. We use a multinomial logit model here rather than an ordered model because especially high values of $e$ can be seen as bad for the patient.

In estimating $f_e$, we include variables for a woman’s age, the average of any AFC scores she receives over the entire treatment history, and her number of initially diagnosed fertility problems. The age variables we include are indicators for whether the patient’s age is: 28, 29-31, 32-34, 35-37, 38-40, 41-43, or 44. (We exclude age 35-37 for the empirical implementation.) We separate the patient’s AFC score ($z_{afc}$) into categories for scores from 1-5, 6-10, 11-15, 16-25, and 26+, with the highest category excluded for the empirical implementation. For patient fertility problems, we include an indicator for whether the patient has one or more distinct diagnosed issues ($z_{ff} = 1$).

In the second stage, the patient observes her realized value of $e$ and considers the number of eggs, $r$, that might be retrieved if she continues treatment. The distribution of $r$ depends on $e$ and $Z_a$. In the data, $r$ takes integer values from 0 to 38 with a mean of 10.6 and median of 10. The 90th percentile is at $r = 18$, and 99% of all $r$ values are below 27. We use an ordered probit model for this distribution, with possible values of $r$ as 0-4, 5-10, 11-20, and 21+. The variables that can affect the realization of $r$ are: indicators for possible values of $e$, split as they are in the model for $f_e$; the same age categories in $f_e$; the AFC score categories from $f_e$; and the indicator for whether a patient has one or more documented fertility problems.

In the third stage, the patient observes her realized value of $r$ and selects a fertilization method ($m$). The patient’s number of transferable embryos, $X$, will depend on $r$, $m$, and the patient’s characteristics. We model the process determining $X$ with an ordered probit. We include as
regressors: the possible values of \( r \) as described in the model for \( f_r \); the patient’s age, AFC score, and fertility problems as described above; and the patient’s choice of \( m \) plus the interaction of \( m \) with an indicator for male-factor infertility.

In the final stage of treatment, the patient is subject to the stochastic process \( f_k \), which determines her number of live births. We model \( f_k \) as a multinomial logit, with the probability of each outcome determined by the number of transferred embryos, the patient’s age, and the indicator for female fertility problems. Some patient and treatment characteristics, like AFC score or male factor infertility, are not relevant here because their roles in determining outcomes is finished once the patient has her set of transferable embryos.

### 6.2 Utility assumptions

We must make functional form assumptions for several expressions that are relevant for patients’ utility. In addition to the restriction that all patients have the payoff of \( U(k|\tilde{k}, \tau) = 0 \) from zero-birth outcomes, we assume that outcomes with \( k > 0 \) provide utility according to:

\[
U(k|\tilde{k}, \tau) = u_k + \kappa \times 1\{\tilde{k} > 0\} + \zeta \times 1\{\tau = 2\}
\]

The parameter vector \((u_1, u_2, u_3)\) captures the lump-sum payoff from a singleton, twin, and triplet birth to a patient with no prior children \((\tilde{k} = 0)\). Given the health risks and other challenges for triplets, we anticipate that \( u_3 < u_2 \) and \( u_3 < u_1 \), but these parameters are unrestricted in estimation. The parameter \( \kappa \) captures any difference in the marginal benefit of a birth to patients with prior children \((\tilde{k} > 0)\); diminishing marginal utility from children would imply that \( \kappa \) is negative. We account for the impact of ASRM guidelines on utility by specifying \( \eta(x, Z_a) = \eta_0 \times 1\{x, Z_a\} \), where \( \eta_0 \) is a constant utility penalty and \( 1\{x, Z_a\} \) is an indicator function that is equal to one for any choice of embryos \( x \) that is outside of the contemporary ASRM guidelines for a patient with state variables \( Z_a \).

We assume a simple two-type structure for patients’ permanent unobserved heterogeneity. A share of patients with type \( \tau = 1 \) has preferences for birth outcomes represented only by \((u_1, u_2, u_3, \kappa)\), while the remaining patients (with \( \tau = 2 \)) has, in addition, its utility payoff shifted by a scalar parameter \( \zeta \). A patient’s probability of being of type \( \tau = 2 \) depends on her state values at the time she initiated treatment, \( Z_{a_0}^D \). Along with \( a_0 \), we allow the distribution of \( \tau \), conditional

\(^{30}\)In practice, no patients in the main data choose to go outside of the guidelines by more than a single embryo, so we do not have the opportunity to estimate different penalties for different degrees of violation.
on initiation, to depend on a measure of her wealth level \((z_w)\), her race \((z_r)\), her initial number of insurance-covered cycles \((t_{a0})\), and a dummy \((z_{asrm0})\) for the ASRM guideline regime when treatment started. The dependence of the distribution of \(\tau\) on the state variables reflects the need to acknowledge that differences across patients’ circumstances will result in a different selection of patients depending upon their intensity of taste for children. The value of initiation depends on various state variables and the unobserved type, and we expect a differential propensity to initiate by the two types. For example, conditional on being uninsured, one would expect a higher prevalence of patients with high taste for children (relative to the prevalence among potential patients). As a result, regardless of whether types are correlated with demographics in the pool of potential patients, the distribution of types within the clinic will surely depend on the state variables. We assume that the probability of a high type \((\tau = 2)\) is

\[
\Pr(\tau = 2 | Z_{a0}^D, I = 1, \rho) = \frac{\exp(\rho_0 + \rho_1 a_0 + \rho_2 z_w + \rho_3 t_{a0} + \rho_4 z_{asrm0} + \rho_5 z_r)}{1 + \exp(\rho_0 + \rho_1 a_0 + \rho_2 z_w + \rho_3 t_{a0} + \rho_4 z_{asrm0} + \rho_5 z_r)}.
\]

During estimation we restrict \(\rho_0 < 0\) for computational purposes, but this adds no real restrictions on the utility parameters. For notational convenience, we let \(\rho\) represent a column vector of \(\{\rho_j\}_{j=0}^5\) values. In addition, we write \([1, Z_{a0}^D]\) as a vector containing 1 and an individual patient’s row vector \(Z_{a0}^D\), and we let \(\Lambda\) represent the logistic distribution function so that \(\Lambda([1, Z_{a0}^D] \rho) = \Pr(\tau = 2 | Z_{a0}^D, I = 1, \rho)\).

As the patient makes her choice between starting a treatment cycle or delaying, she considers the additional flow benefit \(u_s\) which she receives (or sacrifices) when she begins a treatment cycle. We assume that \(u_s = \delta\), a scalar parameter. The value of \(u_s\) is identified, in part, by the frequency with which clinic patients return for additional treatment cycles following their first cycle.

The first three stages of IVF treatment include \(\alpha(z_w)\), the disutility from paying a price \(p\) for some treatment component. We specify \(\alpha(z_w)\) as an affine function of \(z_w\): \(\alpha(z_w) = \alpha_0 + \alpha_w z_w\). Since the effect of price is subtracted from within-stage value functions above, we expect \(\alpha_0\) to be positive for consistency with downward-sloping demand. If wealthier patients are less price sensitive, this will be captured through \(\alpha_w < 0\).

We assume that the terminal payoff \(u_T\) is a function of the patient’s cumulative payments for treatment. Children born due to treatment are not included here because those benefits are included in \(U(k|k, \tau)\). We add the variable \(z_p\) as an indicator for whether a patient ever paid full price for a treatment cycle. We assume \(u_T = \gamma_p z_p\), which includes the normalization \(u_T = 0\) for
patients who have never paid the full price of treatment.

At the initiation stage we specify that the individual-specific taste shock $\nu$ is distributed according to a continuous distribution $F(\nu)$ in the population of potential patients. The realizations of $\nu$ are i.i.d. Moreover, we assume $\nu$ is independent of infertility problems and other observables in our model, so $F(\nu|\tau,Z_{a_0}^D) = F(\nu)$. We assume $\nu \sim \text{Logistic}$ so we have $F(\nu) = \Lambda(\nu) = \frac{\exp(\nu)}{1+\exp(\nu)}$.

Let $\varphi$ represent a vector of all of the parameters except $\mu$, $\zeta$, and $\rho$, and define $\theta = (\zeta, \varphi, \rho)$. We estimate $\mu$ separately from $\theta$ so it is convenient for us to distinguish between the two.

### 7 Estimation

We estimate the model in three stages. We estimate the treatment technologies, $f_e$, $f_r$, $f_X$, and $f_k$ in the first stage. These models are easy to estimate using conventional statistics packages. We use the parameter estimates from this estimation step to characterize the stage-specific distributions of treatment outcomes for each combination of fertility-related state variables and each possible stage-specific action a patient may take. We implicitly assume that we, as econometricians, have the same information on outcome probabilities as the patient and her doctor. Within this stage we also estimate the distribution of $f_{Z^B}(Z^B|a_0)$ non-parametrically using frequencies of $Z^B$ realizations from within the population of women who initiate treatment. In the second stage we estimate the parameters in $\theta$ using data exclusively from the population of 587 patients who are observed within the clinic. In the final stage, we estimate $\mu(z_r)$ using our estimates of $E[W_{s,1}(Z_{a_0})|Z_{a_0}^D]$ together with the market-level data.

#### 7.1 Within-clinic Choices

Given the estimated treatment technologies, a guess at the value of the structural parameters in $(\zeta, \varphi)$, and the distributional assumptions on $\varepsilon$, we are able to calculate $W_{y,j}(Z_{a},\tau;\zeta,\varphi)$ and $E[W_{j}(Z_{a},\tau;\zeta,\varphi)]$ for each $y$ and $j$ at every $Z_{a}$. We perform this calculation by backward recursion separately for each type $\tau$. For each potential state that might be reached when the patient is age $a_{\text{max}}$, we use $(\zeta, \varphi)$ to compute the terminal payoff, the values of $W_{y,j}(Z_{a_{\text{max}}},\tau;\zeta,\varphi)$ working backwards through treatment stages, and the logit inclusive value $E[W_{j}(Z_{a_{\text{max}}},\tau;\zeta,\varphi)]$ for each stage. We then move to age $a_{\text{max}} - 1$ and use the $a_{\text{max}}$ expected utility values while constructing $W_{y,j}(Z_{a_{\text{max}}-1},\tau;\zeta,\varphi)$ and $E[W_{j}(Z_{a_{\text{max}}-1},\tau;\zeta,\varphi)]$. The procedure continues back to age $a_{\text{min}}$.

Let $d_{y,j,a,i} \in \{0, 1\}$ represent patient $i$’s binary choice whether to take action $y$ in stage $j$ while
at age $a$. We write $d_i$ as the patient’s complete history of choices at the clinic. We use the calculated values of $W_{y,j}(Z_a, \tau; \zeta, \varphi)$ for all $Z_a$ and $\tau$ to compute choice probabilities for each observed decision in our data. Conditional on a patient’s type $\tau$, calculating this probability is a straightforward task due to the i.i.d. extreme value assumption for the $\varepsilon$ terms. For example, conditional on a patient reaching a stage 2 decision over whether to continue (c) or cancel (nc) the current treatment cycle, her probability of continuing is:

$$\Pr(d_{c,2,a,i} = 1 | Z_a, \tau; \zeta, \varphi) = \frac{\exp\left[ W_{c,2}(Z_a, \tau; \zeta, \varphi) \right]}{\exp\left[ W_{c,2}(Z_a, \tau; \zeta, \varphi) + W_{nc,2}(Z_a, \tau; \zeta, \varphi) \right]}$$

The values of $W_{c,2}(Z_a, \tau; \zeta, \varphi)$ and $W_{nc,2}(Z_a, \tau; \zeta, \varphi)$ are relatively simple functions of the estimated treatment technology $\hat{f}$, price and its disutility parameter, and the calculated values of $E[W_3(\tau, Z_a, \varepsilon_{3,a})]$ and $E[W_1(Z_{a+1}, \varepsilon_{1,a+1})]$. We calculate a probability like this one for each observed decision by each patient, including the implicit choices to delay further treatment attempts which occur during periods when the patient does not appear in the data despite starting treatment during some earlier period.

A patient’s permanent unobserved type, $\tau$, affects every period and stage of her decision problem. Let $\Pr(d_{y,j,a,i} = 1; Z_a, \tau, \zeta, \varphi)$ represent the predicted probability that patient $i$ takes the observed action $d_{y,j,a,i}$ if she has type $\tau$. The patient is observed starting in period $t_i,0$ and ending in $T_i$. Conditional on $\zeta$ and $\varphi$, the type-specific joint probability of observing patient $i$’s sequence of choices is:

$$L_i(d_i; \tau, \zeta, \varphi) = \prod_{a=a_0}^{T_i} \prod_{j=1}^{Y_i} \prod_{y=1}^{Y_j} \Pr(d_{y,j,a,i} = 1; Z_a, \tau, \zeta, \varphi)^{d_{y,j,a,i}}.$$ 

With $i$’s true type $\tau$ unobserved, the likelihood of observing her choices requires integration over $\tau$, which is simply

$$L_i(d_i; \theta) = \sum_\tau L_i(d_i; \tau, \zeta, \varphi)f_\tau(\tau|Z_{i,a_0}, I = 1, \rho).$$

The log-likelihood of observing the choices of all patients in the clinic data is

$$\mathcal{L}(\theta) = \sum_i \log[L_i(d_i; \theta)].$$

We estimate $\theta$ by maximizing the value of $\mathcal{L}(\theta)$. We compute standard errors following the “outer product of the score” method for $\theta$ only. In computing standard errors we do not account for potential sampling error in our first stage estimates.
In this second stage, the key model parameters recovered by the maximum likelihood procedure are the “price coefficient” \( \alpha_0 \) and the non-parametric utility from children, given by \( u_k \) for \( k = 1, 2, 3 \). Identification of \( \alpha_0 \) comes from various features of the clinic data. Specifically, it primarily draws on the following three sources of variation. First, since every patient that we observe at the clinic started at least one cycle, cross-sectional differences in insurance coverage during the first cycle provide identifying variation through different cancellation decisions. Greater price sensitivity induces patients facing higher prices (due to insurance variation) to be more selective in their decision to continue on to the second stage – the most expensive one – involving egg retrieval. Second, while all clinic patients started at least one cycle, uninsured patients are (all else equal) less likely to return for another attempt after an initial failure. Again, the greater the price sensitivity measured by \( \alpha_0 \), the greater the observed differential return rate of uninsured vs. insured patients. Third, additional variation comes from the observed behavior of the subsample of initially-insured patients as they approach the exhaustion of their covered cycles, relative to their behavior in earlier cycles. The greater the price sensitivity, the greater the tendency of insured patients to take actions that either preserve the last remaining insured cycles (by cancelling more often) or make sure that the cycle succeeds (by increasing the number of embryos transferred). Identification of \( \alpha_w \) comes from contrasting these arguments in subsamples of low versus high wealth patients.

The identification of the \( u_k \) values can be obtained with the embryo-transfer choice data under our assumption that patients know the probabilities of different birth outcomes for each potential embryo choice. Through her embryo-transfer choice, the patient essentially chooses among different potential lotteries over birth outcomes \( k \). For example, if patients strongly dislike triplet outcomes (i.e. they have a very negative value for \( u_3 \)), then they will avoid embryo choices that are more likely to produce triplets. While the identification of the \( u_k \) does not require variation in ASRM guidelines, which changed in the middle of our sample period (2004), such variation is also helpful for identification. Comparing the transfer behavior of patients with similar characteristics facing different recommended choice sets helps identify preferences for birth outcomes as well as the penalty parameter \( \eta_0 \). Of particular value is data on how similar patients behave when guidelines change with respect to single embryo transfers.
7.2 Treatment Initiation

We estimate the initiation decision in a third step, taking the within-clinic estimates from the second step \( \hat{\theta} = (\hat{\zeta}, \hat{\rho}, \hat{\varphi}) \) as given. Under our assumptions about initiation, we may write

\[
\Pr (I = 1|Z_{a_0}^D, \tau, \varphi, \zeta, g_E, \mu) = \Lambda \left( W \left( Z_{a_0}^D, \tau, g_E, \varphi, \zeta \right) - \mu (z_r) \right),
\]

where the variable \( I \) indicates whether a patient with characteristics \( Z_{a_0}^D \) started treatment at age \( a_0 \). We integrate over observed and unobserved patient characteristics to compute the model predicted rates at which the clinic’s potential patients of both races actually become patients, \( \hat{s}^{\text{init}} (\mu (z_r); g_E, \hat{\theta}) \). These race-specific distributions – \( f_{Z^D|z_r} (Z_{a_0}^D) \) for observed characteristics and \( f_{\tau|z_r} (\tau|Z_{a_0}^D) \) for unobserved heterogeneity – will in general be different in the full potential patient pool versus among patients who choose to initiate treatment. We estimate the parameters \( \mu (z_r) \) by solving

\[
\hat{s}^{\text{init}} (\mu (z_r); g_E, \hat{\theta}) = s^{\text{init}} (z_r)
\]

for each race \( z_r \) under the empirical policy setting, \( g_E \). \( s^{\text{init}} (z_r) \) is the race-specific, empirical initiation share that we construct from the count of actual patients given \( z_r \) and our estimate of the size of the potential patient pool with race \( z_r \). \( \hat{s}^{\text{init}} \) is the initiation share predicted by the model for a given value of \( \mu(z_r) \). We estimate \( \mu \) for each race by finding the value that makes the model-predicted race-specific initiation share \( \hat{s}^{\text{init}} \) match the observed share, \( s^{\text{init}} \). Note that under alternative policies, \( W \left( Z_{a_0}^D, \tau, g, \varphi, \zeta \right) \) will change but \( \mu (z_r) \) remains fixed.

We approach the distributions \( f_{\tau|z_r} (\tau|Z_{a_0}^D) \) and \( f_{Z^D|z_r} (Z_{a_0}^D) \) using different strategies. In Appendix A we show that our assumptions on: a) the distribution of unobserved types conditional on treatment initiation, \( f_{\tau} (\tau|Z_{a_0}^D, I_i = 1, \rho) \); and b) the initiation decision, are sufficient to back-out the unconditional (on initiation) race-specific distributions \( f_{\tau|z_r} (\tau|Z_{a_0}^D) \). We write the incidence of \( \tau = 2 \) within-clinic as \( \Lambda (1, Z_{a_0}^D|\rho), \) and \( \Lambda \left( W \left( Z_{a_0}^D, \tau, g_E, \varphi \right) - \mu (z_r) \right) \) provides the race-specific probability of initiation for \( \tau = 1, 2 \). In Appendix B we describe our approach to constructing \( f_{Z^D|z_r} (Z_{a_0}^D) \) using market data.

The estimates for \( f_{\tau|z_r} (\tau|Z_{a_0}^D) \) and \( f_{Z^D|z_r} (Z_{a_0}^D) \) allow us to derive \( s^{\text{init}} (\theta, \mu (z_r), g_E) \), the model-predicted fraction of potential patients of race \( z_r \) who actually become patients). To obtain \( s^{\text{init}} (\mu (z_r); g_E, \theta) \), we integrate the initiation probability \( \Pr (I = 1|Z_{a_0}^D, \theta, \tau, \mu (z_r)) \) over the
race-specific distribution of $Z_{a0}^D$ and $\tau$ among potential patients

$$\hat{s}^{\text{init}}(\mu(z_r); g_E, \hat{\theta}) = \Pr(I = 1|\hat{\theta}, \mu(z_r), g_E) = \sum_{Z_{a0}^D} \sum_{\tau} \Lambda \left( W \left( Z_{a0}^D, \tau, g_E, \hat{\varphi}, \hat{\zeta} \right) - \mu(z_r) \right) f_{\tau|z_r} \left( \tau|Z_{a0}^D, \mu, \hat{\theta} \right) f_{Z_{a0}^D|z_r}(Z_{a0}^D)$$

We use a bootstrap procedure based on the sampling distribution of $\hat{\theta}$, to construct a confidence interval on $\hat{\mu}$ for each race. In particular, we draw 400 times from $\hat{\theta}$'s distribution, and for each draw we calculate the values of $\mu$ that equate $s^{\text{init}}$ and $\hat{s}^{\text{init}}$ for each race. We then sort the individual estimates of $\mu$ and use the 2.5\textsuperscript{th} and 97.5\textsuperscript{th} percentile values as the 95\% confidence interval. The confidence interval on $\mu$ is not interesting in own right, but it plays a critical role in describing the precision of predicted treatment-initiation decisions, which we discuss below.

8 Results

8.1 Technology estimates

In this subsection we discuss our estimates of the four treatment stages’ technologies. These technologies are dependent on a patient’s characteristics, and a patient’s knowledge of them is a crucial part of how she solves her personal dynamic optimization problem. Rather than providing parameter estimates for each treatment technology, we use a collection of figures to discuss the role each technology plays in the choice process. One of our overall goals is to emphasize the importance of allowing forward-looking dynamic behavior at each treatment stage.

During the first treatment stage, the patient decides whether to start or delay an IVF cycle. She is aware of her full state vector, $Z$, which includes her AFC score, $z_{afc}$. At this point in the decision process, she considers her probable peak estradiol score ($e$), which will be revealed in Stage 2 if she starts treatment. In Figure 2 we display (estimated) probability distributions over $e$ for two AFC score categories. The figure shows that having an AFC score below 5 substantially shifts to the left the distribution of $e$ that the patient can expect to realize at the beginning of stage 2.

The patient cares about her value of $e$ because it affects outcomes in later stages. In Figure 3 we show that the realized $e$ influences the distribution of the number of eggs that will be successfully retrieved ($r$) in stage 3. Indeed, if $e$ is low (e.g. in the 500-1000 range) the mode of the distribution of eggs is 6-10 whereas if $e$ is relatively high (2000-2500) the mode of the distribution of eggs is 11-20.
and the probability of a low egg count (1-5) is almost zero. This strong difference in \( r \) outcomes at different values of \( e \) justifies our treatment of \( e \) as a within-period state variable that is critical to continuation/cancellation decisions in stage 2.

In treatment stage 3, a patient chooses her fertilization method (\( m \)). This choice, interacted with the patient’s state variables, influences the distribution of available embryos (\( X \)) in stage 4. In Figure 4 we display the distributions of \( X \) with \( (m_2) \) and without \( (m_1) \) ICSI for patients whose partners have male-factor infertility. The figure shows that the more technologically advanced fertilization method (ICSI) shifts the distribution to the right, increasing the probability of having 4 or more viable embryos and reducing the probability of having a small embryo count.

Once the patient has realized her value of \( X \), she chooses the number of embryos (\( x \)) to transfer back into the uterus subject to \( x \leq X \). In Figure 5 we display evidence on how \( x \) affects the distribution of births (\( k \)). Transferring 3 embryos instead of 2 reduces the chance of no birth from about 60% to under 50%, but the probabilities of twins and triplets increase. It is important to notice, however, that the probability of having no live births is fairly high regardless of whether 2 or 3 embryos are transferred. Finally, in Figure 6 we explore the effects of age. We focus on patients who transfer \( x = 3 \) embryos in stage 4. As expected, the distribution for older (age > 35) women shifts to the left, noticeably increasing the odds of no live birth.

### 8.2 Utility parameters

Taking as inputs the technology parameters described above, we estimate the model’s structural taste parameters. In Table 4 we display our estimates of \( U(k|\tilde{k}, \tau), \alpha, \delta, \gamma, \) and \( \eta \). Our estimates of \( u_1, u_2, \) and \( u_3 \) represent payoffs from different birth outcomes to patients with \( \tau = 1 \) and no prior children. These estimates show that patients receive a positive payoff from a singleton or twin birth, with the latter valued slightly more. Triplet births, by contrast, have a negative utility payoff for patients. The estimate of \( \kappa \) indicates that patients with 1 or 2 prior children have their utility from births shifted downward substantially. For example, for a patient with \( \tilde{k} > 0 \) and \( \tau = 1 \), the estimated \( \kappa \) implies that the patient would prefer no additional children. The taste shifter \( \zeta \) associated with type 2, however, is sufficient to increase the utility from additional births to be positive for patients with \( \tilde{k} > 0 \).

Table 4’s results indicate that the baseline price disutility is significantly different from zero for all patients, and this disutility is smaller for high-wealth patients. We recover a significantly negative estimate for the start/delay parameter \( \delta \), which plays a large role in determining whether a
patient returns for additional treatment cycles after her first. Our estimate of the parameter $\gamma$, for a patient’s terminal payoff $w_T$, shows no significant difference between the utility of patients who have paid out-of-pocket for a treatment and those who have not. The final utility parameter on Table 4 is $\eta_0$, the utility shifter from selecting an $x$ outside of ASRM embryo transfer guidelines. We recover a negative value for this parameter, indicating a penalty for deviating from the guidelines.

Table 5 reports results on the distribution of $\tau$ within the treated population. We estimate that about half of the patient population has type $\tau = 2$ given their $Z$ values. To interpret the individual $\rho$ parameters, consider the case of patient wealth. The negative coefficient ($\rho_2$) on the wealth measure indicates that a high-wealth person selected from the treated population is less likely to have type $\tau = 2$ than a treated low-wealth person. This accords with the intuition that treatment expenses are most likely to discourage low-wealth individuals with relatively small payoffs from having children through IVF.

Finally, in the third estimation step we recover $\hat{\mu}(1) = -0.34$ for African Americans and $\hat{\mu}(0) = -2.17$ for all other potential patients. These values of $\mu$ ensure that the initiation model generates treatment initiation decisions such that, as estimated from our data, 30% of all potential clinic patients (7.2% of African Americans and 34.6% of others) indeed choose to become clinic patients and undergo at least one IVF cycle.

8.3 Model fit

We conduct two procedures to evaluate model fit. First, we compare the estimated model’s predicted choice probabilities to those we observe in the data. This provides a straightforward way to examine choice probabilities at the four stages of IVF treatment; all predictions match the data fairly well. Start/delay decisions, which are observed most frequently in the data (and are assisted by the intercept term $\delta$) have the tightest fit. In all periods after initiation, patients in the data choose “start” in 3.9% of all opportunities, while our estimated model predicts that patients choose “start” with frequency of 3.5%. Stage 2 and 3 predicted decisions also follow the data fairly closely. Some differences are to be expected, however, because these stages’ fits depend on overall $W_j$ values rather than individual parameters. We observe cancelation (stage 2) and ICSI (stage 3) frequencies of 15.0% and 42.7%, respectively, and our model provides choice probabilities of 21.9% and 57.3%. Figure 7 provides a comparison of distributions across stage 4 choices. The estimated model succeeds in matching $x = 2$ as the most common choice in stage 4, followed by $x = 3$. Transfers of 1

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$^{31}$The 95% confidence interval for $\hat{\mu}(1)$ is $[-0.85, 0.50]$ and for $\hat{\mu}(0)$ is $[-2.57, -1.57]$
and 4 embryos are rare in the data (and model) because of the utility penalty for deviating from ASRM guidelines and the negative payoff from a triplet birth (in the case of $x = 4$).\footnote{We have explored whether choices in a patient’s second IVF cycle or beyond can be explained by outcomes during stage 1-3 of her first IVF cycle. These variables have no significant impact on later-cycle choices. We view this result as evidence to support our assumption that the patient does not respond to health variables other than those in $\mathbf{Z}^H$ or revealed during the current cycle.}

In a second set of exercises, we evaluate the predicted choice and outcome histories for the population of 587 observed patients. These histories begin with the same state variables ($\mathbf{Z}$) as the patients in the data, but then random draws on medical outcomes and taste shocks determine choices and outcomes over time. For each patient we repeat the process ten times, allowing for the realization of different taste shocks and stochastic medical outcomes. We average over patients and their individual simulated histories in computing the statistics we report below.

We focus on two critical measures of effectiveness and efficiency of IVF treatment. First we ask: What proportion of patients eventually succeed in delivering at least one live birth through IVF, regardless of the number of attempted cycles required to do so? We find that 59% of our simulated patient histories include a birth, which is reasonably close to the empirical value of 53% reported on Table 2. Second, we investigate how many cycles an individual patient receives at the clinic. In our simulation, 53% of patients are observed taking a single cycle, 28% undergo two cycles, and 19% receive three or more cycles. These results compare very well to the data, in which we see 54%, 27%, and 19% of patients receive one, two, or three or more cycles, respectively. Patients’ responses to price variation, which come through differences in insurance status, also match well between the data and model. In the data, insured patients take an average of 1.97 cycles during their full treatment histories, while uninsured patients average 1.50 cycles. Our simulated patient histories contain an average of 1.99 cycles for insured patients and 1.56 for uninsured. Both the data and simulated histories contain only small differences in embryos transferred by insurance status; we return to the relationship between insurance and embryos below.

9 Counterfactual experiments

We use the estimated model to consider a set of counterfactual policy experiments which analyze potential IVF patients’ responses to changes in their decision environment ($g$). Extensive-margin choices are crucial for this analysis, so we employ the full “at risk” population of $N^{inf} = 2781$ potential patients described above.\footnote{Women’s human capital accumulation, career decisions, age at marriage, and age at first birth may be affected by some of the changes we implement in our counterfactuals experiments. These responses might have an effect on their future decisions and choices in IVF treatment. We assume that these factors are exogenous to the model and do not interact with the treatment decisions.} These potential patients represent the portion of the St.
Louis market served by the clinic we study. While we do not discuss other clinics in the market, in our counterfactuals we implicitly assume that all clinics are subject to the same policies. When considering absolute magnitudes below (e.g., numbers of births, dollar values) these figures can be multiplied by about three to understand the impact of a policy on outcomes in the St. Louis market as a whole. In 2012, St. Louis clinics performed about 1% of all cycles in U.S. clinics.

For each potential patient, we draw age, wealth, insurance, race, and ASRM regime values that are consistent with the empirical distributions of these values. Along with the distribution of biological state variables (not yet revealed to potential patients), we use the estimated model to construct $W \left( Z_{a0}^D, \tau, g, \tilde{\tau}, \tilde{\zeta} \right)$ for each simulated woman. The values of $W \left( Z_{a0}^D, \tau, g, \tilde{\tau}, \tilde{\zeta} \right)$ differ across policy experiments. We then allow potential patients to elect whether to begin treatment by comparing $W \left( Z_{a0}^D, \tau, g, \tilde{\tau}, \tilde{\zeta} \right)$ to the population-wide utility parameters $\tilde{\mu}(z_r)$ and a simulated value for the potential patient’s taste shock $\nu$. For all potential patients, we simulate initiation choices and decision histories in the same way described above for evaluating model fit, including repeating the process ten times for each potential patient in $N^{inf}$. Potential patients who do not start treatment at $a_0$ exit the model forever.

We assume that the $N^{inf}$ simulated potential patients arrive at the fertility decision uniformly over the 2001-07 window during which the 587 observed clinic patients began treatment. As in the data used for estimation, the simulated patients’ histories are followed from their initiation decision through 2009. To maintain consistency with our empirical model, we focus on counterfactual outcomes during 2001-09, and we continue to refer to this window as the “sample period.”

Across all experiments we hold fixed the clinic’s prices. While substantial changes in the policy environment may prompt the clinic to adjust its prices, we do not offer a model of how new equilibrium prices would be set. The clinic is part of a large medical school’s teaching hospital, so it is not clear what objective function is used to set prices. We note that during the full sample period the clinic elected to keep its prices fixed at the same level. In fact, the typical IVF cycle price in the U.S. has remained approximately unchanged between the mid-1990s and the present, despite a substantial increase in the number of treated patients.

We report our main results in Tables 6-7 and Figures 8-9. The tables contain both point estimates of counterfactual outcomes and 95% confidence intervals calculated with the same bootstrap procedure described above. The figures focus on embryo transfer choices and birth outcomes the size and composition of the pool of potential patients. We abstract from these considerations. Buckles (2005), Abramowitz (2014) and Gershoni and Low (2015) explore the existence and magnitude of such effects.
under selected policies in which these choices and outcomes are particularly interesting. Because
the figures and tables contain results from all experiments collected together, it is worthwhile to
introduce them briefly and define terms. First, we calculate histories for \( N^{inf} \) potential patients
under the observed choice environment; we refer to this as the “Empirical baseline” and index it as
\( g_E \). We then consider a variety of insurance policies that provide patients with a specified number
of treatments. We begin by simulating the market when no patients have treatment insurance (“No
insurance,” \( g_N \)). We contrast this with a policy that provides Illinois-style insurance for four IVF
cycles to all potential patients, without exceptions, in both states; this is “Universal insurance for
treatment” and is indexed as \( g_{IT} \). We augment \( g_{IT} \) with three policies designed to reduce embryo
transfers. An “IT + embryo cap” (\( g_C \)) policy limits all patients to transferring a single embryo.
The policy “IT + actuarially fair top-up prices” (\( g_{AT} \)) allows patients to receive multiple embryos,
but they bear the entire additional expected birth costs from multiple-embryo transfers. In the
final experiment with treatment-focused insurance, we illustrate the implications of reduced but
positive top-up prices (“IT + moderate top-up prices,” \( g_{MT} \)). We contrast treatment-focused in-
surance with outcome-focused insurance in two final policy simulations. First, we allow patients to
receive as many insured treatments as they choose, provided they have one or fewer children when
each cycle begins (“Universal insurance for outcomes,” \( g_{IO} \)). Second, we demonstrate the impact
of dynamics and forward-looking behavior by simulating the impact of an outcome-based insurance
policy in which insurance benefits are reduced for older patients (“Age-adjusted insurance for
outcomes,” \( g_{IA} \)).

Before describing the individual policy experiments, we describe some of the outcomes that
we calculate under the empirical distribution of insurance (\( g_E \)). Under the observed prices and
constraints, we find that 29.9% of potential patients elect to begin treatment. This initiation rate,
combined with success probabilities within the clinic, results in 15.9% of women in \( N^{inf} \) achieving
at least one birth during the sample period. About 53% of simulated patients who begin IVF
achieve a birth at some point in the treatment history; this matches the observed rate in the actual
patient population. On average across ten simulated histories under \( g_E \), the baseline simulations
average 456 births for the 2781 patients in \( N^{inf} \); these births deliver 636 infants to the population,
implying an average number of infants per birth of 1.4.

For each patient who begins treatment we calculate \( \Delta_i = W \left( Z_{i,a_0}, \tau_i, g, \hat{\varphi}, \hat{\zeta} \right) - (\hat{\mu}(z_r) + \nu_i) \),
use each pair \((\theta, \mu)\) to compute the full set of patient histories under each counterfactual policy described below. We construct confidence intervals using the 2.5^th and 97.5^th percentile of each outcome (across \((\theta, \mu)\) pairs) within a policy setting.

38
which is a measure of the net utility gain from initiating IVF above the outside option. Patients who elect to forego treatment receive $\Delta_i = 0$. We use $\hat{\alpha}_i$, our estimate of the disutility from payments for each patient $i$ (which varies depending on $i$’s wealth) to obtain a patient-specific dollar-valued surplus measure, $CS_i(g) = \Delta_i/\alpha_i$. Across all potential patients in $N^{inf}$, including those who do not initiate treatment, the total $CS(g_E) = $10.3M, or about $3,700 per person in the risk population (or $12,400 conditional on initiation). If insurers must pay the difference between insured patients’ prices and the full price, the empirical baseline requires a total of $3.6 million in payments from insurers to the clinic. Finally, we calculate the total medical costs of all pregnancies and births that occur under $g_E$, using the cost estimates from Lemos et al. (2013) discussed above. Using these figures, the total pregnancy- and delivery-related medical cost of the baseline is $31.4 million, or $68,900 per birth. When insurance costs for treatment are included along with delivery costs, the average cost per birth is $76,872 (or $55,105 per child).

We use the simulated population to calculate price elasticities as well. Prices paid by insured and uninsured patients have different interpretations, so we calculate changes separately with respect to each price. When out-of-pocket prices for uninsured patients rise by 5%, we calculate that 6.4% fewer uninsured patients initiate treatment, implying an elasticity of $-1.28$ at the extensive margin. The same price increase has a slightly larger impact on the total number of uninsured cycles, which falls by 6.7% for an elasticity of $-1.33$. The elasticities values are different, in part, because patients who continue to initiate despite higher prices may choose to reduce their total numbers of cycles. We perform the same calculations with prices paid by insured patients (holding fixed uninsured prices), and we obtain elasticities that are smaller in magnitude. The impact of a 5% increase in out-of-pocket expenses for insured patients results in 1% fewer insured patients initiating and a total reduction of 1.4% in insured cycles. While elasticities above $-1$ are inconsistent with profit maximization, the clinic may have different objectives than a traditional firm. These elasticities are comparable to others from the health care literature (e.g., Manning et al., 1987).

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35Policies that have increased insurance costs (e.g. from universal insurance) will eventually pass these costs on to consumers in the form of higher premiums, and this could reduce welfare. Two factors, however, may moderate this welfare loss. First, the population of individuals purchasing health insurance policies is much larger that the risk population we focus on, so per-capita premium increases could be small. Second, insurance coverage of IVF would provide additional benefits to women who do not know whether they will join the risk pool. These issues are beyond the scope of our paper.

36We were unable to obtain actual cost data for individuals in our sample since deliveries may occur at any hospital chosen by the patient. Data from the National Inpatient Sample shows that delivery costs in Missouri are similar to those nationwide, while Illinois is slightly above the national average.
9.1 Impact of insured treatment

In our first set of counterfactual policies, we consider the impact of a substantial expansion of insurance in the market. To establish a baseline, we begin by simulating treatment choices and outcomes when no patients have insurance ($g_N$). In this setting, we find that 24.2% of the at-risk population chooses to initiate IVF, and 12.7% of the at-risk population conclude treatment with one or more births. The availability of IVF generates $7.6M in surplus for patients, who initiate treatment only if expected surplus is positive. While there are no insurance costs of treatment in this setting, patients who become pregnant and give birth generate $25M in medical costs, which amount to $69,414 per birth.

When Illinois-style insurance is extended to all potential patients ($g_{IT}$), the number of treated women and births increase substantially. We find that 57.7% of potential patients in the simulated risk pool initiate treatment, and 31.5% in this population experience a birth during the sample period.\(^{37}\) The presence of insurance has an impact on both initiation and the choice whether to continue treatment after a failure. While patients without insurance (in $g_N$) take an average of 1.24 cycles over their treatment histories, insured patients receive 1.43 IVF cycles on average. Despite a reduction in the price of treatment, the distribution of embryos transferred is very similar under $g_N$ and $g_{IT}$ (Figure 8). Likewise, the distribution of births (Figure 9), shows little difference between $g_N$ and $g_{IT}$. This suggests that the extension of insurance benefits has a minimal impact on the multiple birth rate, whether through patient selection or the incentives of patients who would have received treatment when paying full price. In our model, this is explained by the strong utility benefits that patients receive from twins, and the relatively low risk of triplets. Taken together, patients have little reason to reduce the aggressiveness of their embryo-transfer decisions.\(^{38}\)

The patient surplus benefits of Illinois-style insurance are substantial, with total $CS(g_{IT}) = $18.4M, which is $10.8M greater than under $g_N$. To evaluate the full impact of $g_{IT}$, however, we must account for additional costs due to insurance payments and medical delivery costs. As reported on Table 7, the insurance costs of $g_{IT}$ are substantial, at $16.4M. The difference between the changes

\(^{37}\)If, contrary to our assumptions, potential patients have some information about $Z^B$ prior to initiating treatment, we expect that this could affect the magnitudes of our policy predictions. For example, if prior information about $Z^B$ implies that patients who select into treatment have better fertility characteristics than the average woman who experiences infertility, then policy changes which reduce IVF’s price would have a smaller impact than we predict. On the other hand, if patients choose how quickly to move from lower-tech infertility treatments to IVF, then a price-reducing policy change might result in relatively more new patients with favorable fertility characteristics.

\(^{38}\)By contrast, Hamilton and McManus (2011) find that insurance mandates reduce embryo transfers. That result, however, is based on an earlier sample period (1995-2003) when IVF technology was more likely to fail and patients transferred an average of one additional embryo per treatment.
in consumer surplus and insurance costs is to be expected considering the traditional medical-demand “moral hazard” incentive of patients to take insured treatment when their willingness to pay is less than the price for uninsured patients. The expansion of insurance coverage, therefore, must be defended through arguments about fairness or equal access. While all potential patients benefit from universal insurance, we find in supplemental analysis that increases in access and surplus are greater for patients from lower wealth areas \((z_w = 0)\). Overall insurance and delivery costs per birth are $85,213 with policy \(g_{IT}\), although the difference between this figure and the no-insurance value is almost entirely due to the introduction of insured treatment costs. Delivery costs per birth are largely unchanged because the distribution of birth outcomes is unchanged.

9.1.1 Embryo caps

We next explore the impact of restricting patients to transfer only a single embryo during treatment. We do this in the context of universal insurance so that our setting is close to the implementation of embryo caps as they have been introduced in practice, i.e. in countries with generous health insurance. To simulate the policy \(g_C\), we solve the model again at the estimated parameters but we impose the restriction \(x \leq 1\) instead of \(x \leq X\) in stage 4 (the embryo transfer stage). We also remove the utility penalty for single-embryo transfers for circumstances when these conflict with ASRM guidelines. We then use the new policy functions together with the same history of \(\varepsilon\) and medical technology shocks to simulate counterfactual patient histories under the one-embryo cap.

The restriction on embryo transfers reduces the expected value of IVF for patients considering treatment. The share of \(N^{inf}\) who initiate is 28.7%, or about half the initiation rate with \(g_{IT}\). The cap has a large mechanical effect on the distribution of embryos transferred (see Figure 8), which in turn yields a substantial shift in the distribution of births (Figure 9). As a consequence, the share of patients with births (7.7%) declines more steeply than the initiation rate. The estimated stage 4 function \(f_k(k|x, Z)\) implies a fairly high twin rate among single-embryo transfers at the clinic, so the number of delivered infants is 1.14 for every birth despite the single-embryo restriction.

Despite an initiation rate that is greater than that of \(g_N\), the embryo cap policy generates less consumer surplus ($5.6M) than the no-insurance scenario. Total insurance and delivery costs are substantially reduced in magnitude, to $7.3M and $8.4M respectively, but important differences exist between measures of costs per birth. Medical costs per birth fall by almost $30,000 relative to \(g_N\) and \(g_{IT}\), down to $38,900, due to the reduction in the numbers of twins and triplets. Patients require more IVF cycles to achieve a birth, however, so insurance expenses along with medical costs
results in total per-birth costs equal to $72,400, which is greater than the average in \( g_N \).

### 9.1.2 Top-up prices

Patients receive substantial value from the opportunity to transfer two or more embryos, which suggests that there may exist beneficial policies that allow patients to trade-off between the benefits and costs associated with transferring multiple embryos. The medical cost of multiple births are largely borne by insurers rather than the patients who choose treatment aggressiveness, which implies a traditional form of moral hazard (distinct from the demand-related version associated with \( g_{IT} \)) in which too much risky behavior occurs in equilibrium.

We construct top-up prices that are paid when a patient transfers two or more embryos. Let \( c_k \) be the average medical cost of a delivering \( k \) infants, and let \( Z \) denote the state variable values for a median-age treated patient with no additional fertility problems. We construct an (approximately) actuarially fair top-up price for transferring \( x > 1 \) embryos as:

\[
p_{x,A} = \sum_{k>1} (c_k - c_1)[f_k(k|x,Z) - f_k(k|1,Z)].
\]

This expression acknowledges that there is some multiple birth risk for patients transferring a single embryo, \( f_k(k|1,Z) \), but patients do not pay for this risk as part of the top-up price. Additionally, by including the cost difference \( (c_k - c_1) \) we exclude the expense of a singleton infant. Given the values of \( c_k \) provided above (roughly $27,000, $115,000, and $435,000 for singletons, twins, and triplets, respectively) and the probabilities in \( f_k \), the top-up price for two embryos is about $12,000, and three or four embryos each entail top-up prices of roughly $19,000.\(^{39}\) In our simulations, when a patient chooses to pay \( p_{x,A} > 0 \), we subtract this price from the summed medical costs of the full population’s treatment (as if the accumulated top-up prices are saved in a fund to pay for medical expenses.) In calculating patient utility from any \( x \), we remove the utility penalty \((\eta_0)\) for any transfer outside of ASRM guidelines.

This top-up price policy \( (g_{AT}) \) generates greater total consumer surplus ($7.8M) than \( g_N \) or \( g_C \), which leads to an IVF initiation rate that is greater as well. In addition, despite positive insurance cost of $8.3M under \( g_{AT} \), the medical cost of births decreases by $13.1M relative to \( g_N \). Together, these results imply that a policy of insured treatment for all patients, but with actuarially fair

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\(^{39}\)For example, a patient with \( Z = \bar{Z} \) who transfers 2 embryos experiences increases in her twin and triplet risks by 12 and 0.3 percentage points, respectively. Each change in risk is multiplied by the corresponding difference in medical cost relative to a singleton birth.
top-up prices, is welfare-improving for both consumers and the insurance firms that pay for IVF and birth costs. Reduced total costs for insurers could lead to lower premiums for patients in a competitive insurance market. The policy $g_{AT}$ has a slightly lower share of potential patients with a birth than $g_N$ (11.3% vs. 12.7%), but this is accompanied by a multiple-birth rate that declines substantially. The average number of infants per delivery is 1.24 under $g_{AT}$, which is about halfway between the rates of $g_N$ and $g_C$. The total cost per birth falls to $63,350 with $g_N$, which is the lowest value of all policies we consider in this paper. While both $g_C$ and $g_{AT}$ have per-birth medical costs of about $37,000, the greater per-treatment success rate of $g_{AT}$ drives total per-birth costs below those of $g_C$.

While $g_{AT}$ has several attractive properties relative to $g_N$ and $g_C$, the actuarially fair top-up prices can lead some patients to pay total prices that are substantially greater than under $g_N$. It is possible scale-down $g_{AT}$’s top-up prices to achieve a variety of policy objectives. For example, the top-up prices could be set so that total consumer surplus is equal to the empirical status quo, or they could be set so that total IVF and medical costs with top-up prices are equal to their level under $g_N$. We conclude our consideration of top-up prices with an additional example: prices that prevent any patient from paying a greater price for an IVF cycle than she would under $g_N$. We scale-down the actuarially fair prices (while keeping their proportions fixed) so that patients pay $5,000 to transfer a second embryo and $8,000 for three or four embryos. These payments are on top of the insured treatment prices, which total $3,000 for a full cycle with ICSI. Under $g_N$ a patient who uses ICSI and receives four embryos also pays $11,000. This policy of “moderate” top-up prices ($g_{MT}$) leads to 85% more patients initiating IVF than under $g_N$, and 62% more patients who ever experience a birth during the sample period. While total insurance plus medical costs are 68% greater with $g_{MT}$ relative to $g_N$, the per-birth medical plus insurance cost is only 3.3% greater.

### 9.2 Insuring outcomes

To highlight the scope of potential IVF policies and the impact of dynamics in this procedure, we study two outcome-focused insurance policies. In policy $g_{IO}$, we again expand insurance to the full population, but now with unlimited attempts at IVF for patients with one or fewer children when beginning a treatment cycle. In contrast to $g_{IT}$, which insures treatments, $g_{IO}$ is focused on outcomes. We also implement outcome-focused insurance with age-linked eligibility conditions. Patients under $g_{IA}$ who begin a cycle younger than age 35 receive the full benefit of $g_{IO}$, while patients with ages between 35 and 40 pay prices halfway between the uninsured price and the
insured one. (This amounts to a discount of about 35%.) Patients age 40 and above are completely excluded from insurance.

The treatment-focused policy $g_{IT}$ and the outcome-focused policy $g_{IO}$ have virtually identical effects on patient initiation, the probability of one or more births per patient, patient surplus, and insurance costs. The strong similarity between the two policies occurs because very few patients under $g_{IO}$ choose to take five or more cycles. In the eyes of most patients, the two policies are similarly generous. As expected, the policy with age-adjusted benefits, $g_{IA}$, has lower overall benefit to patients. Although older patients are most sharply affected by these limits, the differences in surplus and costs between $g_{IO}$ and $g_{IA}$ are not especially large. The older patients who would start treatment under $g_{IO}$ but not $g_{IA}$ are also the patients most likely to fail, so the share of patients with a birth falls by about 16% while insurance costs for treatment decline by 26%.

Comparisons across patient ages offer the best opportunity to examine differences between $g_{IO}$ and $g_{IA}$. In Figure 10 we graph the differences in expected value by age from initiating IVF for the first time. The largest difference in value is between ages 35 and 40, when insurance’s price benefit is reduced but not zero. Although the total reduction in price benefit is greater for patients above age 40, the reduced likelihood of a birth at these ages dampens the value difference between the policies. It is interesting to note that patients younger than age 35 also have a lower expected value of initiating treatment under $g_{IA}$. This is due to cycles after age 35 being subject to the reduced price benefit. Note that if patients were myopic, the two policies would have the same value for patients initiating before age 35. The dynamic effects of $g_{IA}$ are also apparent in simulated treatment histories for patients who initiate treatment between ages 33 and 35. Among patients who take more than one cycle in total, the average number of quarters between treatments is 6.0 under $g_{IO}$, but the patients under $g_{IA}$ delay 5.3 quarters on average. A similar reduction in delay occurs for patients who initiate between ages 35 and 40.

10 Conclusions

Healthcare policymakers face the challenge of designing policies that simultaneously improve access to care and contain costs. These challenges are particularly acute in the market for IVF, where treatment is costly, outcomes are uncertain, and there is substantial variation in insurance coverage for the procedure. A variety of policies have been proposed to address these issues, ranging from universal insurance mandates to cover IVF, to restrictions on treatment choice in the form of em-
bryo caps. To investigate the impact of these and other policies on patient welfare, outcomes, and healthcare costs, we estimate a structural dynamic model of the treatment choices made by infertile women undergoing IVF. Our framework incorporates important mechanisms influencing these decisions, including patient preferences, the evolution of patient health, IVF treatment technologies, and financial incentives. In addition to the treatment initiation decision, our model highlights the key tradeoff faced by women undergoing IVF: More aggressive treatment choices increase the likelihood of a birth, and so reduce future treatment costs, but also increase the possibility of potentially undesirable higher-order births. We apply the model to a unique dataset of women undergoing IVF treatment at a major clinic in the St. Louis, Missouri, area between 2001 and 2009. The clinic is situated such that it draws clients from both the Illinois side of the St. Louis metro area, where IVF is covered under a mandated insurance benefit, and the Missouri side, where it is not. Consequently, patients being treated at the clinic face very different financial incentives.

Counterfactual simulations from our model show that a universal mandate to cover IVF substantially increases patient welfare by increasing IVF use. However, the mandate also increases both treatment and birth costs. We find similar results for an outcome-based policy that insures births as opposed to treatment. Embryo caps have been proposed as a way to reduce the relatively high rates of expensive multiple births associated with IVF. We find that a policy of single embryo transfer (simultaneous with insured treatment) does indeed substantially lower aggregate costs, but this reduction is largely due to a reduction in patients who initiate treatment. Due to low birth probabilities with an embryo cap, the total cost per birth is greater than when no patients have insurance. In addition, our estimates imply that patients receive positive utility from twin births, which are limited under the embryo cap.

Given that neither unrestricted universal insurance nor embryo caps achieves the dual goals of increased access and lower per-birth costs, we propose a “value-based” policy in the spirit of Baicker et al. (2013) and Einav et al. (2016) in which all patients receive insurance coverage for the transfer of a single embryo, but then must pay a top-up price of $12,000 - $19,000 if they wish to transfer additional embryos. These prices are chosen to fully internalize the expected medical costs of more aggressive treatments. This policy generates more patient surplus than the embryo cap or the no-insurance baseline, and insurance plus medical costs are lower than the no-insurance baseline as well. In addition, there is room to reduce the top-up prices below their fully internalizing level in an effort to increase patient surplus while still achieving significant cost savings.

Our study of IVF has several contributions for other areas of health economics. We emphasize
the importance of how future treatment opportunities affect today’s choices, which is also important in several diseases with long-term treatment strategies, such as heart disease and cancer. Our consideration of top-up prices is relevant for insurance policy in areas where patients may have discretion over treatment approach, which can be particularly important in areas where compromises must be struck between patients’ utility and other medical concerns or costs. Finally, our framework illustrates the benefits of using a welfare approach to evaluate policies which may be different in structure (e.g. treatment- or outcome-based insurance) or different in goals (e.g. patients’ surplus or number of births).

The favorable outcomes of the top-up price policies naturally leads to a question of why these contracts have not yet emerged in the real world. To understand this, it is important to distinguish between plans offered by insurers under a mandate, versus offerings by insurers not subject to a mandate. In a setting without mandates, adverse selection and unravelling could result in individual insurers being unwilling to offer unilaterally any plans with IVF coverage. Our results show that, in principle, insurers could be better off under a mandate which allows them to coordinate offering coverage for IVF access while encouraging less aggressive embryo transfer behavior through embryo caps or top-up prices.
Appendix A: Distribution of Types Among Potential Patients

After estimating the model of decision making within the clinic, we know \( \hat{\theta} = (\hat{\varphi}, \hat{\zeta}, \hat{\rho}) \) and therefore \( W \left( Z_{a0}^D, \tau, g_E, \hat{\varphi}, \hat{\zeta} \right) \). We also know

\[
Pr \left( \tau = 2 | Z_{a0}^D I = 1, \hat{\rho} \right) = \Lambda([1, Z_{a0}^D] \bar{\rho}).
\]

(13)

In addition, from the treatment initiation model we know, for each possible \( \mu(z_r) \) and \( Z_{a0}^D \), the race-specific initiation rate among potential patients of each type. That is, we know

\[
\Lambda \left( W \left( Z_{a0}^D, \tau, \hat{\varphi}, \hat{\zeta} \right) - \mu(z_r) \right) \text{ for } \tau = 1, 2 \text{ and } z_r = 0, 1
\]

(14)

For each \( Z_{a0}^D \) we also know the total (i.e. unconditional on type) number of women of each race with other demographic characteristics \( Z_{a0}^D \) who came into the clinic. Let this number be \( N_{Z_{a0}}^{clin}(z_r) \). Together with \( Pr \left( \tau = 1 | Z_{a0}^D, I_i = 1, \bar{\rho} \right) \) we then have an estimate of the race-specific number of patients of type 1 with characteristics \( Z_{a0}^D \) who came into the clinic, say \( N_{Z_{a0},1,z_r}^{clin} \left( \bar{\rho} \right) \), where

\[
N_{Z_{a0},1,z_r}^{clin} \left( \bar{\rho} \right) = N_{Z_{a0}}^{clin}(z_r) \times \left[ 1 - f_{\tau} \left( \tau = 2 | Z_{a0}^D, I = 1, \bar{\rho} \right) \right].
\]

(15)

Similarly for type 2, we know:

\[
N_{Z_{a0},2,z_r}^{clin} \left( \bar{\rho} \right) = N_{Z_{a0}}^{clin}(z_r) \times f_{\tau} \left( \tau = 2 | Z_{a0}^D, I = 1, \bar{\rho} \right).
\]

(16)

Note that while \( N_{Z_{a0}}^{clin}(z_r) \) is data, \( [N_{Z_{a0},1,z_r}^{clin} \left( \bar{\rho} \right), N_{Z_{a0},2,z_r}^{clin} \left( \bar{\rho} \right)] \) depend on \( \rho \), which is identified by the differential behavior of the two types in the (within-clinic) patient histories. Recall that \( \rho \) parameterizes the within-clinic distribution of types and is estimated in our second step with \( (\varphi; \zeta) \).

Given \( \mu(z_r) \), from the initiation model we know that 100 \( \times \Lambda \left( W \left( Z_{a0}^D, \tau, \hat{\varphi}, \hat{\zeta} \right) - \mu(z_r) \right) \) percent of potential patients of a given race, with additional initial non-biological states \( Z_{a0}^D \) and type \( \tau \) will choose to initiate treatment. We also know that there we predict \( N_{Z_{a0},r,z_r}^{clin} \left( \bar{\rho} \right) \) patients of type \( \tau \). Then it must be the case that the number of potential patients of each type, with that combination
of demographic states $Z_{a0}^D$ and for that race is given by

$$N_{Z_{a0,1},zr}^{\text{inf}} = \frac{N_{Z_{a0,1},zr}^{\text{clin}}(\hat{\rho})}{\Lambda \left(W \left(Z_{a0}^D, \tau = 1; \hat{\varphi}, \hat{\zeta} \right) - \mu(z_r) \right)} = \frac{N_{Z_{a0}^D}^{\text{clin}}(z_r) \left[1 - \Lambda([1, Z_{a0}^D]\hat{\rho}) \right]}{\Lambda \left(W \left(Z_{a0}^D, \tau = 1; \hat{\varphi}, \hat{\zeta} \right) - \mu(z_r) \right)},$$  

(17)

$$N_{Z_{a0,2},zr}^{\text{inf}} = \frac{N_{Z_{a0,2},zr}^{\text{clin}}(\hat{\rho})}{\Lambda \left(W \left(Z_{a0}^D, \tau = 2; \hat{\varphi}, \hat{\zeta} \right) - \mu(z_r) \right)} = \frac{N_{Z_{a0}^D}^{\text{clin}}(z_r) \Lambda([1, Z_{a0}^D, z_r]\hat{\rho})}{\Lambda \left(W \left(Z_{a0}^D, \tau = 2; \hat{\varphi}, \hat{\zeta} \right) - \mu(z_r) \right)},$$  

(18)

Then we can estimate the unconditional (i.e. not conditional on $I = 1$) prevalence of type 2 among potential patients of that race with state $Z_{a0}^D$ as

$$f_{\tau|z_r}(\tau = 2|Z_{a0}^D) \approx \frac{N_{Z_{a0,2},zr}^{\text{inf}}}{N_{Z_{a0,1},zr}^{\text{inf}} + N_{Z_{a0,2},zr}^{\text{inf}}} = \left(1 + \frac{1 - \Lambda([1, Z_{a0}^D]\hat{\rho})}{\Lambda([1, Z_{a0}^D]\hat{\rho})} \right)^{-1}.$$  

(19)

Note that for given $\mu(z_r)$, everything in the RHS is known, so $f_{\tau|z_r}(\tau = 2|Z_{a0}^D)$ is known and so is $f_{\tau|z_r}(\tau = 1|Z_{a0}^D) = 1 - f_{\tau|z_r}(\tau = 2|Z_{a0}^D, z_r)$. If, for a given race, both types were to select into the clinic at the same rate (i.e. they do not really have different preferences for children), we would have $W \left(Z_{a0}^D, \tau = 1; g_E, \theta \right) = W \left(Z_{a0}^D, \tau = 2; g_E, \theta \right)$ so $\Lambda(W(Z_{a0}^D, \tau = 1; \theta) - \mu(z_r)) = \Lambda(W(Z_{a0}^D, \tau = 2; \theta) - \mu(z_r)) = 1$ and the distribution of types within the clinic and among potential patients would be the same, $f_{\tau|z_r}(\tau = 2|Z_{a0}^D, I = 1) = f_{\tau|z_r}(\tau = 2|Z_{a0}^D)$, which is not consistent with our estimates.

**Appendix B: Approximating $N^{\text{inf}}$ and $f_{ZD}(Z_{a0}^D)$**

To obtain a model-predicted IVF initiation rate among potential patients of each race we must use an estimate of $f_{ZD|z_r}(Z_{a0}^D)$. Note that since the expected value of initiation depends on $Z_{a0}^D$, the distribution of $Z_{a0}^D$ among patients who initiate differs from the distribution among potential patients. In particular, we expect active patients at the clinic to be older, more likely to be covered by insurance, wealthier, and less likely to be African American. To approximate $f_{ZD}(Z_{a0}^D)$ among potential patients we use the following assumptions:

- **Assumption 0 (Exogenous ASRM Guidelines).** The particular ASRM guidelines in place are independent of everything else in the model:

$$\text{asrm} \perp (Z^B, t_{a0}, z_w, a_0, z_r).$$  

(20)
• **Assumption 1 (Conditional Independence).** Conditional on age at initiation, the 3 biological state variables related to infertility, $Z^B$, are independent of insurance, wealth and race:

$$Z^B \perp (t_0, z_w, z_r) \mid a_0. \quad (21)$$

Note that Assumption 1 and the fact that the value of $Z^B$ only becomes observable after deciding to start a first cycle, imply that these variables will have the same conditional (on age) distribution in the risk set and in the clinic:

$$f(Z^B | a_0) = f(Z^B | a_0, I = 1). \quad (22)$$

• **Assumption 2 (Surprise).** Individuals only become aware of their infertility at age $a_0$. Therefore, the joint distribution of wealth and insurance coverage among women at $a_0$ should be independent of whether they have any infertility problem (i.e. independent of whether they are among the potential patients or not). Therefore, $\Pr(t_{a_0}, z_w, z_r | a_0)$ is the same regardless of whether a woman is a potential patient or not. We further assume that $\Pr(t_{a_0}, z_w, z_r | a_0) = \Pr(t_{a_0}, z_w, z_r)$ for all $a_0$.

Using these assumptions we can approximate the joint distribution of all state variables among potential patients as $f_Z(Z_{a_0}) = f_Z(Z^D_{a_0}, Z^B_{a_0}) = f_{Z^B}(Z^D_{a_0}) f_{Z^D_{a_0}}(Z^D_{a_0})$.

First note that by Assumptions 0 and 1, $f_{Z^B}(Z^D_{a_0}) = f_{Z^B}(Z^D_{a_0} | a_0) = f_{Z^B}(Z^D_{a_0}, I = 1)$ and we can easily construct an estimate $\hat{f}_{Z^B}(Z^D_{a_0}, I = 1)$ using patient data. So we only need to focus on $f_{Z^D_{a_0}}(Z^D_{a_0})$, which is the critical input for the share-matching procedure described in Section 7.2.

By Assumption 0,

$$f_{Z^D_{a_0}}(Z^D_{a_0}) = f_{a_0,t_{a_0},z_w,z_r}(a_0, t_{a_0}, z_w, z_r) f_{asrm}(z_{asrm a_0}). \quad (23)$$

To estimate $f_{a_0,t_{a_0},z_w,z_r}(a_0, t_{a_0}, z_w, z_r)$ we note that

$$f_{a_0,t_{a_0},z_w,z_r}(a_0, t_{a_0}, z_w, z_r) = f_{a_0,t_{a_0},z_w,z_r}(a_0, t_{a_0}, z_w | z_r) f_{z_r}(z_r)$$

$$= f_{a_0 | z_r}(a_0 | z_r) f_{t_{a_0},z_w,z_r}(t_{a_0}, z_w | z_r) f_{z_r}(z_r)$$

**Distribution of age among potential patients.** We first estimate $f_{a_0 | z_r}(a_0 | z_r)$ using data from the St. Louis region on (first) births and the maternal age associated with those births, by
race. Also because of Assumption 2, this gives us the distribution of age at first attempted birth (regardless of whether the attempt was successful or not) when combined with estimates of race-specific infertility rates by age. This provides the race-specific age distribution for our potential patients.

**Joint distribution of IVF coverage and wealth.** Finally we collect data on the joint distribution of IVF coverage and wealth, \((t, z_w)\) conditional on race. To estimate \(f_{t_{a_0}, z_w | z_r}(t_{a_0}, z_w | z_r)\) we consider

\[
f_{t_{a_0}, z_w | z_r}(t_{a_0}, z_w | z_r) = f_{t_{a_0} | z_w, z_r}(t_{a_0} | z_w, z_r) f_{z_w | z_r}(z_w | z_r)
\]

and develop a strategy at the zip code level for estimating \(f_t(t | z_w)\) and \(f_{z_w | z_r}(z_w | z_r)\) using information from zip codes whose center is located within 75 miles from our clinic. To estimate \(f_{z_w | z_r}(z_w | z_r)\) we assume patients from same zip code are homogenous regarding \((t, z_w)\). In particular, we know whether each zip code in the St. Louis area is considered “wealthy” or not by construction: we defined \(z_w;l = 1\) if zip code \(l\)’s median home value is above $100,000. This is consistent with the way we are defining a patient to be “wealthy” or not (i.e. whether she comes from a zip code where the median home value is above $100,000). We estimate \(f_{z_w | z_r}(z_w | z_r)\) by

\[
f_{z_w | z_r}(z_w = 1 | z_r) = \sum_{l \in STL} I \{z_w;l = 1\} \left\{ \frac{P^z_r l}{\sum_{m \in STL} P^z_r m} \right\}
\]

(24)

where \(P^z_r l\) is the population of a given race \((z_r)\) in zip code \(l\) within the St. Louis region. We have the population by race for each zip code, so we can construct \(P^z_r l\) easily.

To estimate \(Pr (t | w)\) we take the following steps. We have the percentage of population who have private insurance for each zip code \(l\) within the St. Louis area: \(f_{priv} (priv_l)\). We obtain this from the 2012 American Community Survey (ACS) 5-year estimate. A 2005 Mercer Survey of Employer Health Insurance reported that 19 percent of those with large (500+ employees) employer-provided health insurance have IVF coverage, and 11 percent of those working for small employers do so. We assume the same rates apply to Missouri zip codes. We then use estimates from Census’s Business Dynamics Statistics as reported by Moscarini and Postel-Vinay (2012) and estimate the employment share of large employers to be 48%.

40 See Table 1 in Moscarini and Postel-Vinay (2012)
factor $\psi^{MO} = 0.52 \times 0.11 + 0.48 \times 0.19 = 0.15$ to adjust the raw insurance coverage rates we obtain from ACS. Then the IVF coverage for each Missouri zip code $l$ is given by $f_{IVF}(t_{IVF}^l) = f_{priv}(priv_l) \times \psi^{MO}$.

Regarding Illinois counties, we know that there is a mandate. But small employers ($< 25$ employees) and self-insured employers (regardless of size) are excluded.\textsuperscript{41} According to a Kaiser Family Foundation (2007) report, 55% of workers nationally are covered by plans that are partially or fully self-insured.\textsuperscript{42} So we adjust the raw county-level employer-sponsored health insurance coverage rate by the percentage of large employers and the percentage not self-funded and assume that no firm with less than 25 employees provides IVF coverage. We obtain the following adjustment factor for Illinois counties $\psi^{IL} = (0.215 \times 0 + 0.785 \times [0.45 \times 1 + 0.55 \times 0.19]) = 0.435$. Then the IVF coverage for each Illinois zip code $l$ is given by: $f_{IVF}(t_{IVF}^l) = f_{priv}(priv_l) \times \psi^{IL}$.

We then compute the aggregate IVF coverage rate for the region conditional on wealth. First, we condition on $z_w = 0$ and compute

\[
\Pr (t = 4|z_w = 0) = \sum_{l: z_w = 1} f_{IVF}(t_{IVF}^l) \left( \frac{\pi_l}{\sum_{l: z_w = 1} \pi_l} \right).
\]

Regarding coverage conditional on high wealth ($z_w = 1$) we take a different approach. Since most of the wealthy zip codes are on the Missouri side but $\psi^{MO}$ is very low relative to $\psi^{IL}$, if we pool zip codes together in the aggregation we would end up with a spurious negative correlation. Therefore we compute $\Pr (t = 4|z_w = 1)$ in the following way:

\[
\Pr (t = 4|z_w = 1) = \Pr (t = 4|z_w = 0) + \Delta,
\]

where

\[
\Delta = \left( \frac{\sum_{l: z_w = 1, l \in IL} \pi_l}{\sum_{l: z_w = 1} \pi_l} \right) \Delta_{IL} + \left( \frac{\sum_{l: z_w = 1, l \in MO} \pi_l}{\sum_{l: z_w = 1} \pi_l} \right) \Delta_{MO}.
\]

\textsuperscript{41}Under this alternative definition of small employer, we interpolate the numbers in Moscarini and Postel-Vinay and find that 21.5% of employment is accounted for by firms with less than 25 employees.

\textsuperscript{42}We assume that in these self-funded plans the same rate found in the Mercer survey (19%) for large employers applies. This is probably an upper bound because large employers here also include firms with 25 to 499 employees, not just those with 500+ as in the Mercer study definition.
\( \hat{\Delta}_s \) provides the estimated average increase in IVF coverage observed for state \( s \) when one moves from poor zip codes to wealthy zip codes within that state.

\[
\hat{\Delta}_s = \left[ \sum_{l:w_l=1,l \in s} f_{IVF}(IVF_l) \left( \frac{\pi_l}{\sum_{l:w_l=1,l \in s} \pi_l} \right) \right] - \left[ \sum_{l:w_l=0,l \in s} f_{IVF}(IVF_l) \left( \frac{\pi_l}{\sum_{l:w_l=0,l \in IL} \pi_l} \right) \right]
\]

for \( s = \text{IL, MO} \). The results indicate that IVF insurance coverage rate depends of wealth. Among poor potential patients, 83% have \( \iota = 0 \) and 17% have \( \iota = 4 \). For wealthy potential patients, 75% have \( \iota = 0 \) and 25% have \( \iota = 4 \).

**Size of Potential Patient Pool.** In addition to the joint distribution of characteristics among potential patients, we need the size of the potential patient pool \( N^{inf} \). We use \( \bar{N}^{inf} \) to refer to all potential patients in the St. Louis area, and \( N^{inf} \) for the subset who might consider the clinic we study. We count the race-specific number of women of each age in the St. Louis region that give birth naturally to a first birth in any given quarter. Let this number be \( \bar{N}_{a,zr} \), which we obtain from Vital Statistics. The total number of women who attempt their first pregnancy at age \( a \) is \( N_{stl}^{inf} \). Of these, \( \bar{N}_{a,zr} \) succeed and have births recorded in Vital Statistics; the group that fails, \( \bar{N}^{inf}_{a,zr} \), contributes to our set of potential patients. Therefore \( N_{stl}^{inf} = \bar{N}_{a,zr} + \bar{N}^{inf}_{a,zr} \).

Then using infertility rates by age and race among women who are attempting to get pregnant, \( inf(a,z_r) \), we back out \( \bar{N}^{inf}_{a,zr} = \frac{inf(a,z_r)}{[1-inf(a,z_r)]} \bar{N}_a \). According to Vital Statistics, the larger counties in and around the St. Louis region have an average of 1172 first births each quarter distributed among mothers aged 28 to 44. To capture births occurring in the more rural areas, but still within our 75-mile radius area, we also estimate the births occurring in smaller counties within this area. An additional 10.4% of births come from these counties.\(^{43}\) So \( \bar{N}_{28-44}^{75m} = 1172 \times 1.104 = 1294 \). Using infertility rates by age and race and summing across ages, we can then determine that there are \( \bar{N}_i^{inf} = 257 \times 1.104 = 284 \) new potential patients, on average, each quarter.\(^{44}\) Since there are 28 quarters between 2001 and 2007, the size of the potential patient pool for our sample period is then \( \bar{N}^{inf}_{2001-07} = 28 \times \bar{N}^{inf} = 28 \times 284 = 7944 \). While this pool of potential patients is valid for the full St. Louis area, our clinic has market share \( s^{clin} < 1 \). According to the CDC, the clinic we observe

\(^{43}\)Births occurring in smaller counties are combined and reported into a single residual county for each state in Vital Stats. So we know how many first births occurred in these “residual” counties. We also know how important (in terms of number of households) the zipcodes belonging to small counties but located within the 75-mile radius are as a share of the each state specific residual county. Therefore we can augment the number of births in the relevant area by assuming that the same share of births comes from these zipcodes.

\(^{44}\)To obtain age-specific infertility rates \( inf(a,z_r) \), we interpolate between ages 28 to 39 and extrapolate for ages 40-44 the 12-month infertility estimates reported in Dunson et al. (2004) and adjust these estimates using relative rates of infertility between black and white women from based on data from NSFG.
has market share of about a third, and we adjust $\tilde{N}^{inf}_{2001-07}$ in a proportional way. Ultimately the potential-patient population for our clinic is $N^{inf} = 2781$. Of these, 486 are black and 2295 are non-black.

References


Figure 1: IVF treatment stages

Stage 1 / Period start

If already initiated

Delay

Start \( \epsilon_s,1 \)

\( \epsilon_d,1 + \beta EW_1(Z_{a+1}) \)

Learn Peak E2

Go to next period

If at initiation decision

Start

No initiation

Learn \( Z^B \)

\( W_{OUT} = \mu + \nu \)

Stage 2

Stage 3

Stage 4

Learn # eggs (r)

No ICSI

ICSI

Learn embryos (X)

Choose \( x \leq X \)

\[ \Sigma_{k>0} f_k(k|x) \left[ U(k|\tilde{k}, \tau) + \beta^4 EW_1(Z_{a+4}) \right] + f_k(0|x) \beta EW_1(Z_{a+1}) + \epsilon_{x,4} \]

Go to next period

Go to next period

Note: We display patients' immediate payoffs at each stage of the decision tree, and include expected future payoffs only where the patient has reached the end of a within-period decision sequence. We omit some notation to avoid clutter.
**Figure 2: Distribution of Peak E2 Outcomes by AFC**

**Figure 3: Distribution of Retrieved Egg Count by Peak E2**
Figure 4: Distribution of Embryos Available by ICSI Use, Male Factor Patients

Figure 5: Distribution of Births by Embryos Transferred, Patient Age 34-36
Figure 6: Distribution of Births by Patient Age, 3 embryos

Figure 7: Predicted Stage 4 Decisions on Embryos Transferred
Figure 8: Embryo Transfer Choices in Counterfactual Experiments

Notes: N = No insurance. IT = Universal insurance for treatment. AT = Insurance plus actuarially fair top-up prices. MT = Insurance plus “moderate” top-up prices.
Figure 9: Births Outcomes in Counterfactual Experiments

Notes: N = No insurance. IT = Universal insurance for treatment. AT = Insurance plus actuarially fair top-up prices. MT = Insurance plus “moderate” top-up prices.
Notes: Vertical axis plots difference between expected value from policy IO (Universal insured outcome) minus IA (Insured outcome with age-adjusted benefits.)
Table 1: This Paper’s Clinic in Context

<table>
<thead>
<tr>
<th></th>
<th>This Paper’s Clinic</th>
<th>All U.S. Clinics</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of cycles per year</td>
<td>370.2</td>
<td>217.1</td>
</tr>
<tr>
<td>Patient median age</td>
<td>34</td>
<td>35-37 (see note)</td>
</tr>
<tr>
<td>Patients with 2+ infertility diagnoses</td>
<td>11%</td>
<td>12%</td>
</tr>
<tr>
<td>Male partners with infertility diagnosis</td>
<td>18%</td>
<td>17%</td>
</tr>
<tr>
<td>ICSI use</td>
<td>50%</td>
<td>59%</td>
</tr>
<tr>
<td>Embryos per cycle</td>
<td>2.41</td>
<td>2.68</td>
</tr>
<tr>
<td>Birth rate per cycle</td>
<td>33.5%</td>
<td>29.9%</td>
</tr>
</tbody>
</table>

Note: We use our main data sample to calculate patient median age for the clinic we study. For all other statistics we use the annual summary data published by the CDC for the clinic we study and the U.S. as a whole. In the CDC’s data patient ages are reported in intervals.
Table 2: Patient-level Characteristics

<table>
<thead>
<tr>
<th></th>
<th>Main sample N = 587</th>
<th>First-stage sample N = 1106</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Mean</td>
<td>Std. dev.</td>
</tr>
<tr>
<td><strong>Demographic state variables ((Z_D))</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Patient age at initiation</td>
<td>34.30</td>
<td>4.02</td>
</tr>
<tr>
<td>Insured at initiation? ((Y = 1))</td>
<td>0.54</td>
<td>0.50</td>
</tr>
<tr>
<td>Wealthy zip code? ((Y = 1))</td>
<td>0.82</td>
<td>0.39</td>
</tr>
<tr>
<td>Prior children at initiation</td>
<td>0.00</td>
<td>0.00</td>
</tr>
<tr>
<td>African American? ((Y = 1))</td>
<td>0.05</td>
<td>0.21</td>
</tr>
<tr>
<td><strong>Biological state variables ((Z_B))</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>AFC score</td>
<td>14.37</td>
<td>7.96</td>
</tr>
<tr>
<td>Female fertility problem? ((Y = 1))</td>
<td>0.80</td>
<td>0.40</td>
</tr>
<tr>
<td>Male fertility problem? ((Y = 1))</td>
<td>0.34</td>
<td>0.48</td>
</tr>
<tr>
<td><strong>Aggregate actions and outcomes</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Total cycles</td>
<td>1.75</td>
<td>1.02</td>
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<tr>
<td>Birth during sample period? ((Y = 1))</td>
<td>0.53</td>
<td>0.50</td>
</tr>
</tbody>
</table>

The “Main sample” is used in second-stage estimation of patients’ choices. The “First-stage sample” is used to estimate treatment technologies.
Table 3: Actions and Outcomes within Treatment

<table>
<thead>
<tr>
<th></th>
<th>Main sample</th>
<th>First-stage sample</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>N</td>
<td>Mean</td>
</tr>
<tr>
<td><strong>Stage 1-4 actions</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Cancel treatment? (Y = 1)</td>
<td>1027</td>
<td>0.14</td>
</tr>
<tr>
<td>Fertilization method? (ICSI = 1)</td>
<td>879</td>
<td>0.60</td>
</tr>
<tr>
<td>Number of embryos transferred</td>
<td>875</td>
<td>2.29</td>
</tr>
<tr>
<td><strong>Stage 1-3 outcomes</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Peak E2 score</td>
<td>1027</td>
<td>16.82</td>
</tr>
<tr>
<td>Eggs retrieved</td>
<td>879</td>
<td>10.60</td>
</tr>
<tr>
<td>Embryos generated</td>
<td>881</td>
<td>6.11</td>
</tr>
<tr>
<td>4+ embryos? (Y = 1)</td>
<td>881</td>
<td>0.74</td>
</tr>
<tr>
<td><strong>Stage 4 outcomes</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Children born</td>
<td>848</td>
<td>0.51</td>
</tr>
<tr>
<td>Singleton birth? (Y = 1)</td>
<td>848</td>
<td>0.27</td>
</tr>
<tr>
<td>Twin birth? (Y = 1)</td>
<td>848</td>
<td>0.12</td>
</tr>
<tr>
<td>Triplet birth? (Y = 1)</td>
<td>848</td>
<td>0.00</td>
</tr>
</tbody>
</table>

The "Main sample" is used in second-stage estimation of patients’ choices. The "First-stage sample" is used to estimate treatment technologies.
Table 4: Utility Parameter Estimates

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Estimate (SE)</th>
<th>Estimate (SE)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Utility of 1 birth ( u_1 )</td>
<td>5.143 (0.928)</td>
<td>Price sensitivity constant ( \alpha_0 )</td>
</tr>
<tr>
<td>Utility of 2 births ( u_2 )</td>
<td>5.866 (1.682)</td>
<td>Price sensitivity X wealth ( \alpha_w )</td>
</tr>
<tr>
<td>Utility of 3 births ( u_3 )</td>
<td>-14.095 (4.411)</td>
<td>Terminal payoff ( \gamma ) X Prev. payment ( \gamma )</td>
</tr>
<tr>
<td>Utility shift when ( k &gt; 0 ) ( \kappa )</td>
<td>-11.868 (0.956)</td>
<td>Utility shift from beginning treatment ( \delta )</td>
</tr>
<tr>
<td>Preference shifter ( \zeta )</td>
<td>9.768 (0.865)</td>
<td>Penalty for violating ASRM embryo guidelines ( \eta_0 )</td>
</tr>
</tbody>
</table>

Standard errors are in parentheses.

Table 5: Utility-Type Distribution Parameter Estimates

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Estimate (SE)</th>
<th>Estimate (SE)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Constant ( \rho_0 )</td>
<td>-1.269 (0.552)</td>
<td>Insurance ( \rho_3 )</td>
</tr>
<tr>
<td>Age ( \rho_1 )</td>
<td>0.041 (0.013)</td>
<td>ASRM regime ( \rho_4 )</td>
</tr>
<tr>
<td>Wealth ( \rho_2 )</td>
<td>-0.864 (0.457)</td>
<td>Race ( \rho_5 )</td>
</tr>
</tbody>
</table>

Standard errors are in parentheses.
<table>
<thead>
<tr>
<th>Policy setting ((g))</th>
<th>Share initiating</th>
<th>N cycles if initiate</th>
<th>Share with birth</th>
<th>N births</th>
<th>N infants</th>
</tr>
</thead>
<tbody>
<tr>
<td>Empirical Baseline (E)</td>
<td>0.299</td>
<td>1.348</td>
<td>0.159</td>
<td>456.2</td>
<td>636.4</td>
</tr>
<tr>
<td></td>
<td>(0.295, 0.305)</td>
<td>(1.280, 1.445)</td>
<td>(0.148, 0.173)</td>
<td>(422.1, 496.8)</td>
<td>(584.6, 691.1)</td>
</tr>
<tr>
<td><strong>Insured treatment policies</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>No insurance (N)</td>
<td>0.242</td>
<td>1.277</td>
<td>0.127</td>
<td>360.7</td>
<td>505.2</td>
</tr>
<tr>
<td></td>
<td>(0.227, 0.258)</td>
<td>(1.204, 1.396)</td>
<td>(0.113, 0.145)</td>
<td>(321.3, 413.3)</td>
<td>(446.0, 576.4)</td>
</tr>
<tr>
<td>Universal insurance for treatment (IT)</td>
<td>0.577</td>
<td>1.426</td>
<td>0.315</td>
<td>902</td>
<td>1245.2</td>
</tr>
<tr>
<td></td>
<td>(0.512, 0.625)</td>
<td>(1.365, 1.507)</td>
<td>(0.281, 0.347)</td>
<td>(808.0, 997.5)</td>
<td>(1114.0, 1373.0)</td>
</tr>
<tr>
<td>IT + embryo cap (C)</td>
<td>0.287</td>
<td>1.238</td>
<td>0.077</td>
<td>217.9</td>
<td>247.4</td>
</tr>
<tr>
<td></td>
<td>(0.226, 0.342)</td>
<td>(1.127, 1.357)</td>
<td>(0.061, 0.093)</td>
<td>(172.7, 263.4)</td>
<td>(197.2, 300.6)</td>
</tr>
<tr>
<td>IT + actuarially fair top-up prices (AT)</td>
<td>0.323</td>
<td>1.271</td>
<td>0.113</td>
<td>320.5</td>
<td>397.7</td>
</tr>
<tr>
<td></td>
<td>(0.280, 0.373)</td>
<td>(1.181, 1.396)</td>
<td>(0.100, 0.130)</td>
<td>(282.3, 371.6)</td>
<td>(349.0, 476.7)</td>
</tr>
<tr>
<td>IT + moderate top-up prices (MT)</td>
<td>0.449</td>
<td>1.356</td>
<td>0.206</td>
<td>586.7</td>
<td>778.8</td>
</tr>
<tr>
<td></td>
<td>(0.407, 0.485)</td>
<td>(1.297, 1.461)</td>
<td>(0.183, 0.231)</td>
<td>(523.6, 656.1)</td>
<td>(688.6, 881.5)</td>
</tr>
<tr>
<td><strong>Insured outcome policies</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Universal insurance for outcomes (IO)</td>
<td>0.576</td>
<td>1.412</td>
<td>0.311</td>
<td>883.2</td>
<td>1210.8</td>
</tr>
<tr>
<td></td>
<td>(0.511, 0.625)</td>
<td>(1.353, 1.494)</td>
<td>(0.277, 0.343)</td>
<td>(788.9, 980.1)</td>
<td>(1081.9, 1336.5)</td>
</tr>
<tr>
<td>Age-adjusted insurance for outcomes (IA)</td>
<td>0.484</td>
<td>1.4</td>
<td>0.278</td>
<td>787.6</td>
<td>1087.9</td>
</tr>
<tr>
<td></td>
<td>(0.442, 0.517)</td>
<td>(1.337, 1.486)</td>
<td>(0.251, 0.307)</td>
<td>(712.6, 869.7)</td>
<td>(979.2, 1194.9)</td>
</tr>
</tbody>
</table>

95% confidence intervals are in parentheses
Table 7: Surplus and Costs across Policy Settings

<table>
<thead>
<tr>
<th>Policy setting (g)</th>
<th>Total surplus in risk population ($M)</th>
<th>Total IVF insurance cost ($M)</th>
<th>Total medical delivery cost ($M)</th>
<th>Medical cost per birth ($000)</th>
<th>Insurance + medical cost per birth ($000)</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Empirical Baseline (E)</strong></td>
<td>10.3</td>
<td>3.6</td>
<td>31.4</td>
<td>68.9</td>
<td>76.9</td>
</tr>
<tr>
<td></td>
<td>( 8.3, 13.7)</td>
<td>( 3.1, 4.0)</td>
<td>(28.6, 33.9)</td>
<td>(66.9, 69.5)</td>
<td>( 74.4, 77.7)</td>
</tr>
<tr>
<td><strong>Insured treatment policies</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>No insurance (N)</td>
<td>7.6</td>
<td>0</td>
<td>25.0</td>
<td>69.4</td>
<td>69.4</td>
</tr>
<tr>
<td></td>
<td>( 5.6, 10.8)</td>
<td>( 0.0, 0.0)</td>
<td>(21.8, 28.5)</td>
<td>(67.0, 70.0)</td>
<td>( 67.0, 70.0)</td>
</tr>
<tr>
<td>Universal insurance for treatment (IT)</td>
<td>18.4</td>
<td>16.4</td>
<td>60.5</td>
<td>67.1</td>
<td>85.2</td>
</tr>
<tr>
<td></td>
<td>(16.0, 22.4)</td>
<td>(14.6, 18.0)</td>
<td>(54.4, 66.8)</td>
<td>(65.9, 68.2)</td>
<td>( 84.4, 86.2)</td>
</tr>
<tr>
<td>IT + embryo cap (C)</td>
<td>5.6</td>
<td>7.3</td>
<td>8.5</td>
<td>38.9</td>
<td>72.4</td>
</tr>
<tr>
<td></td>
<td>( 4.4, 7.4)</td>
<td>( 5.7, 8.8)</td>
<td>( 6.8, 10.4)</td>
<td>(38.8, 39.7)</td>
<td>( 71.8, 73.8)</td>
</tr>
<tr>
<td>IT + actuarially fair top-up prices (AT)</td>
<td>7.8</td>
<td>8.3</td>
<td>11.9</td>
<td>37.1</td>
<td>63.1</td>
</tr>
<tr>
<td></td>
<td>( 6.0, 11.4)</td>
<td>( 7.3, 9.7)</td>
<td>(10.5, 13.8)</td>
<td>(36.0, 38.4)</td>
<td>( 59.4, 66.2)</td>
</tr>
<tr>
<td>IT + moderate top-up prices (MT)</td>
<td>13.3</td>
<td>12.2</td>
<td>29.9</td>
<td>50.9</td>
<td>71.7</td>
</tr>
<tr>
<td></td>
<td>(10.5, 17.9)</td>
<td>(11.1, 13.7)</td>
<td>(26.1, 34.3)</td>
<td>(48.4, 52.7)</td>
<td>( 70.4, 72.7)</td>
</tr>
<tr>
<td><strong>Insured outcome policies</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Universal insurance for outcomes (IO)</td>
<td>18.5</td>
<td>16.2</td>
<td>58.3</td>
<td>66.1</td>
<td>84.4</td>
</tr>
<tr>
<td></td>
<td>(16.0, 22.6)</td>
<td>(14.5, 18.0)</td>
<td>(52.4, 64.4)</td>
<td>(64.9, 67.2)</td>
<td>( 83.6, 85.4)</td>
</tr>
<tr>
<td>Age-adjusted insurance for outcomes (IA)</td>
<td>15.7</td>
<td>12.0</td>
<td>52.7</td>
<td>66.9</td>
<td>82.1</td>
</tr>
<tr>
<td></td>
<td>(13.3, 19.6)</td>
<td>(10.7, 13.3)</td>
<td>(46.8, 57.5)</td>
<td>(65.2, 67.7)</td>
<td>( 80.5, 82.8)</td>
</tr>
</tbody>
</table>

95% confidence intervals are in parentheses